

# Optoelectrică

Curs 4

2017/2018

# Disciplina 2017/2018

- ▶ 2C/1L Optoelectronicaă **OPTO**
- ▶ **Minim 7 prezente curs + laborator**
- ▶ Curs – **sl. Radu Damian**
  - an IV μE
  - Vineri 8–11, P5
  - E – 70% din nota
    - **20% test la curs**, saptamana 4–5?
  - probleme + (? 1 subiect teorie) + (2p prez. curs)
  - **toate materialele permise**
- ▶ Laborator – **sl. Daniel Matasaru**
  - an IV μE, an IV Tc
    - Joi 14-16 par/impar
  - L – 15% din nota
  - C – 15% din nota

# Orar 2017/2018

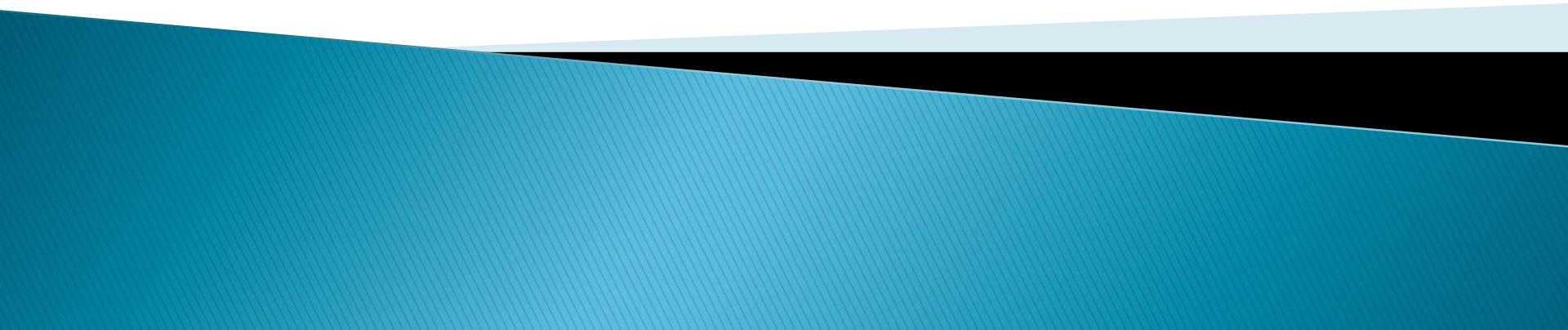
## ► Curs

- Vineri 8-11, P5
- **2C ⇒ 3C**
  - $14 \cdot 2 / 3 \approx 9.33$
  - 9÷10 C

# Examen partial 2017/2018

- ▶ Vineri 16.03.2018, 10, P5
  - toate materialele permise
- ▶ 20% nota
  - Singura probă la care minim 5 nu e necesar
  - Absenta = 0p
- ▶ Primele 3 capitole
  - Introducere
  - Lumina ca undă electromagnetică
  - Fotometrie și radiometrie

# Recapitulare



# Reprezentare logaritmică!!!

$$\text{dB} = 10 \cdot \log_{10} (P_2 / P_1)$$

$$\text{dBm} = 10 \cdot \log_{10} (P / 1 \text{ mW})$$

$$0 \text{ dB} = 1$$

$$+ 0.1 \text{ dB} = 1.023 (+2.3\%)$$

$$+ 3 \text{ dB} = 2$$

$$+ 5 \text{ dB} = 3$$

$$+ 10 \text{ dB} = 10$$

$$-3 \text{ dB} = 0.5$$

$$-10 \text{ dB} = 0.1$$

$$-20 \text{ dB} = 0.01$$

$$-30 \text{ dB} = 0.001$$

$$0 \text{ dBm} = 1 \text{ mW}$$

$$3 \text{ dBm} = 2 \text{ mW}$$

$$5 \text{ dBm} = 3 \text{ mW}$$

$$10 \text{ dBm} = 10 \text{ mW}$$

$$20 \text{ dBm} = 100 \text{ mW}$$

$$-3 \text{ dBm} = 0.5 \text{ mW}$$

$$-10 \text{ dBm} = 100 \mu\text{W}$$

$$-30 \text{ dBm} = 1 \mu\text{W}$$

$$-60 \text{ dBm} = 1 \text{ nW}$$

$$[\text{dBm}] + [\text{dB}] = [\text{dBm}]$$

$$[\text{dBm}/\text{Hz}] + [\text{dB}] = [\text{dBm}/\text{Hz}]$$

$$[x] + [\text{dB}] = [x]$$

# Lumina ca undă electromagnetică

Capitolul 2

# Parametri, dependenta de mediu

$$\eta_0 = \sqrt{\frac{\mu_0}{\epsilon_0}} = 377\Omega$$

$$c_0 = \frac{1}{\sqrt{\epsilon_0 \cdot \mu_0}} = 2,99790 \cdot 10^8 \text{ m/s}$$

$n=1$

$$T = \frac{2\pi}{\omega} = \frac{1}{f}$$

$$\lambda_0 = \frac{2\pi}{\beta} = \frac{c_0}{f}$$

$$\eta = \frac{\eta_0}{n}$$

$$c = \frac{c_0}{n}$$

$n = \sqrt{\epsilon_r}$

$$T = \frac{2\pi}{\omega} = \frac{1}{f}$$

$$\lambda = \frac{c_0}{n \cdot f} = \frac{\lambda_0}{n}$$

$$\lambda = \lambda(n)$$

$f = \text{indep.}$

**ITU G.692**

"the allowed channel frequencies are based on a 50 GHz grid with the reference frequency at 193.10 THz"

**SI**

"a source that emits monochromatic radiation of frequency  $540 \cdot 10^{12}$  Hz"

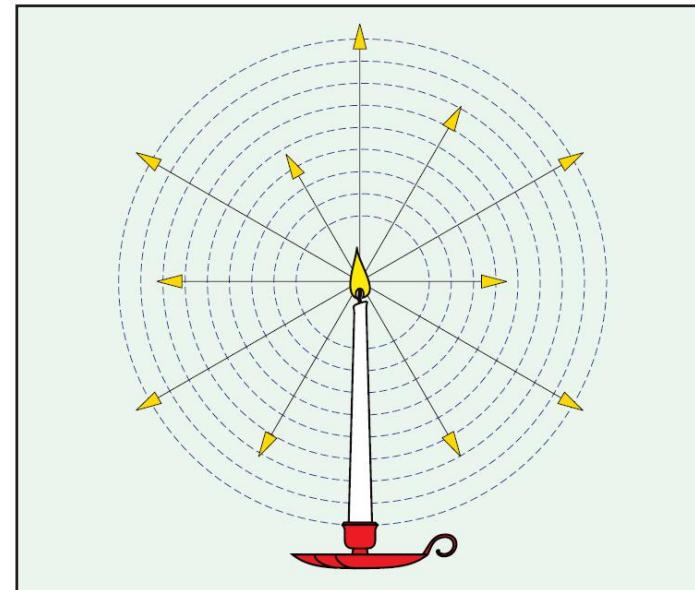
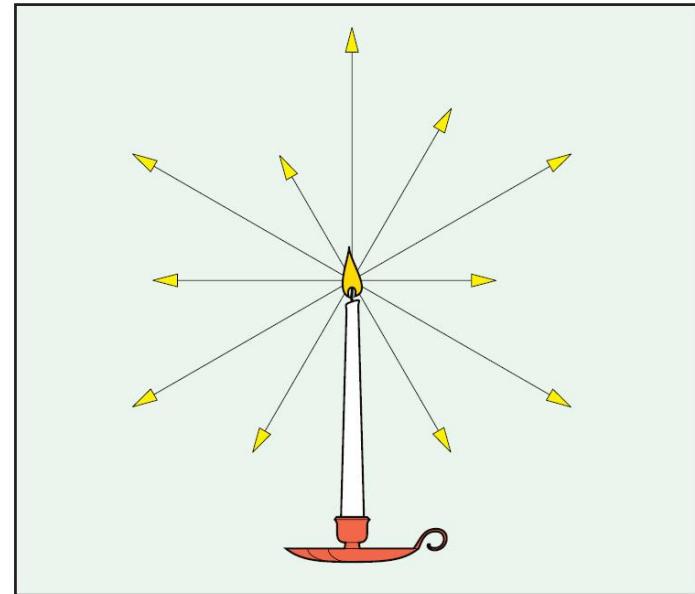
# Optică geometrică

Capitolul 2

# Raze de lumina

- ▶ Lumina este constituită din raze care se propagă în linie dreaptă în medii omogene
- ▶ Sursa omnidirecțională: emite similar în toate direcțiile
- ▶ Densitatea de energie luminoasă descrește invers proporțional cu pătratul distanței față de sursă (energia se împarte uniform pe suprafața întregii sfere)

$$P = \frac{P_0}{r^2}$$



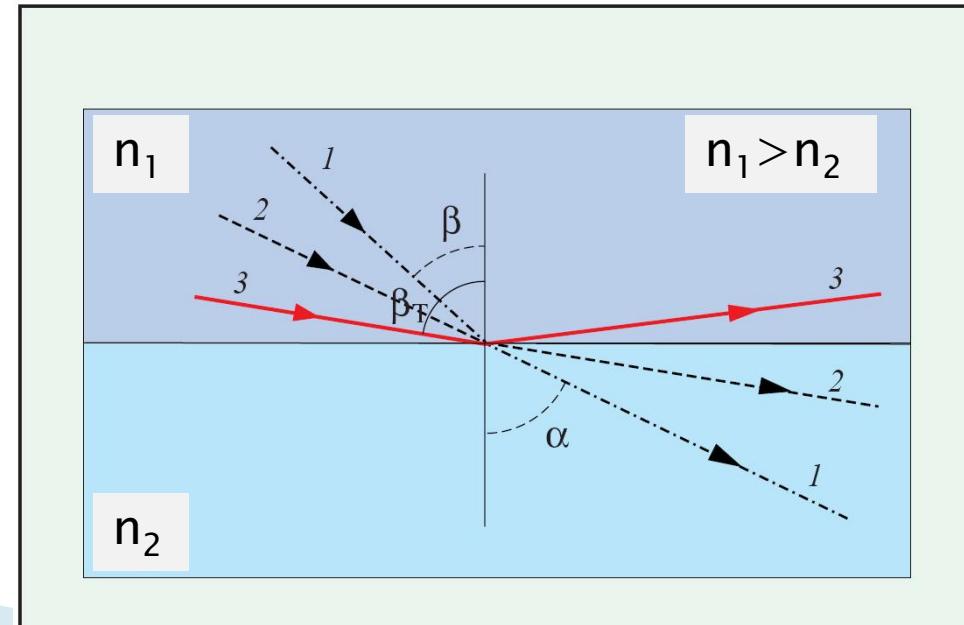
# Reflexia totală

- ▶ Apare **numai când** lumina se propaga dintr-un mediu mai dens optic intr-un mediu mai puțin dens
- ▶ La intersecția luminii cu suprafața de separație a două medii se întâlnesc în general raze reflectate **și** raze refractate
- ▶ Pentru un unghi de incidenta numit **unghi critic**, raza refractată se obține în lungul suprafeței de separație
- ▶ Pentru orice unghi mai mare decât unghiul critic există numai raza reflectată

$$n_1 > n_2; \quad \phi_R = 90^\circ$$

$$n_1 \cdot \sin \phi_C = n_2$$

$$\phi_C = \arcsin \left( \frac{n_2}{n_1} \right)$$



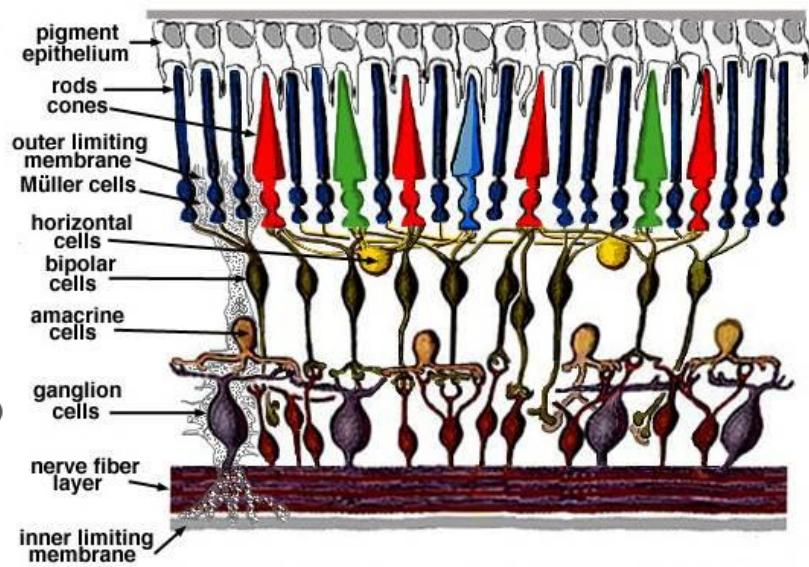
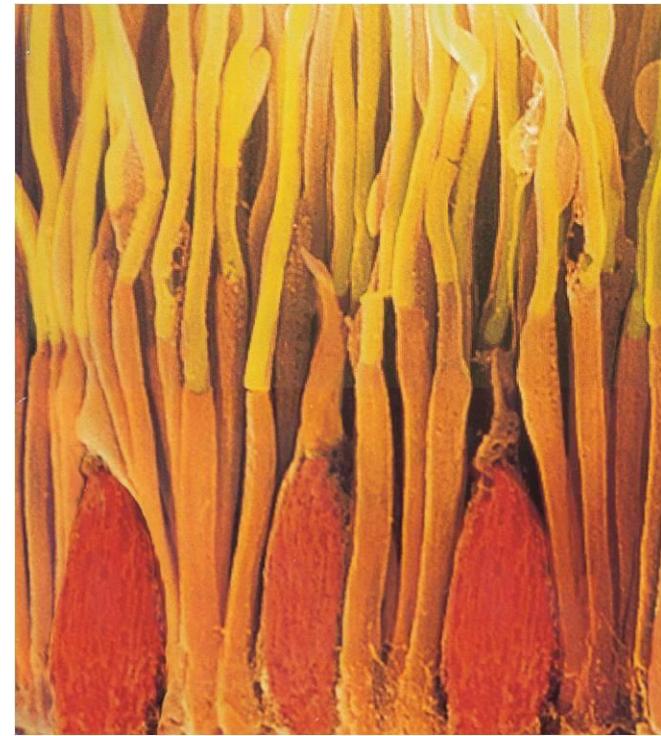
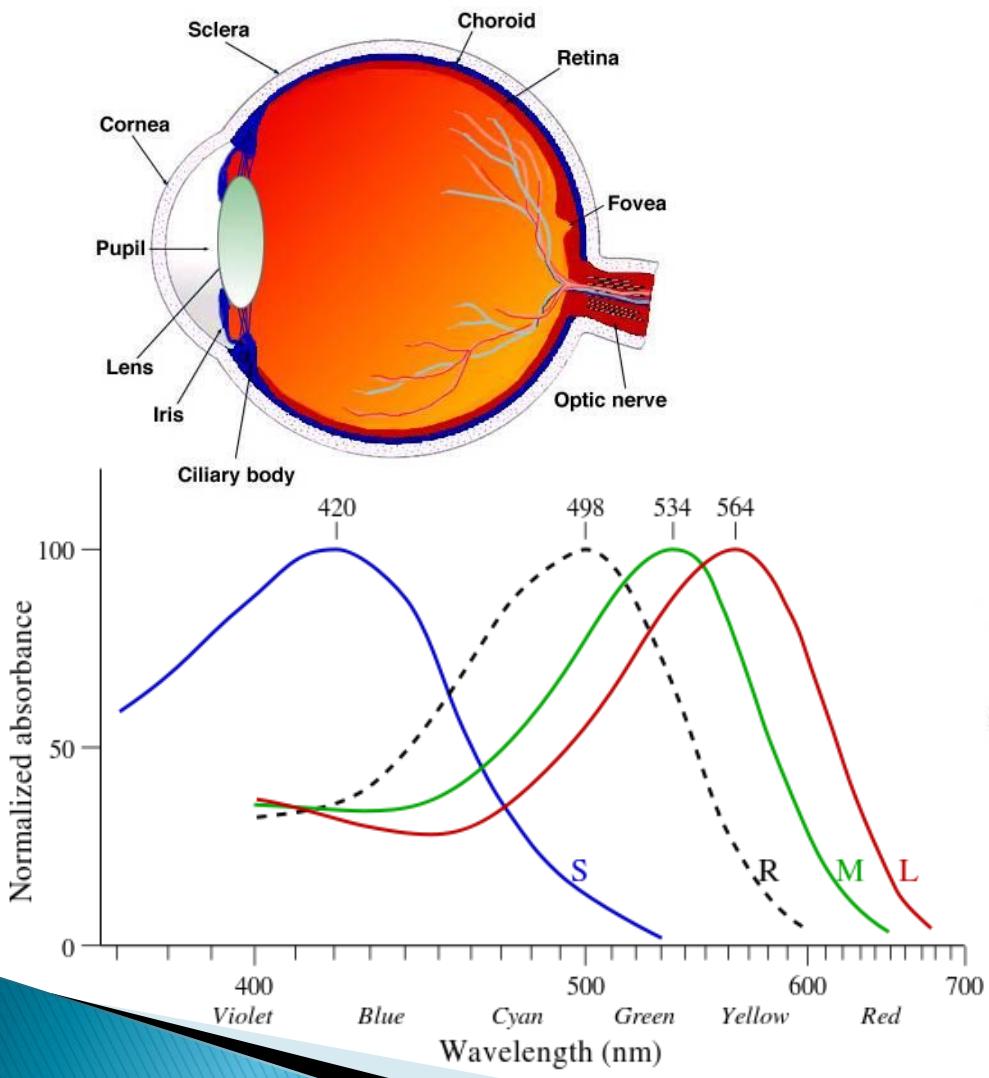
# Fotometrie și radiometrie

Capitolul 3

# O alta dualitate

- ▶ În optoelectronica, lumina poate fi privita din doua puncte de vedere
  - energetic (efect asupra dispozitivului)
  - uman (efect asupra ochiului uman)
- ▶ Dualitatea mărimilor implicate
  - energetice
  - luminoase
- ▶ Candela (cd) **este** una din cele 7 mărimi fundamentale ale SI
  - Cd = intensitatea luminoasa a unei surse ce emite o radiație monocromatica cu frecventa  $540 \cdot 10^{12}$  Hz ( $\lambda = 555\text{nm}$  în vid) și are o intensitate radianta de  $1/683\text{ W/sr}$

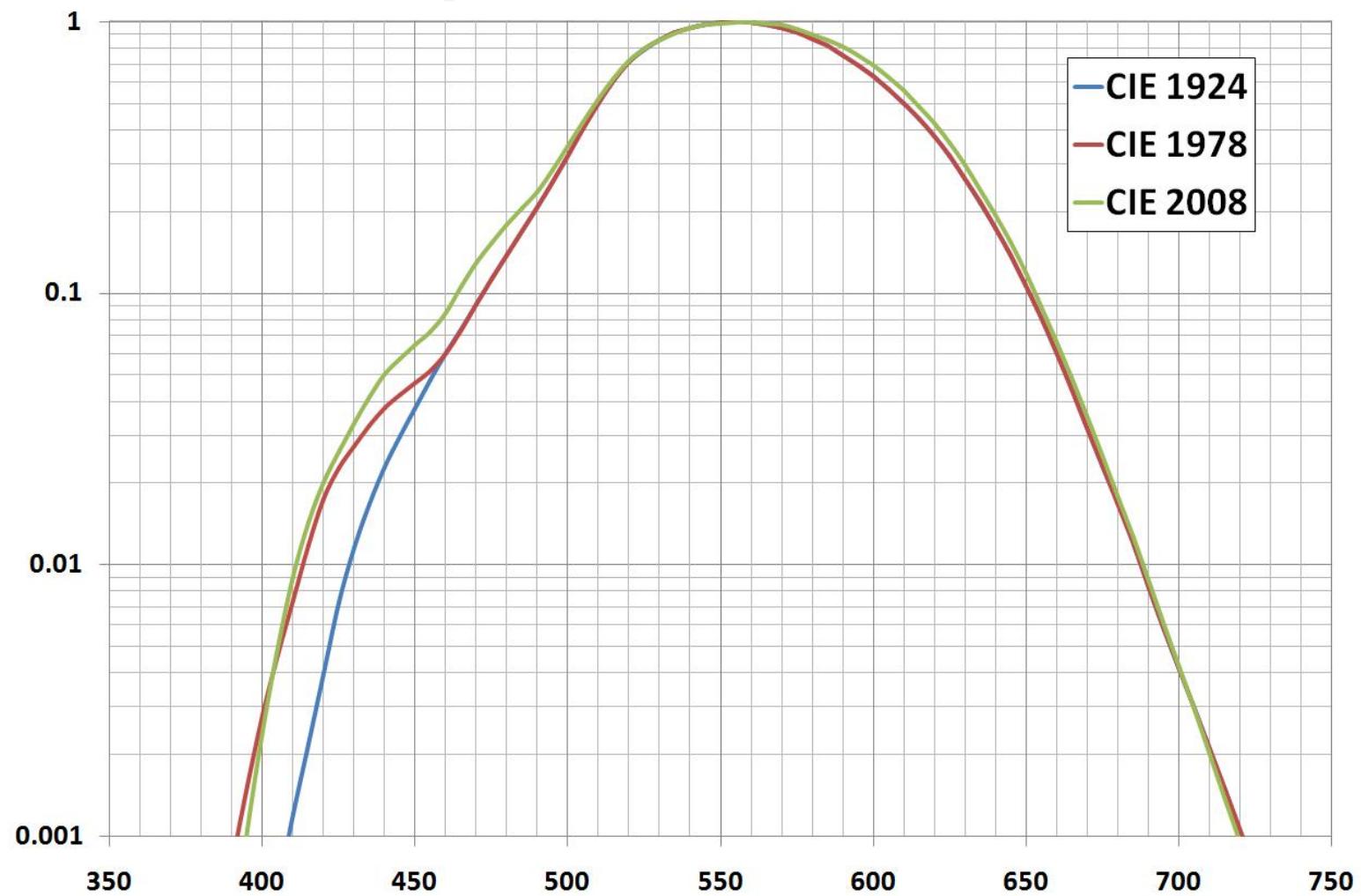
# Ochiul uman



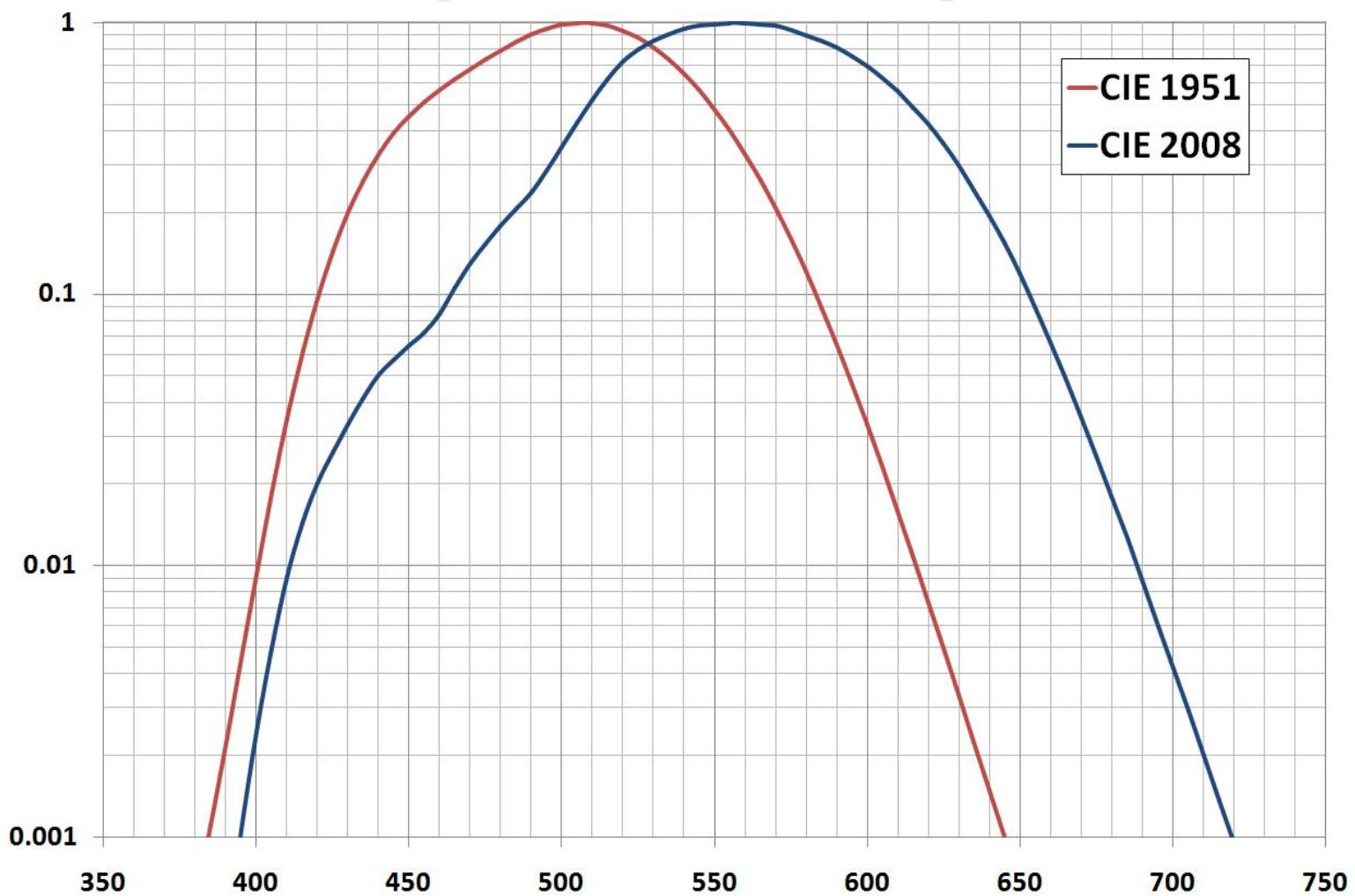
# Standarde

- ▶ Seincearca definirea omului “standard”
- ▶ CIE – Commission Internationale de l'Éclairage
  - 1931 – luminozitatea relativa standard  $V(\lambda)$  – **fotopic**
  - 1951 – luminozitatea relativa standard  $V(\lambda)$  – **scotopic**
  - 1978 – Vos
  - 2005 – Sharpe, Stockman, Jagla, Jägle
  - 2008 – CIE  $V(\lambda)$  – fotopic (~Sharpe)
- ▶ Sensibilitatea maxima a ochiului uman
  - vedere diurna (**fotopic**),  $\lambda=555$  nm,  $\eta_v = 683$  lm/W
  - vedere nocturna (**scotopic** ),  $\lambda=507$  nm ,  $\eta_v = 1700$  lm/W

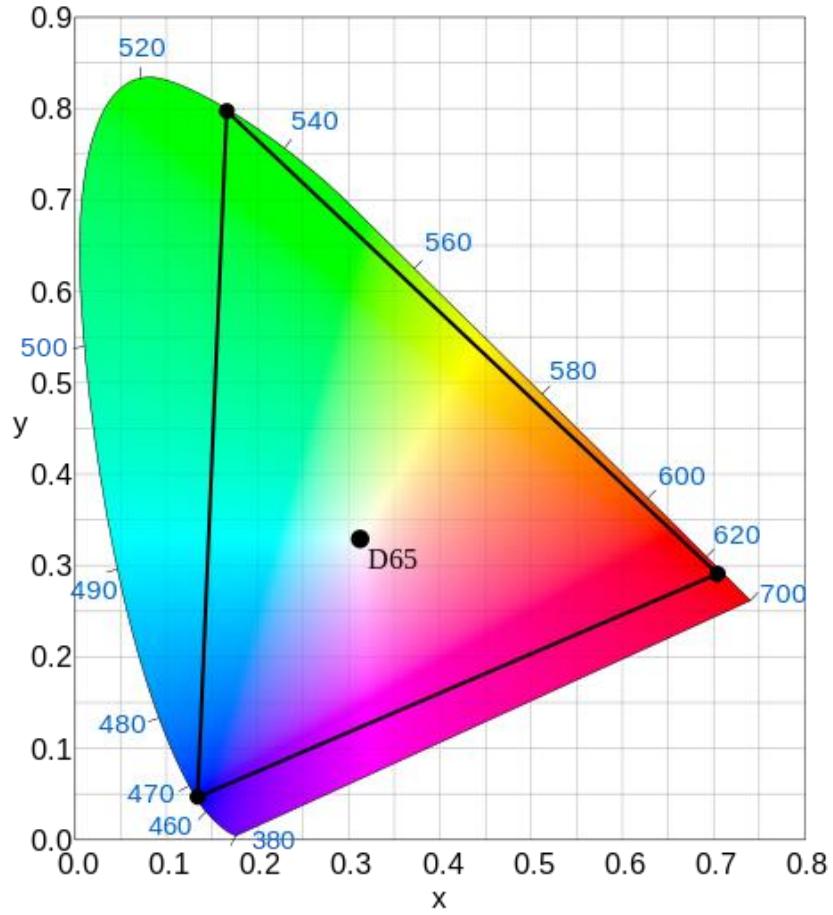
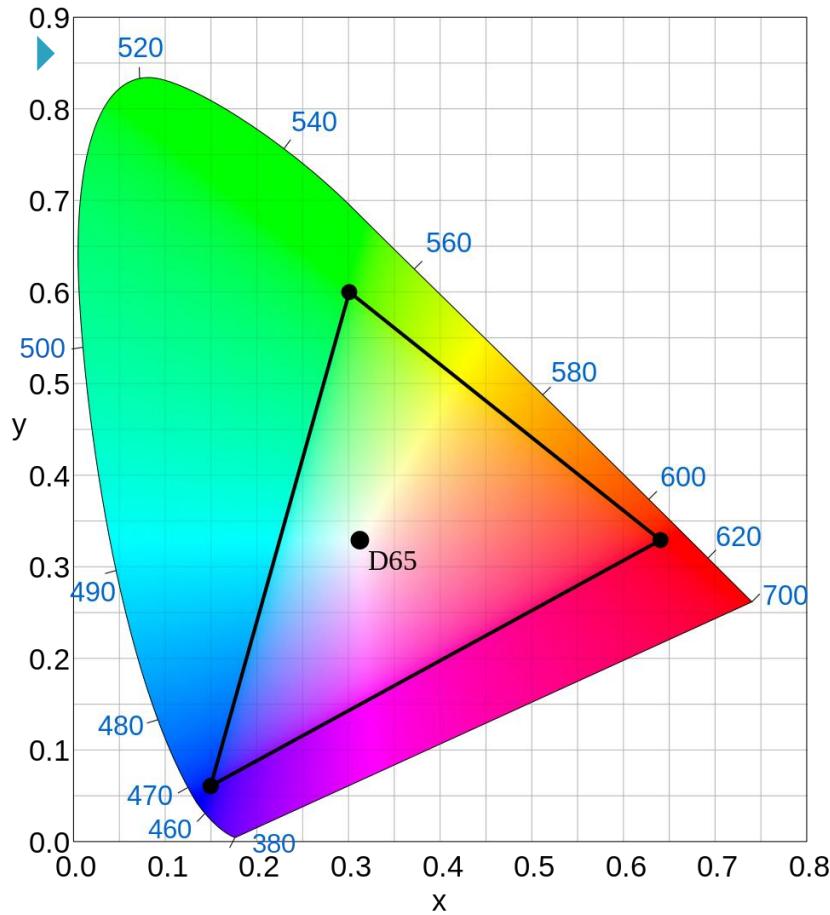
# CIE $V(\lambda)$ fotopic



# CIE $V(\lambda)$ fotopic / scotopic



# ITU-R BT.709/.2020



# Marimi luminoase

## ▶ Intensitatea

- raportul dintre fluxul care părăsește sursa și se propagă într-un element de unghi solid ce conține direcția de propagare și elementul de unghi solid.
- o masura a puterii emise de o sursa într-un element de unghi solid

Intensitatea			
Fotometrie		Radiometrie	
$I_v = \frac{d\Phi_v}{d\Omega}$	SI: cd	$I_e = \frac{d\Phi_e}{d\Omega}$	SI: W/sr

# Marimi luminoase

- ▶ Standardele pentru surse luminoase (de ex. semne de circulatie), iluminarea spatiilor de lucru/odihna
  - sunt concepute cu marimi luminoase
  - lm, cd, lx, cd/m<sup>2</sup> etc.
- ▶ de multe ori se adapteaza relatiile pentru surse mai simple:

$$I_v = \frac{d\Phi_v}{d\Omega} \rightarrow I_v = \left. \frac{\Phi_v}{\Omega} \right|_{I_v \approx ct. \text{ in } \Omega}$$

$$E_v = \frac{d\Phi_v}{dS} \rightarrow E_v = \left. \frac{\Phi_v}{S} \right|_{\Phi_v \approx ct. \text{ pe } S}$$

$$\Phi_v = 683 \frac{lm}{W} \int_{390nm}^{830nm} \frac{d\Phi_e}{d\lambda} \cdot V(\lambda) d\lambda \rightarrow \Phi_v = 683 \frac{lm}{W} \cdot \sum_i \Phi_e(\lambda_i) \cdot V(\lambda_i)$$

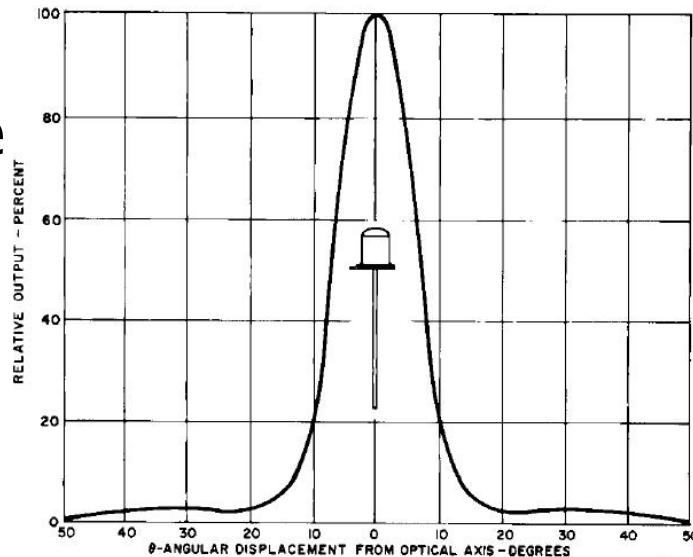
# Directivitatea radiatiei exterioare

## SLED

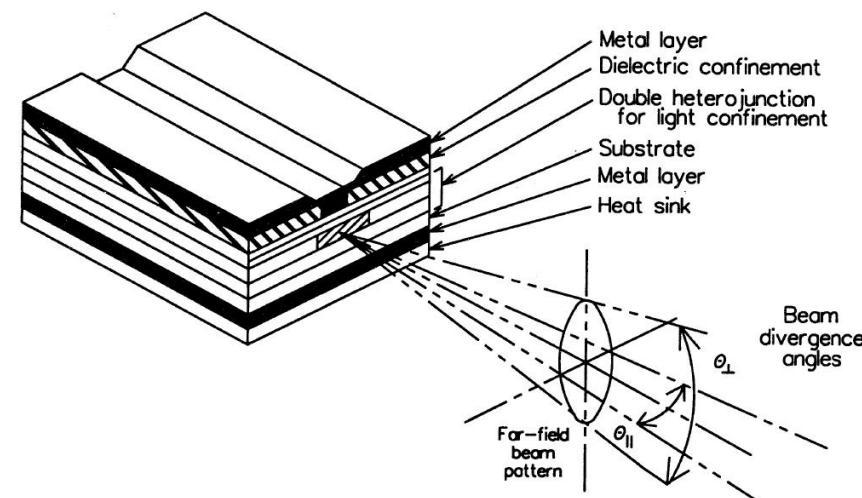
- radiatia este emisa cu simetrie circulara, in interiorul unui con cu unghi la varf tipic de  $60^\circ$
- Viewing Half Angle  $\sim 10 \div 15^\circ$

## ELED

- radiatia emisa nesimetric in forma de con eliptic
  - perpendicular pe jonctiune  $\sim 60^\circ$
  - paralel cu jonctiunea  $\sim 30^\circ$



ST1054



# Probleme

- ▶ Panoul unui dispozitiv conține două LED-uri de semnalizare, unul de culoare verde și unul roșu standard. Doriți ca ambele să ofere aceeași luminozitate relativă și cât mai mare posibilă. Dacă ambele LED-uri acceptă un curent maxim de 50 mA, calculați curentul prin cele două LED-uri.
- ▶ Rezolvari: <http://rf-opto.eti.tuiasi.ro>

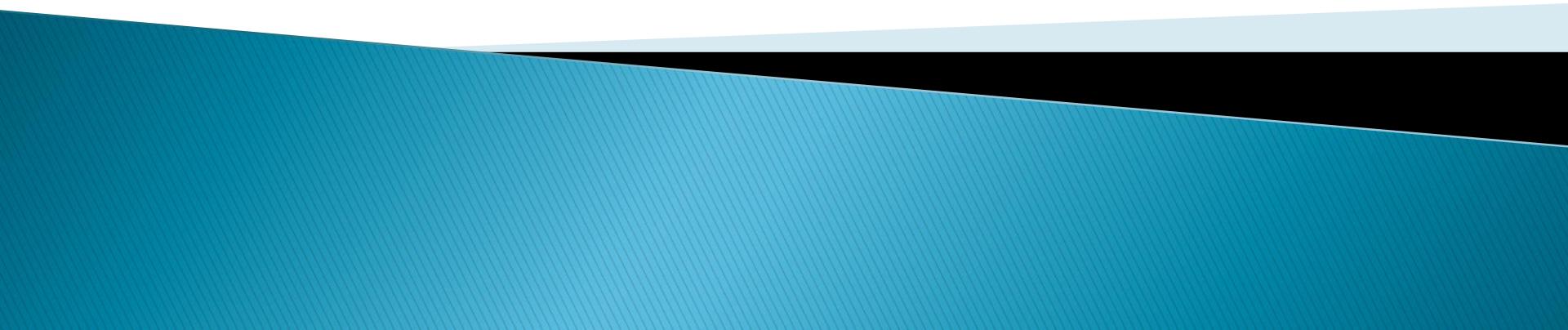
# Probleme

- ▶ Trebuie să proiectați un semafor cu LED-uri. LED-urile care intră în compoñența sa sunt caracterizate de eficiență cuantică egală (aceeași tehnologie), iar parametrii de catalog pentru LED-ul roșu sunt ...
- ▶ Proiectați semaforul, pentru a obține o iluminare la 5m, pe direcție normală, de 50 lx pe timp de zi și 2 lx pe timp de noapte.
- ▶ Cerințe: luminozitate egală pentru cele 3 culori, alegerea numărului de LED-uri (considerente electronice/practice), necesitățile de curent ale fiecărui LED, parametrii pentru sursa de alimentare, parametrii unui sistem de control a intensității luminoase pentru reglare zi/noapte.
- ▶ Rezolvari: <http://rf-opto.etti.tuiasi.ro>

# Probleme

- ▶ O instalație de iluminare de urgență este realizată cu LED-uri care emit lungimea de undă dominantă  $\lambda_0 = 520\text{nm}$  sub un con cu unghi la vârf de  $8.9^\circ$  (**emisie presupusă uniformă în acest con**). LED-urile sunt montate în tavanul unei încăperi înaltă de  $2.8\text{m}$  și cu o suprafață de  $36.5\text{m}^2$  și trebuie să asigure o iluminare de  $0.95\text{lx}$  la nivelul podelei.
- ▶ Rezolvari: <http://rf-opto.etti.tuiasi.ro>

# Continuare

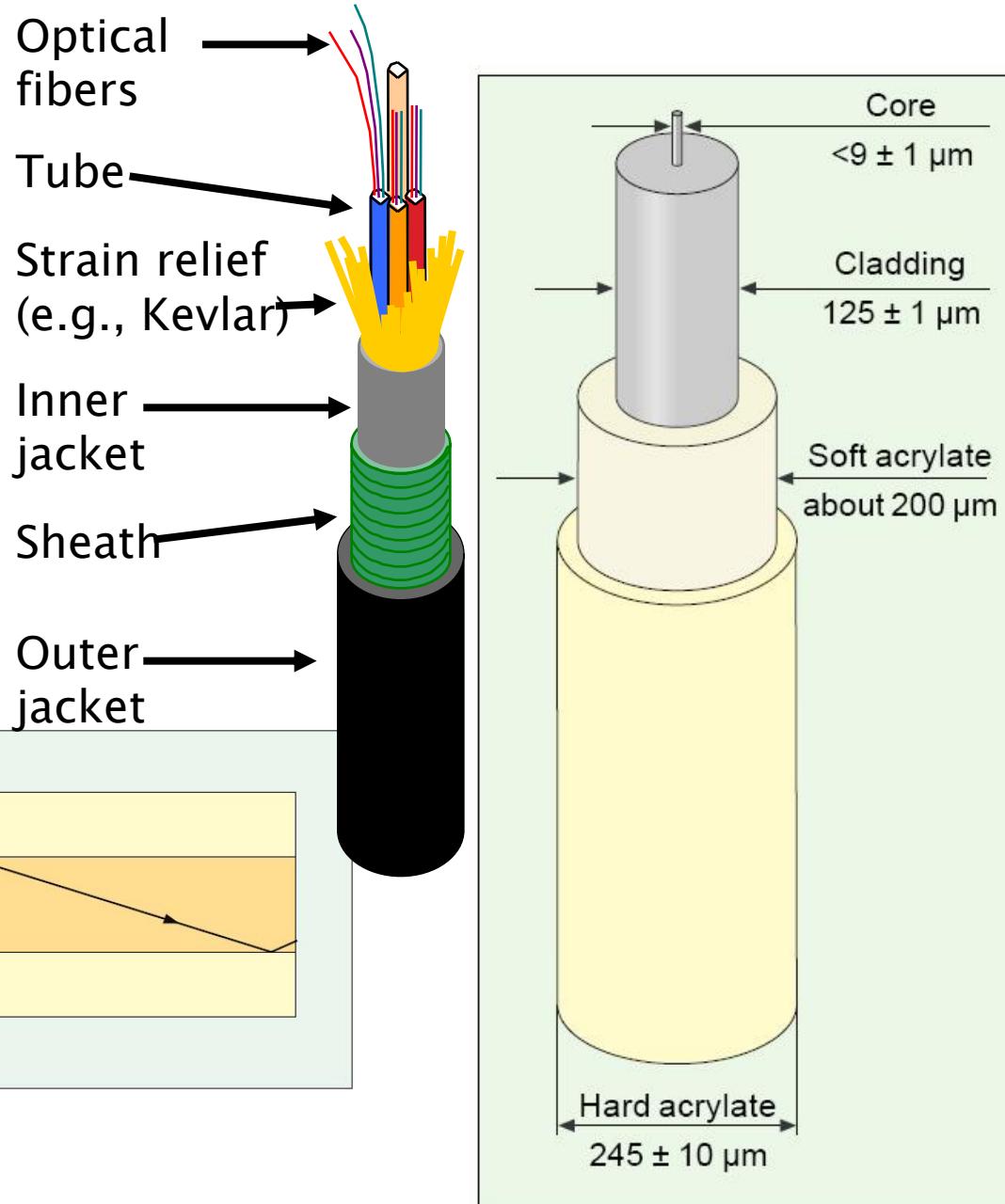


# **Fibra optică**

**Capitolul 4**

# Fibra optica

- ▶ un ghid de unda dielectric
  - miez
  - teaca

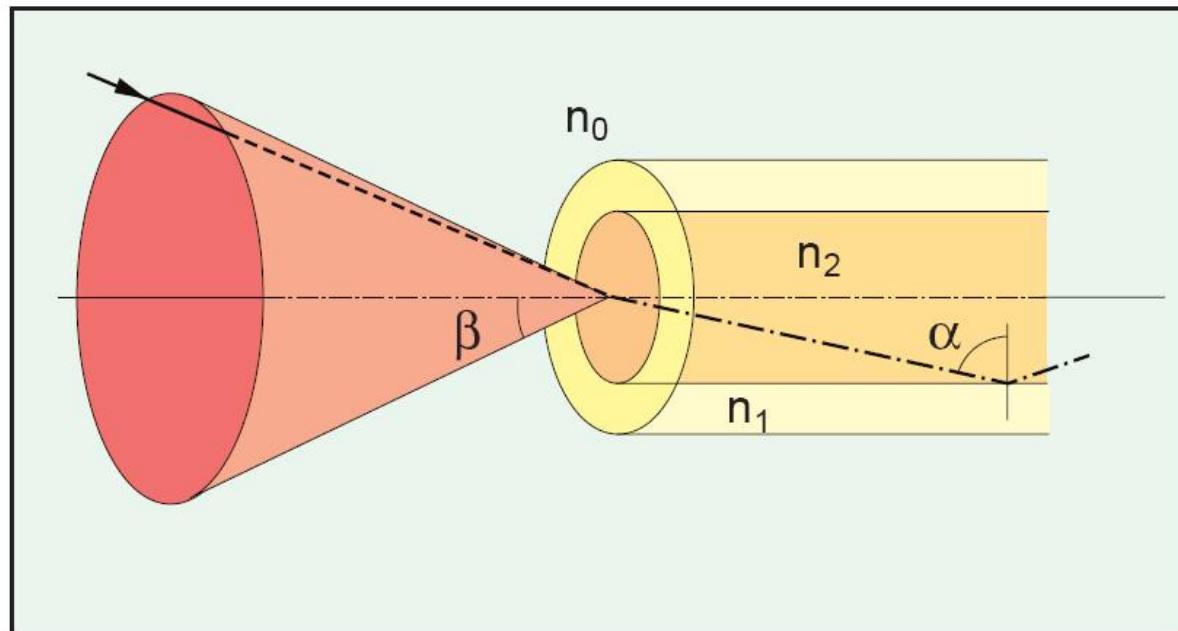


# Unghi de acceptanta, apertura numerica

- ▶ Unghi de acceptanta

$$n_0 \cdot \sin \theta_{ACC} = n_2 \cdot \sin \phi_c$$

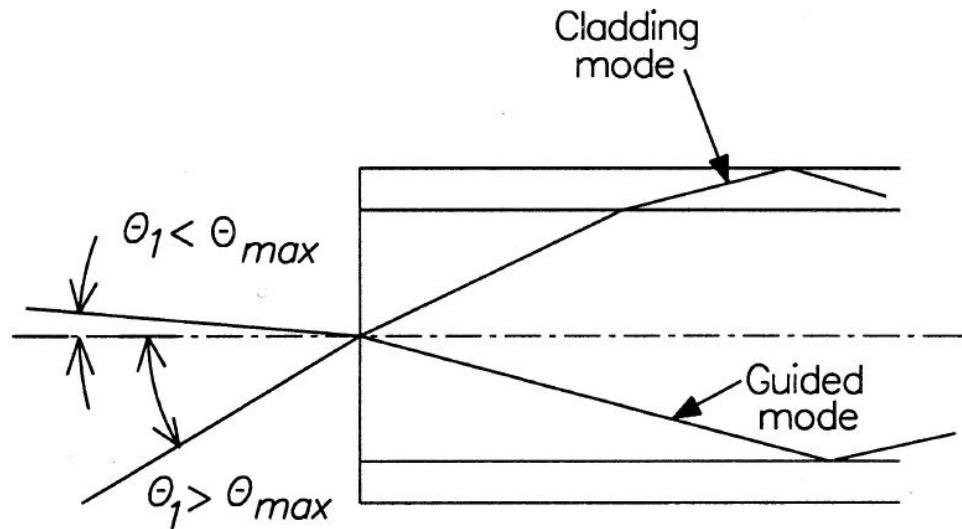
- ▶ Apertura numerica



$$NA = n_0 \cdot \sin \theta_{ACC}$$

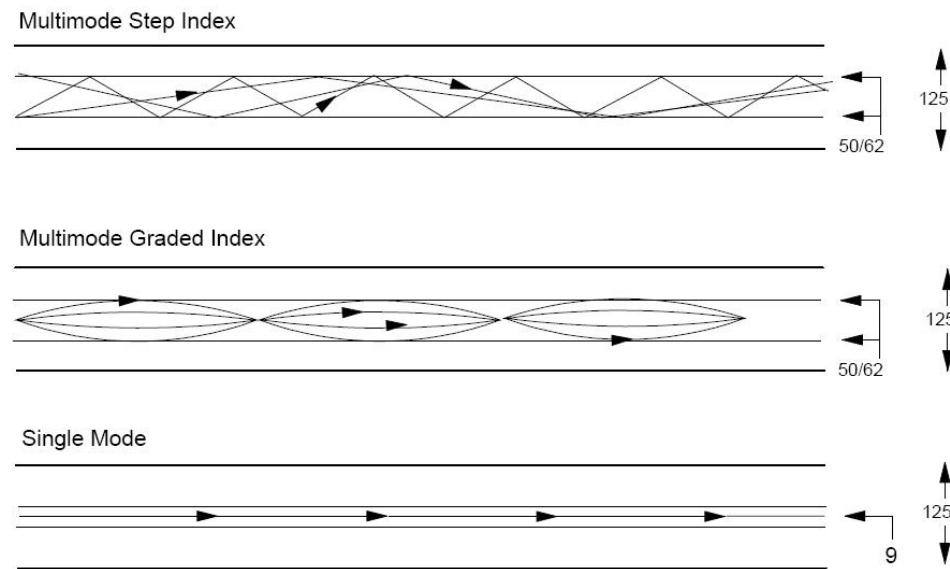
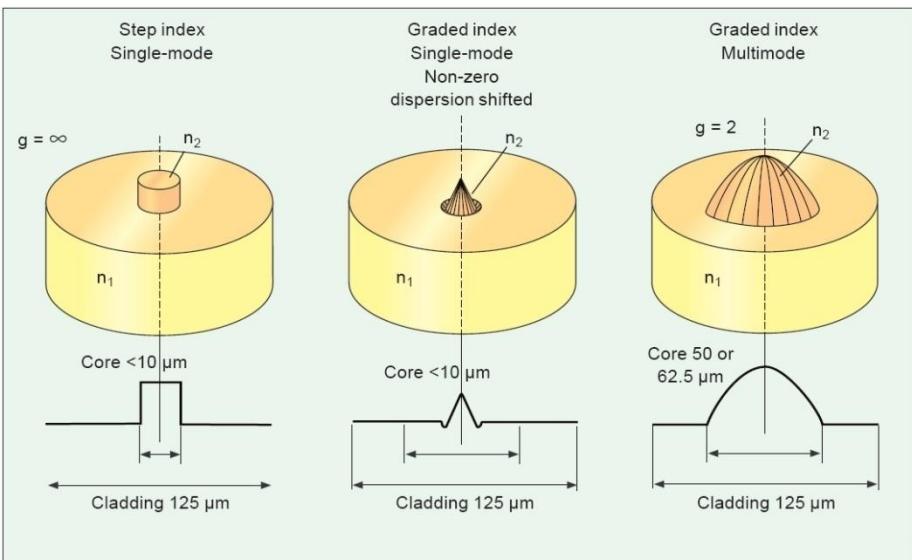
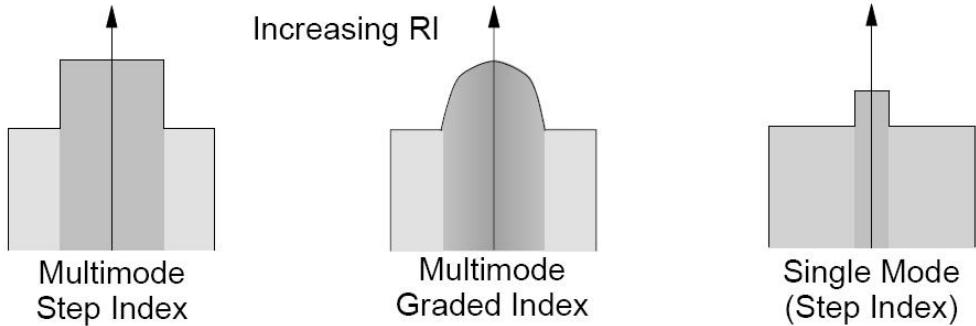
$$NA = n_2 \sqrt{\frac{n_2^2 - n_1^2}{n_2^2}} = \sqrt{n_2^2 - n_1^2}$$

$n_2$  - miez  
 $n_1$  - teaca  
 **$n_2 > n_1 !!$**

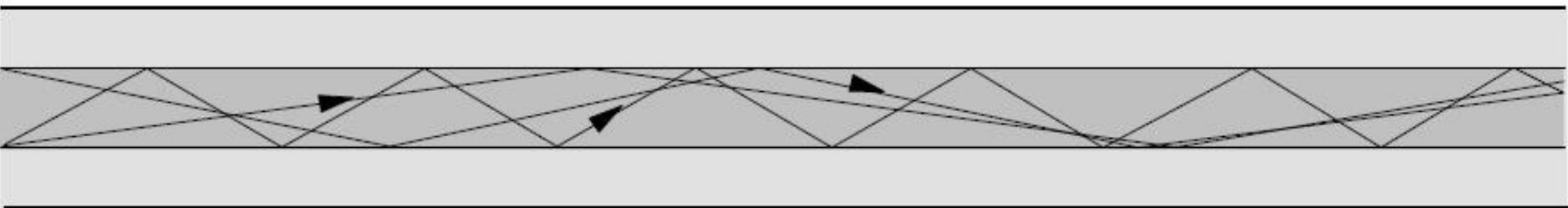


# Tipuri de fibra

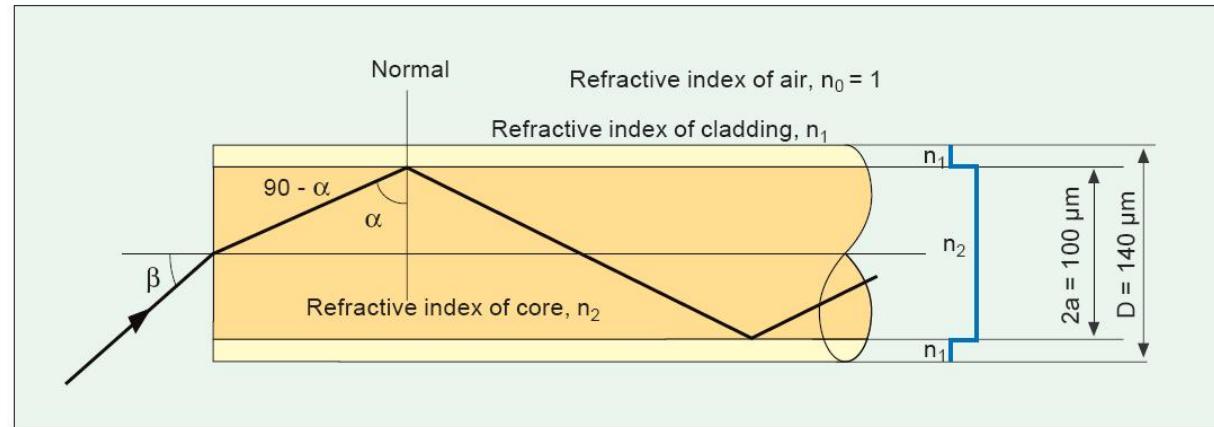
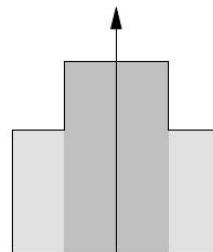
- ▶ Monomod
- ▶ Multimod
  - cu salt de indice
  - cu indice gradat



# Fibre multimod cu salt de indice



- ▶ 50/125 sau  
62.5/125  
( $\mu\text{m}$ )
- ▶ 15–50 MHz · km

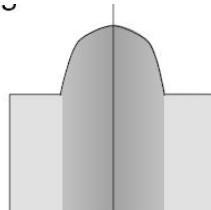
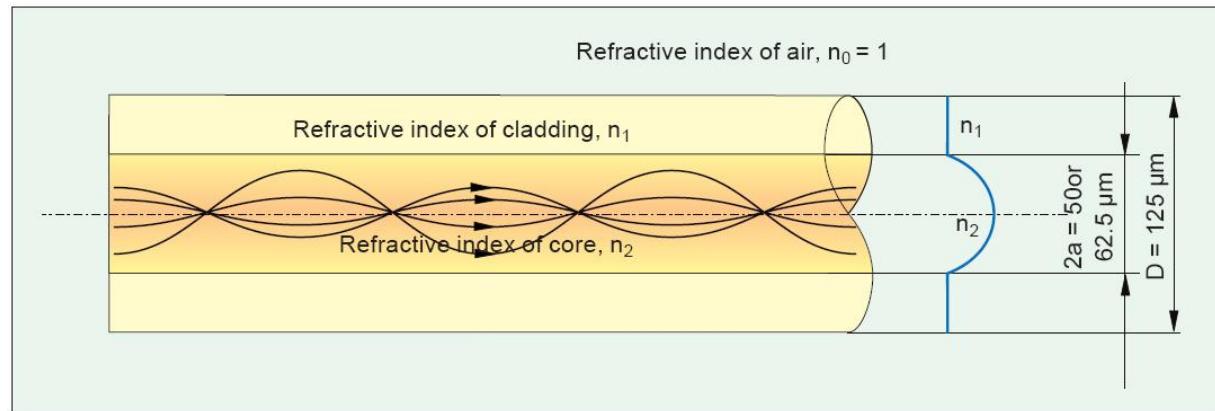


	glass	plastic
core diameter 2a	100 $\mu\text{m}$	980 $\mu\text{m}$
cladding diameter D	140 $\mu\text{m}$	1000 $\mu\text{m}$
core refractive index n <sub>2</sub>	1.48	
cladding refractive index n <sub>1</sub>	1.45	

# Fibre multimod cu indice gradat

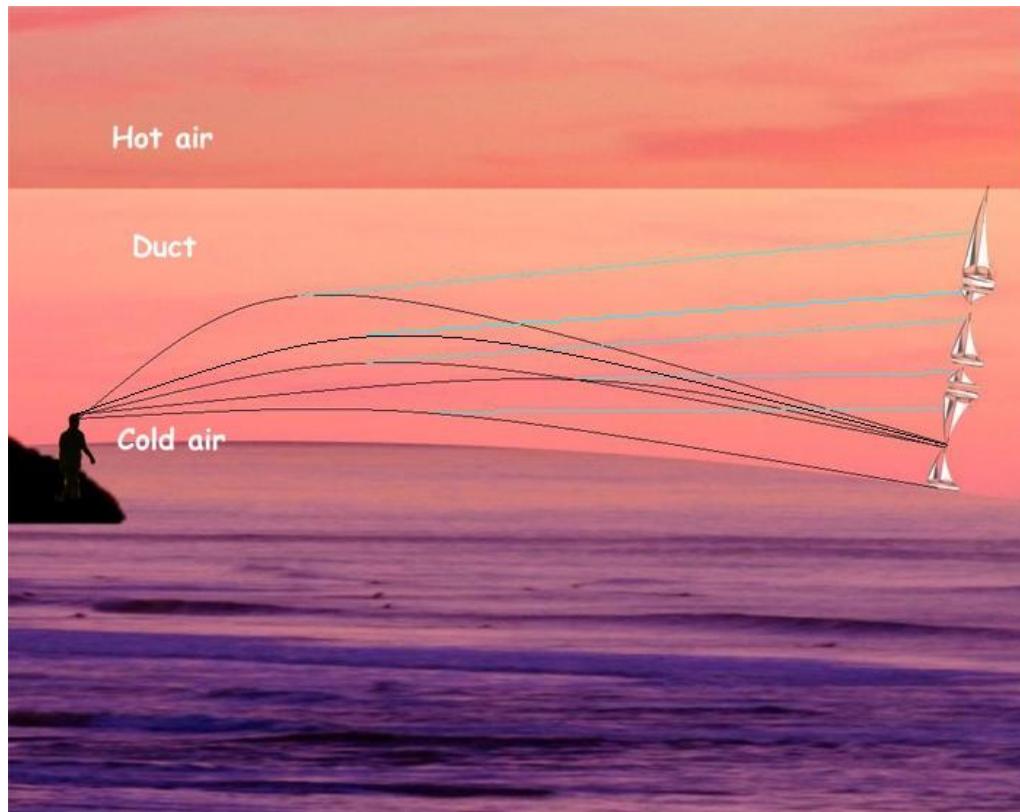


- ▶ 50/125 sau  
62.5/125  
( $\mu\text{m}$ )
- ▶ 700–1200  
MHz · km

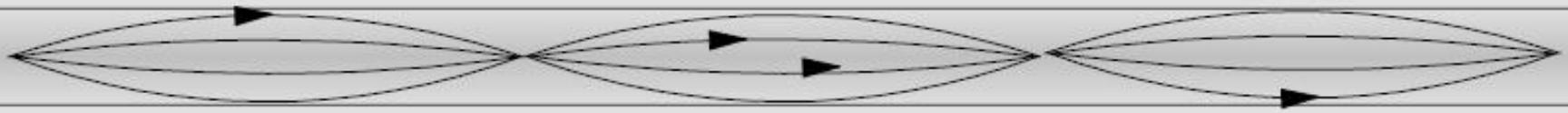


Core diameter $2a$	50 or 62.5 $\mu\text{m}$
Cladding diameter $D$	125 $\mu\text{m}$
Maximum refractive index, core	1.46
Relative differential refractive index	0.010

# Fata Morgana



# Fibre multimod cu indice gradat



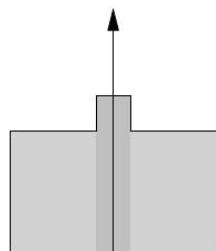
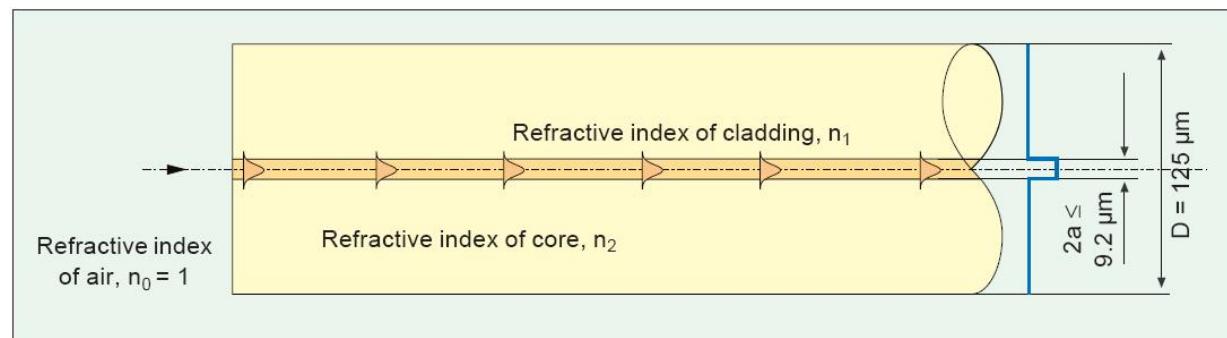
$$n(r) = n_2 \left[ 1 - \Delta \left( \frac{r}{a} \right)^g \right]$$

$$\Delta = \frac{NA^2}{2n_2^2} = \frac{n_2^2 - n_1^2}{2n_2^2} \approx \frac{n_2 - n_1}{n_2} \approx \frac{\Delta n}{n} \quad \text{for } \Delta \ll 1$$

- ▶  $g = 1$  – indice gradat triunghiular
- ▶  $g = 2$  – indice gradat parabolic
- ▶  $g = \infty$  – salt de indice

# Fibre monomod

- ▶ 6-8/125 ( $\mu\text{m}$ )
- ▶ MHz · km  
nerelevant
- ▶ MFD – Mode Field Diameter



Cladding diameter D	125 $\mu\text{m}$
Core refractive index $n_2$	1.4485
Cladding refractive index $n_1$	1.4440
Refractive index differential	0.003 = 0.3%

# Ghid cilindric dielectric

## ► Ecuatiile lui Maxwell in coordonate cilindrice

$$\frac{\partial^2 U}{\partial r^2} + \frac{1}{r} \frac{\partial U}{\partial r} + \frac{1}{r^2} \frac{\partial^2 U}{\partial \phi^2} + \frac{\partial^2 U}{\partial z^2} + n^2 k_o^2 U = 0 \quad \begin{matrix} a - \text{raza miezului} \\ U - E(r) \text{ sau } H(r) \end{matrix}$$

$$U(r, \phi, z) = u(r)e^{-jl\phi}e^{-j\beta z}, \quad l = 0, \pm 1, \pm 2, \dots$$

$$\frac{d^2 u}{dr^2} + \frac{1}{r} \frac{du}{dr} + \left( n^2(r) k_o^2 - \beta^2 - \frac{l^2}{r^2} \right) u = 0$$

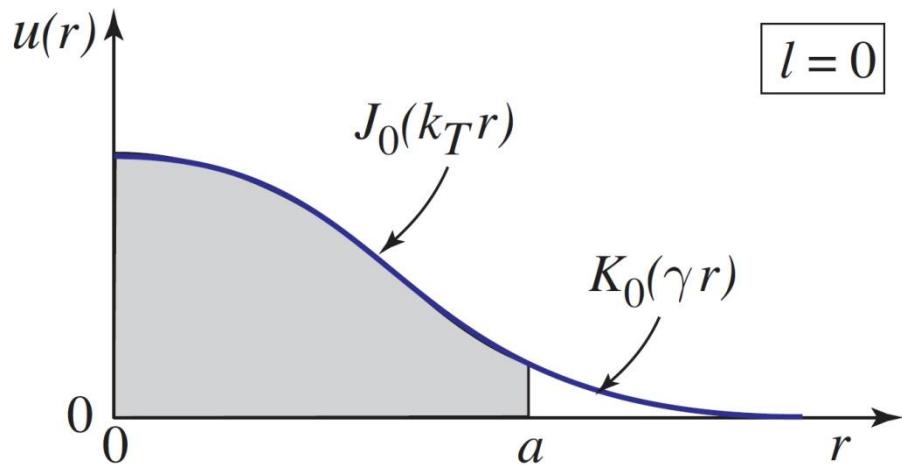
$$\frac{d^2 u}{dr^2} + \frac{1}{r} \frac{du}{dr} + \left( k_T^2 - \frac{l^2}{r^2} \right) u = 0, \quad r < a$$

$$\frac{d^2 u}{dr^2} + \frac{1}{r} \frac{du}{dr} - \left( \gamma^2 + \frac{l^2}{r^2} \right) u = 0, \quad r > a$$

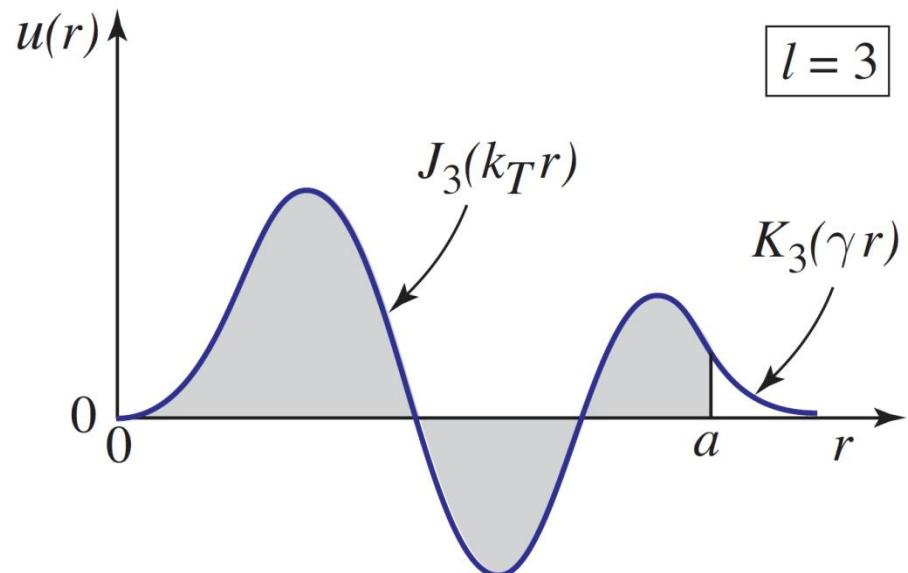
# Ghid cilindric dielectric

- solutii proportionale cu functii Bessel

$$u(r) \propto \begin{cases} J_l(k_T r), & r < a \quad (\text{core}) \\ K_l(\gamma r), & r > a \quad (\text{cladding}) \end{cases}$$



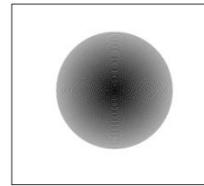
$l = 0$



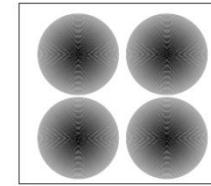
$l = 3$

# Moduri in fibra

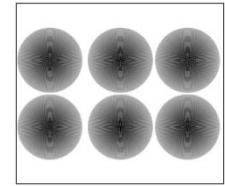
- ▶ Moduri in ghid rectangular



TEM<sub>00</sub>

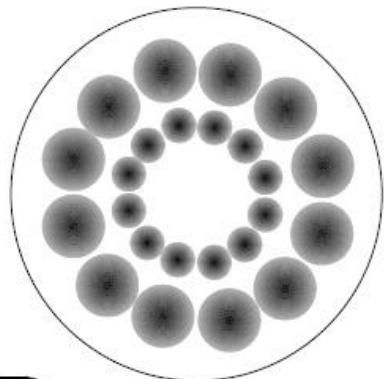


TEM<sub>11</sub>

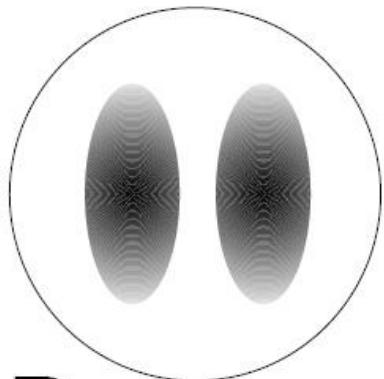


TEM<sub>21</sub>

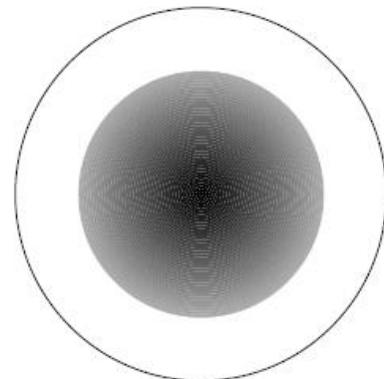
- ▶ Moduri linear polarizate in fibra



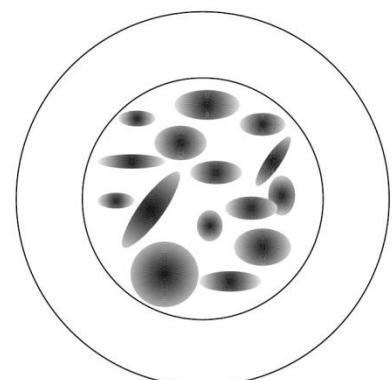
LP<sub>62</sub>



LP<sub>11</sub>



LP<sub>01</sub>



“Sparkle” pattern

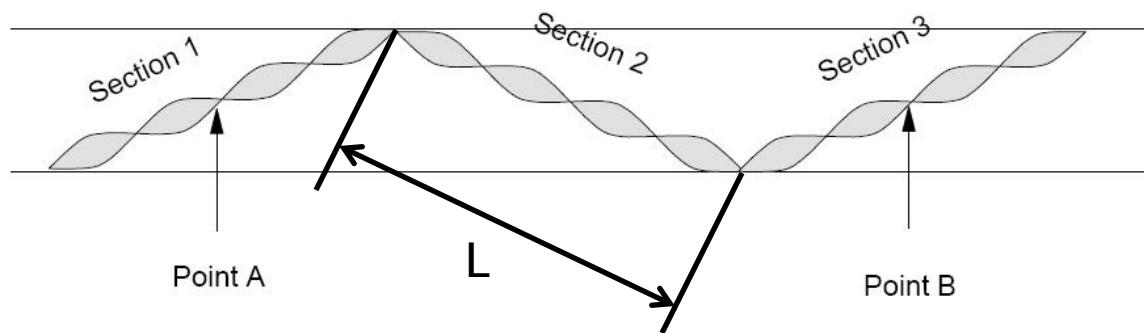
# Frecventa normalizata

## ▶ Frecventa normalizata

$$V = 2\pi \frac{a}{\lambda} NA = k \cdot a \cdot NA \quad a - \text{raza miezului}$$

$$k = \frac{2\pi}{\lambda}$$

## ▶ Numar de moduri

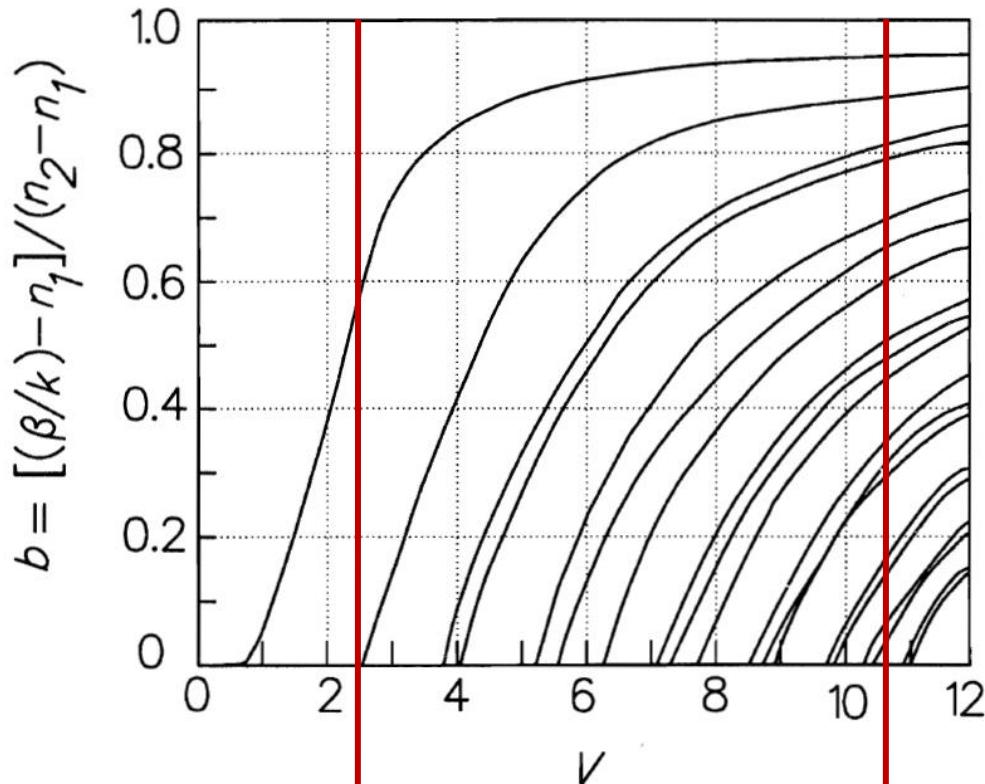


$$L = m \cdot \lambda$$

$$N \approx \frac{V^2}{2} \cdot \frac{g}{g+2}$$

# Frecventa normalizata – monomod

## ► Fibre monomod



$b$  – coeficient de propagare modal relativ

$$V \leq V_C = 2.405$$

exista un **singur** mod (solutii fc. Bessel)

$$\lambda \geq \lambda_C = \pi \frac{2a}{V_C} NA = \pi \frac{2a}{2.405} NA$$

Exemplu:

$$2a = 8.5 \mu\text{m}$$

$$NA = 0.11$$

$$\lambda_C = \pi \frac{8.5}{2.405} 0.11 = 1210 \text{ nm}$$

# Frecventa normalizata

- ▶ Numar de moduri
  - Multimod cu salt de indice

$$g = \infty \Rightarrow N \approx \frac{V^2}{2}$$

- Multimod cu indice gradat

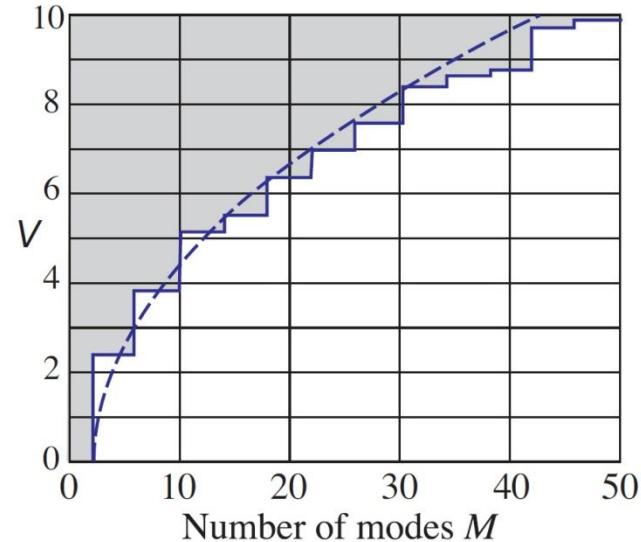
$$g = 2 \Rightarrow N \approx \frac{V^2}{4}$$

- Monomod

$$V \leq V_C = 2.405$$

există un singur mod (solutii fc. Bessel)

$$N \approx \frac{V^2}{2} \cdot \frac{g}{g+2}$$



# Exemplu

## ► fibra tipica multimod

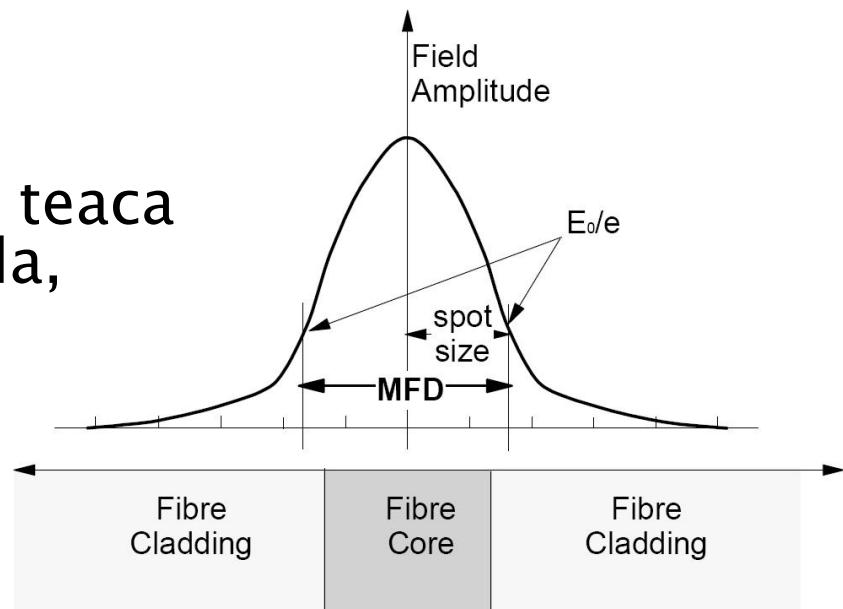
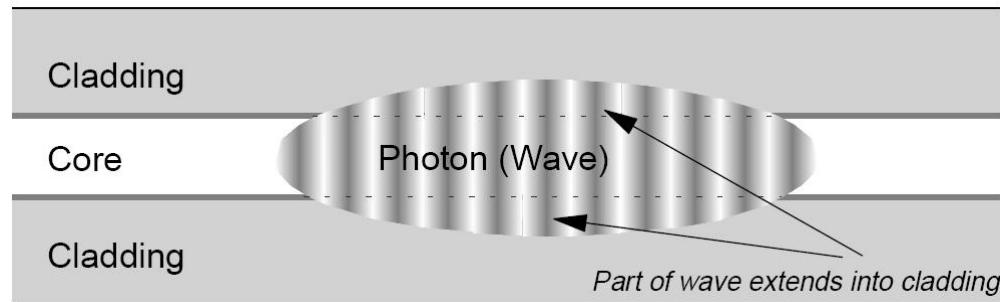
- $g=2$
- $2a = 50\mu m \rightarrow a = 25\mu m$
- $NA = 0.2$  la  $\lambda = 1\mu m$

$$V = 2\pi \frac{a}{\lambda} NA = 2\pi \frac{25}{1} 0.2 = 2 \cdot \pi \cdot 5 \approx 31.4$$

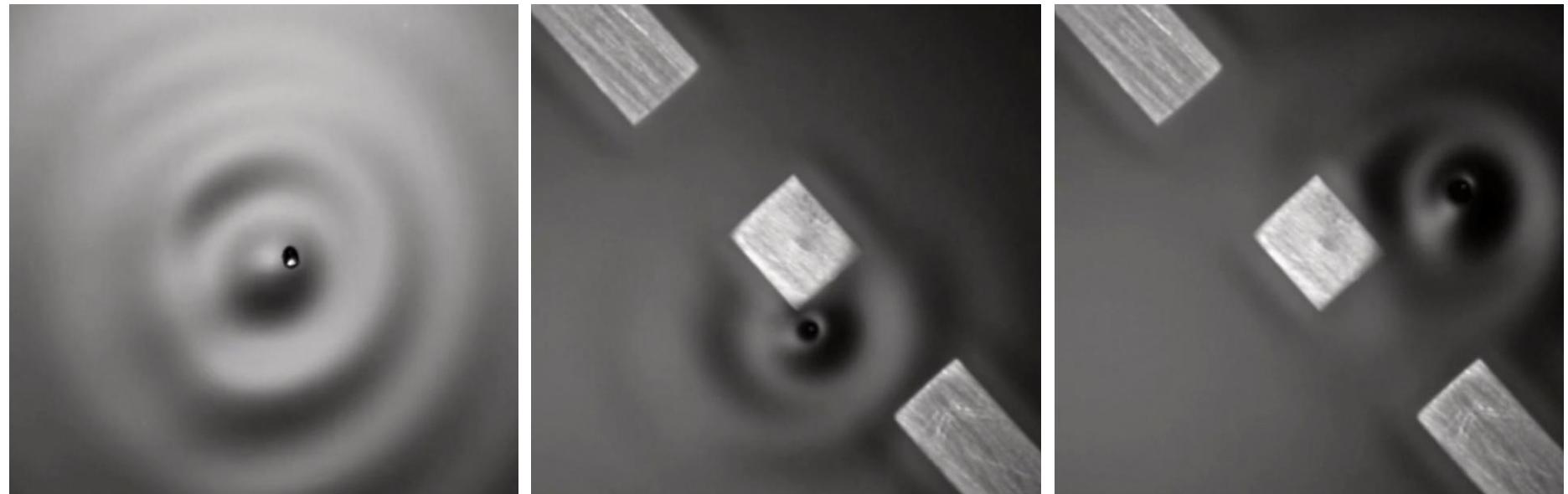
$$g = 2 \Rightarrow N = \frac{V^2}{4} = \frac{31.4^2}{4} = 247$$

# Propagarea in fibra monomod

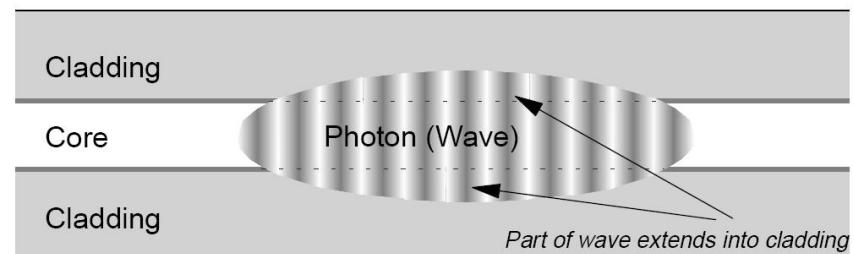
- ▶ Propagarea luminii poate fi explicata doar prin teoria electromagneticica
- ▶ Energia campului se extinde in teaca (diametrul efectiv al spotului luminos – MFD, Mode Field Diameter)
- ▶  $MFD > 2a$
- ▶ Adancimea de patrundere in teaca depinde de lungimea de unda, generand dispersia de ghid



# Modelare



Through the Wormhole  
S02E07 How Does the Universe Work



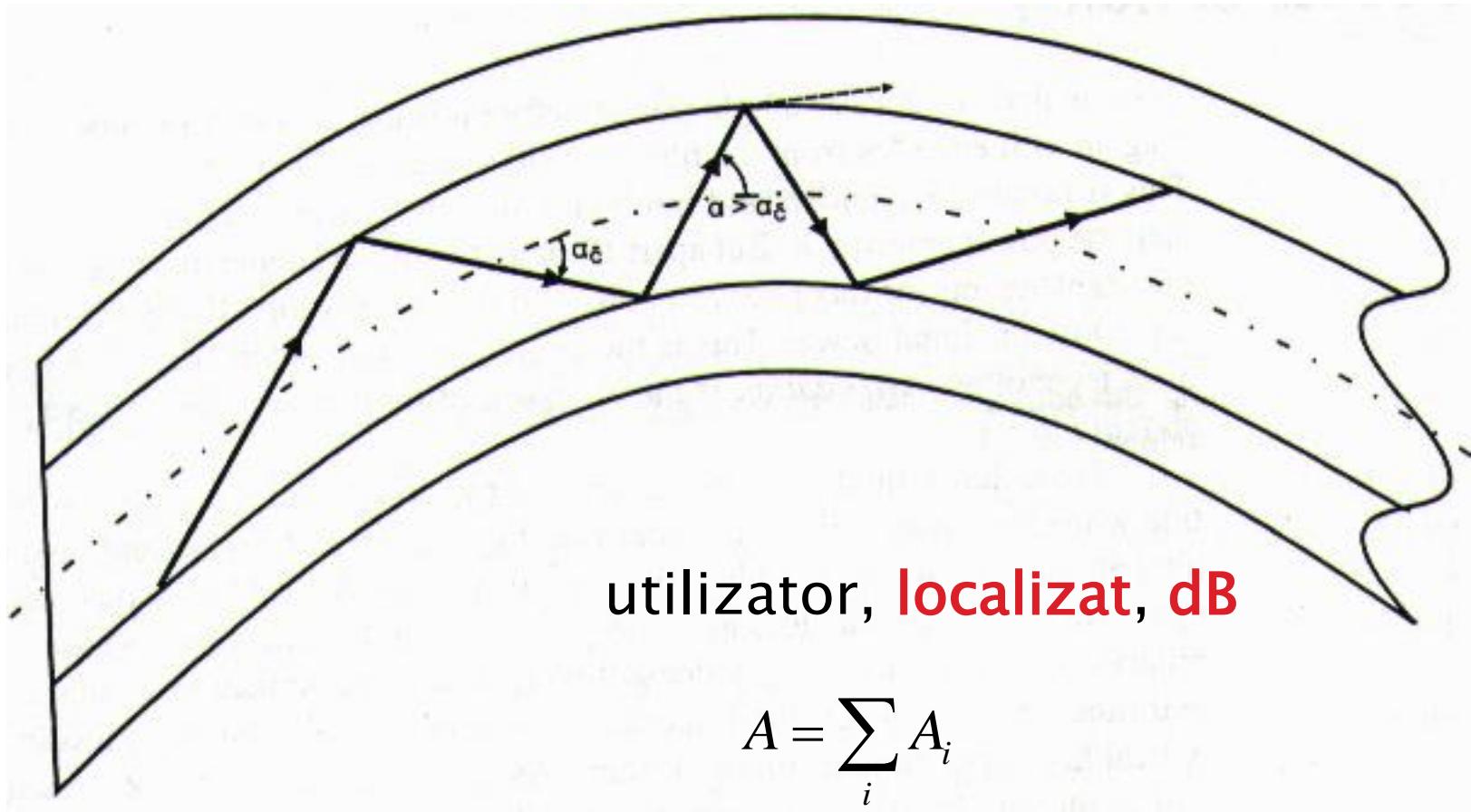
# Fenomene de interes

- ▶ Cat de departe pot transmite semnalul luminos pe fibra
  - **atenuare**
- ▶ Cat de rapid pot transmite informația
  - dispersie

# Atenuare

- ▶ Macrocurburi
  - utilizator, **localizat**, dB
- ▶ Discontinuitate in fibra
  - utilizator, **localizat**, dB
- ▶ Microcurburi
  - **distribuit**, tehnologie, dB/km
- ▶ Imprastiere
  - **distribuit**, tehnologie, dB/km
- ▶ Absorbtie
  - **distribuit**, material, dB/km

# Macrocurburi



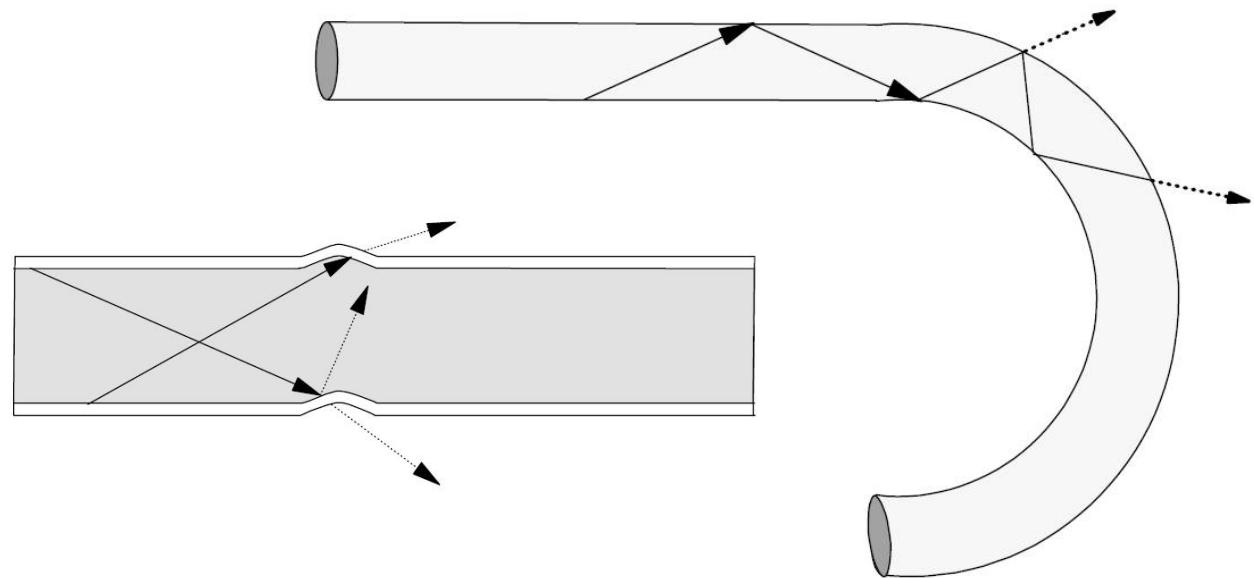
utilizator, **localizat**, dB

$$A = \sum_i A_i$$

$$A = N \cdot A_i$$

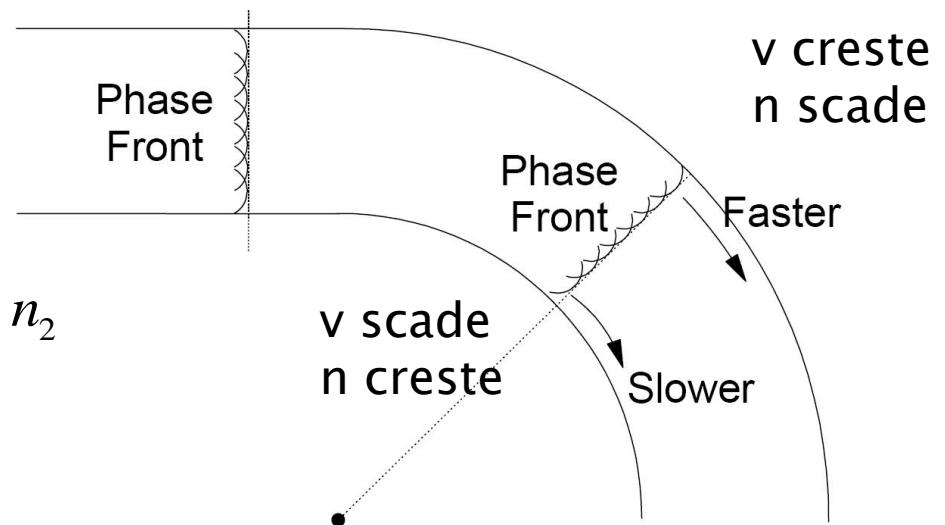
# Efectul curburilor

## ► Multimod



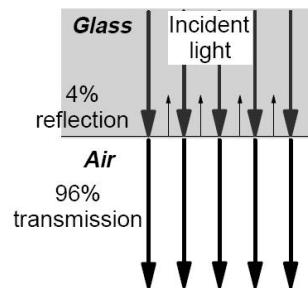
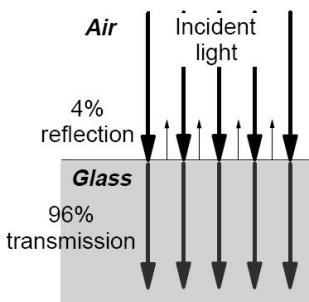
## ► Monomod

$$R > R_c \Rightarrow n_{1,ext} > n_2$$



# Discontinuitate in fibra

- ▶ Apare cand nu putem considera fibra un singur ghid dielectric
  - defectiuni
  - conectori

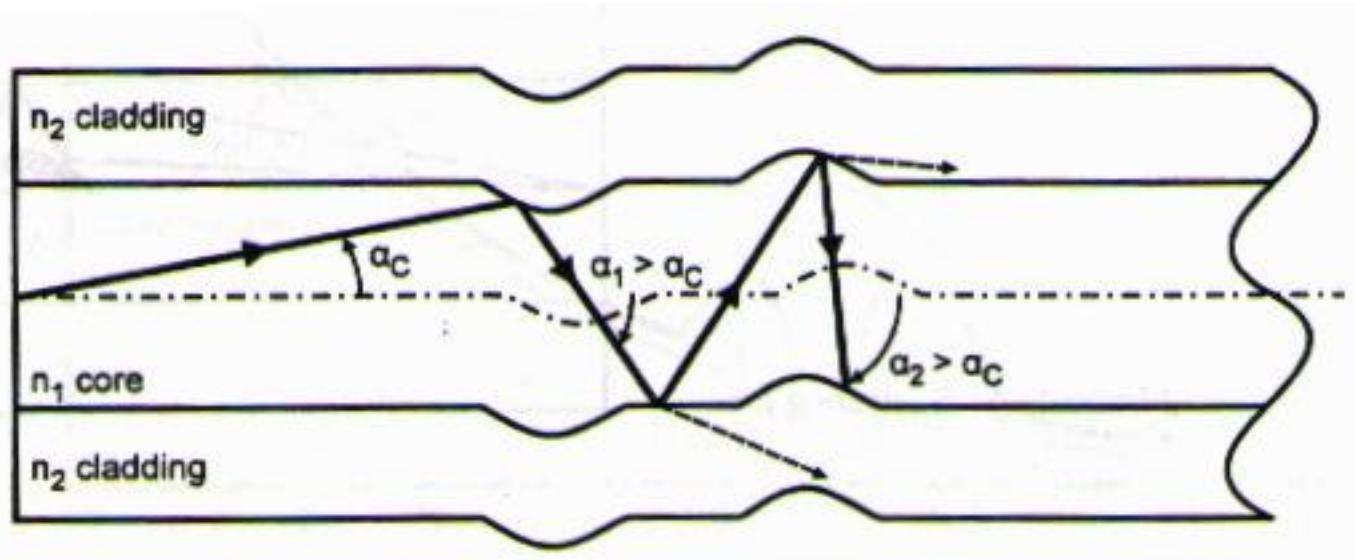


utilizator, **localizat**, dB

$$A = \sum_i A_i$$

$$A = N \cdot A_i$$

# Microcurburi

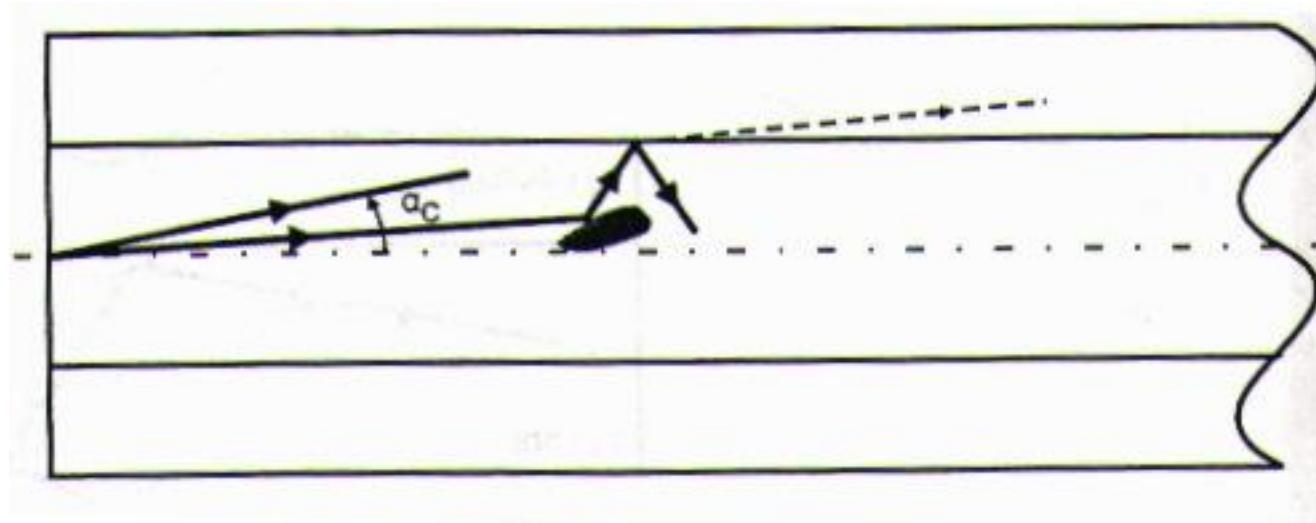


**distribuit, tehnologie, dB/km**

$$A = A_i \cdot L$$

$$A[dB] = A_i[dB/km] \cdot L[km]$$

# Imprastiere

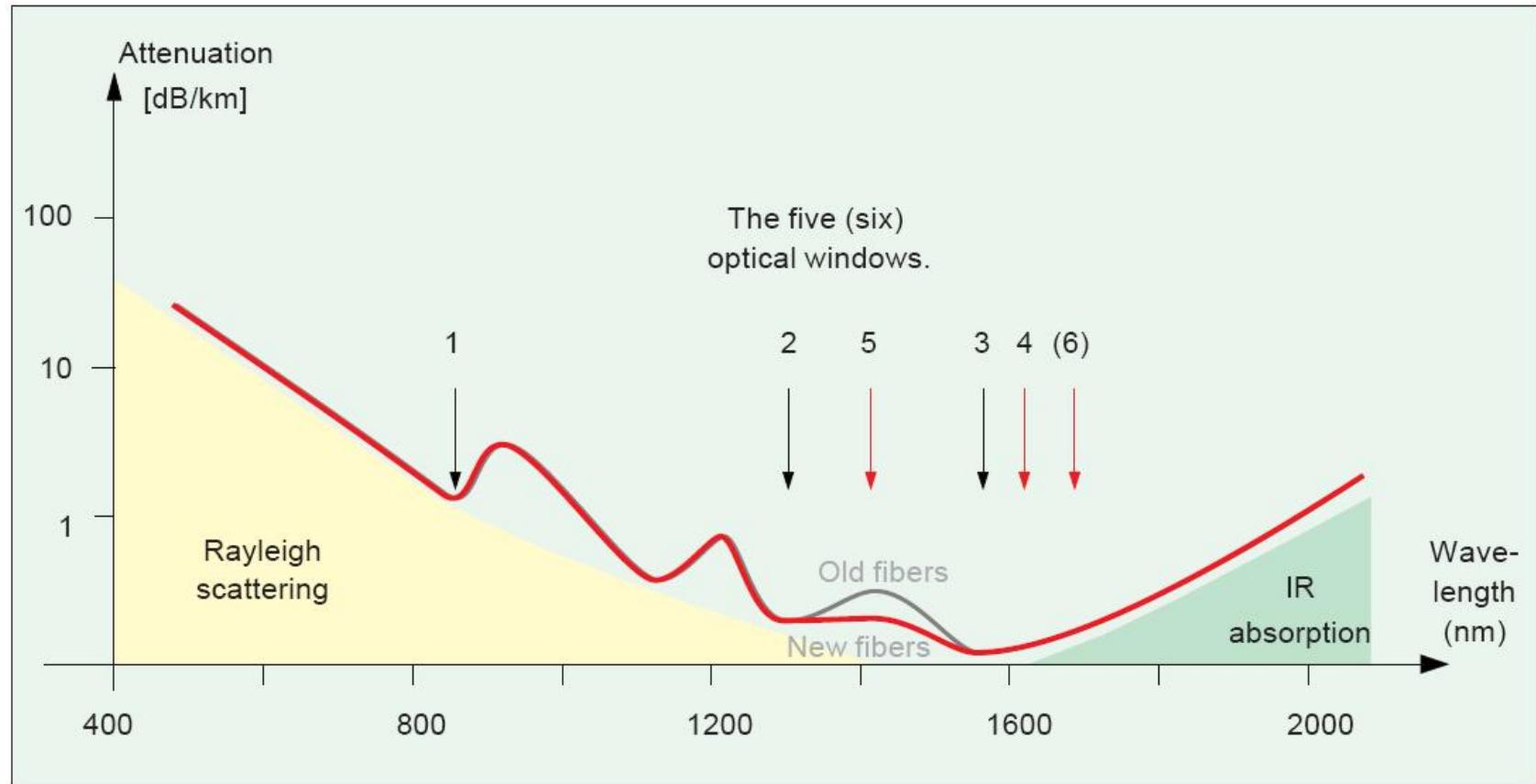


**distribuit, tehnologie, dB/km**

$$A = A_i \cdot L$$

$$A[\text{dB}] = A_i[\text{dB/km}] \cdot L[\text{km}]$$

# Absorbtie

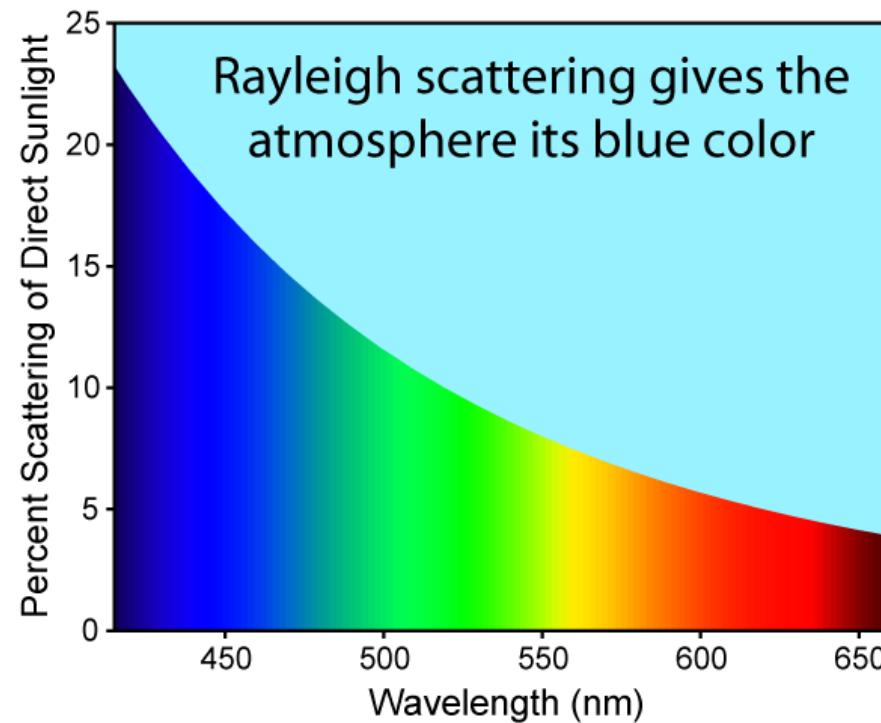


distribuit, material, dB/km

$$A[\text{dB}] = A_i[\text{dB / km}] \cdot L[\text{km}]$$

# Difractie Rayleigh

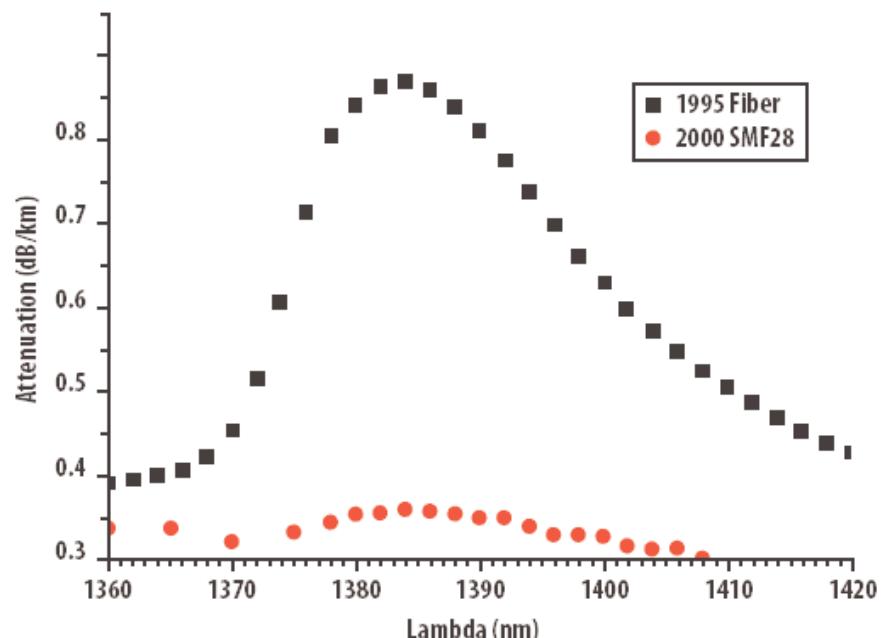
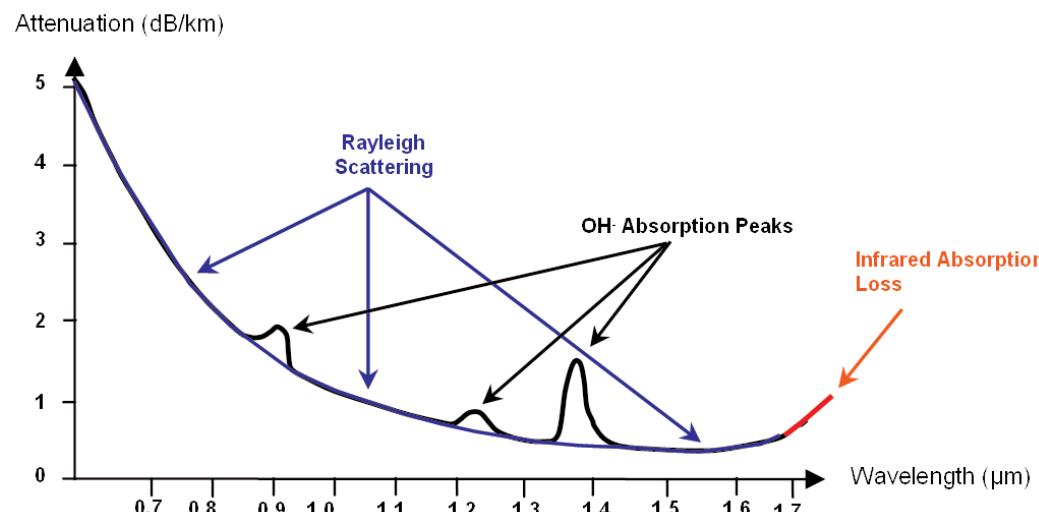
- ▶ imprastierea luminii (si a altor radiatii electromagnetice) de particule (molecule) mult mai mici decat lungimea de unda



$$A \sim \frac{1}{\lambda^4}$$

# Absorbtie OH

- ▶ Absorbtie
  - 950nm
  - 1244nm
  - 1383nm
- ▶ Apa!



Fiber Attenuation Comparison

# Atenuare

$$E_y(z_1) = Ct \cdot e^{-\alpha \cdot z_1} \cdot e^{j(\omega t - \beta \cdot z_1)}$$

$$E_y(z_2) = Ct \cdot e^{-\alpha \cdot z_2} \cdot e^{j(\omega t - \beta \cdot z_2)}$$

$$W, P \sim \int E^2$$

$$A = \frac{P_2}{P_1} = \frac{Ct^2 \cdot e^{-2\alpha \cdot z_2}}{Ct^2 \cdot e^{-2\alpha \cdot z_1}} = e^{-2\alpha \cdot (z_2 - z_1)}$$

$$A[dB] = 10 \log_{10} \frac{P_2}{P_1} = 10 \log_{10} [e^{-2\alpha \cdot (z_2 - z_1)}]$$

$$A[dB] = -20 \cdot \alpha \cdot (z_2 - z_1) \log_{10} e = -8.686 \cdot \alpha \cdot (z_2 - z_1)$$

$$A/L[dB/km] = -8.686 \cdot \alpha < 0$$

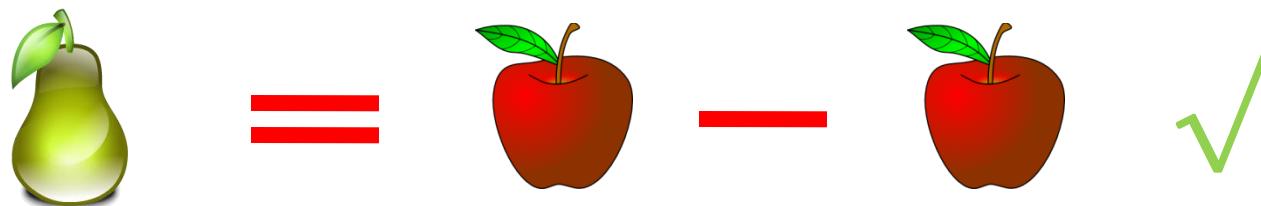
- ▶ Atenuarea se exprima de obicei in **dB/km**
  - ▶ de obicei valori pozitive
  - ▶ semnul = **implicit**

# Calculul atenuarii

$$\text{Pierderi} = \frac{P_{out}}{P_{in}}$$

$$\text{Pierderi [dB]} = [-] 10 \cdot \log_{10} \left( \frac{P_{out}}{P_{in}} \right)$$

$$\text{Pierderi [dB]} = [-] (P_{out} [\text{dBm}] - P_{in} [\text{dBm}])$$



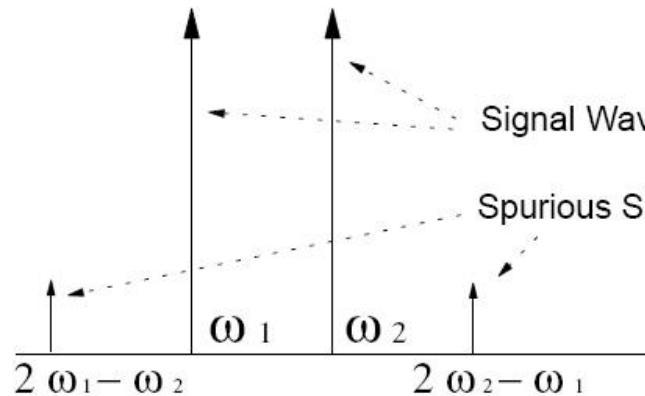
$$\text{Atenuare [dB/km]} = \frac{\text{Pierderi [dB]}}{\text{lungime [km]}}$$

# Efecte neliniare in fibra

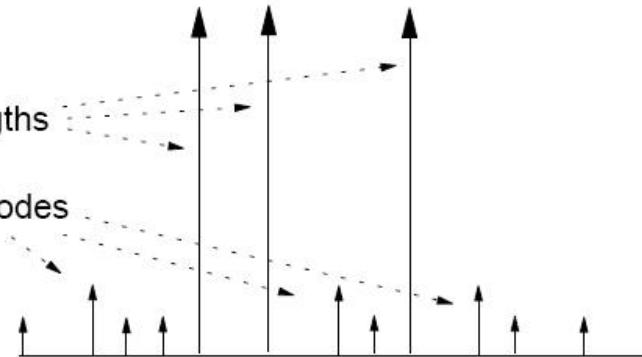
- ▶ Stimulated Brillouin Scattering, SBC
  - difractia luminii inspre emitator datorita undelor mecano-acustice generate in fibra
  - 6–10 dBm
- ▶ Stimulated Raman Scattering, SRS
  - interactiunea luminii cu vibratiile moleculare
  - 27 dBm (~1W)
- ▶ Self Phase Modulation, SPM
  - Frontiera impulsului implica indice de refractie variabil in timp moduland faza impulsului
  - 5 dBm
  - Cross Phase Modulation, CPM
- ▶ Four-Wave Mixing, FWM
  - 0 dBm

# Four-Wave Mixing, FWM

Two Channels



Three Channels

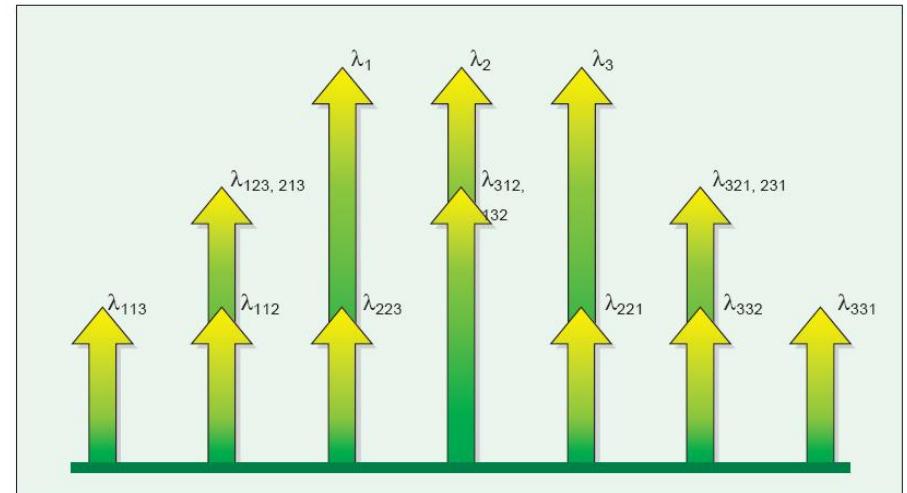


$$NL = \frac{1}{2} (N^3 - N^2)$$

$N = 2, NL = 4$

$N = 3, NL = 9$

$N = 16, NL = 1920$

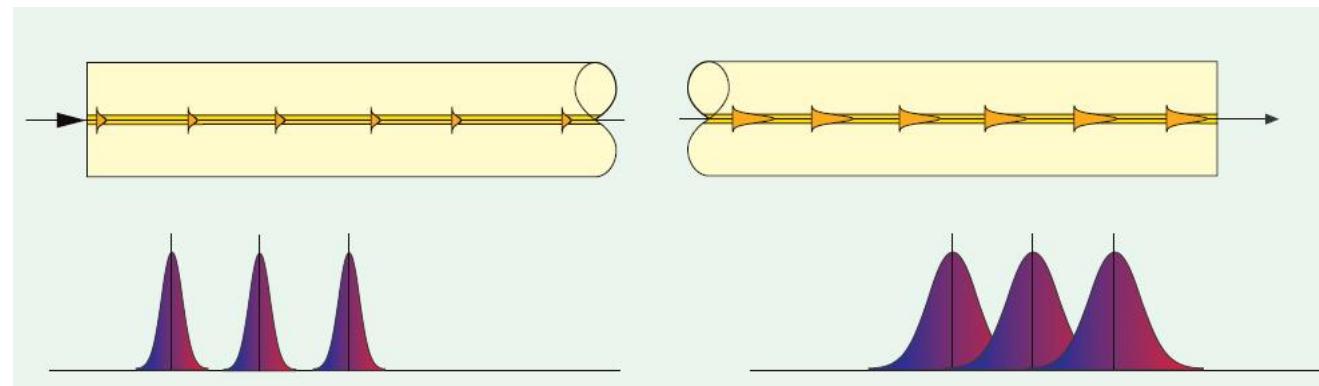


# Fenomene de interes

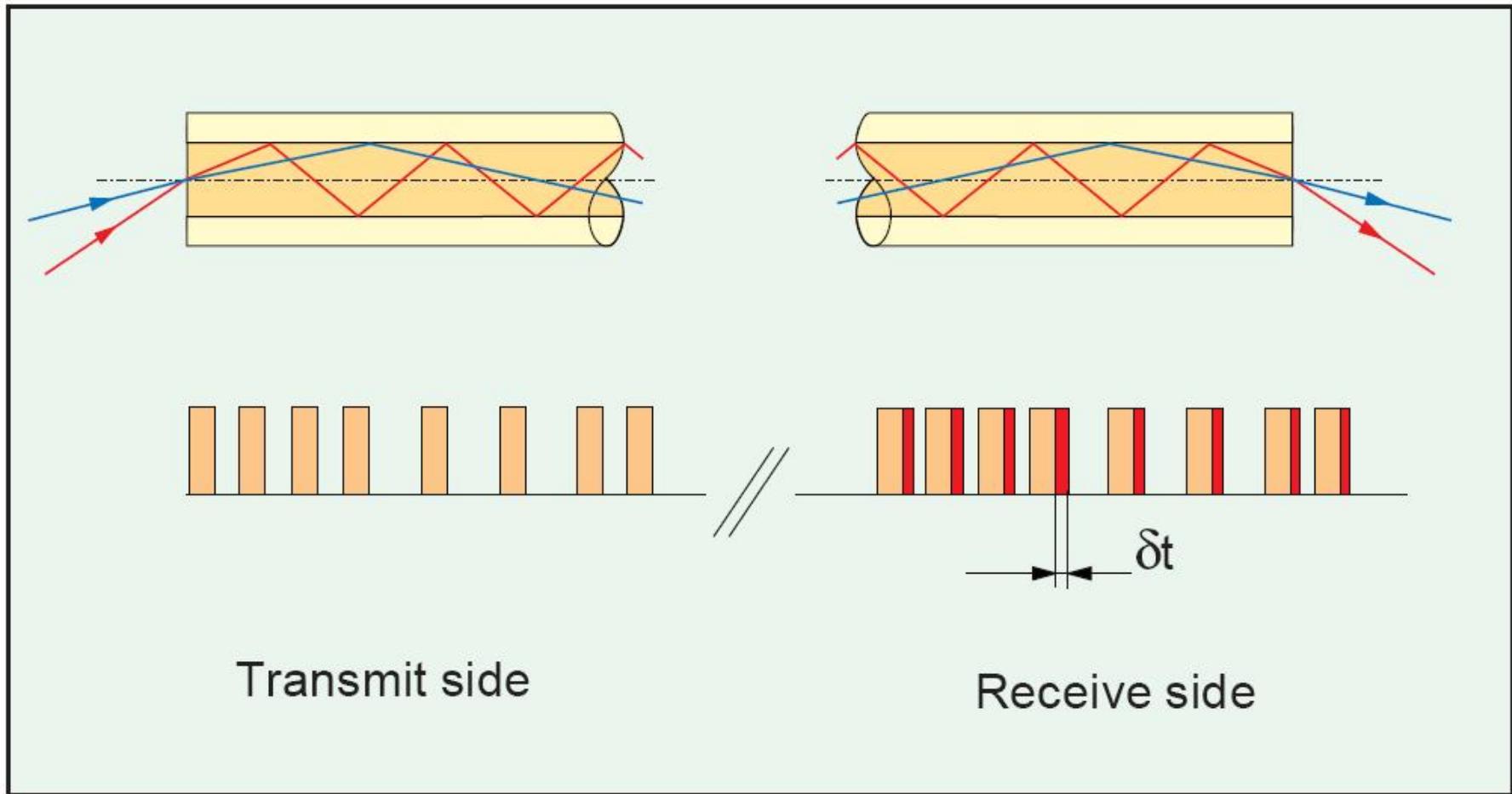
- ▶ Cat de departe pot transmite semnalul luminos pe fibra
  - atenuare
- ▶ Cat de rapid pot transmite informația
  - **dispersie**

# Dispersia

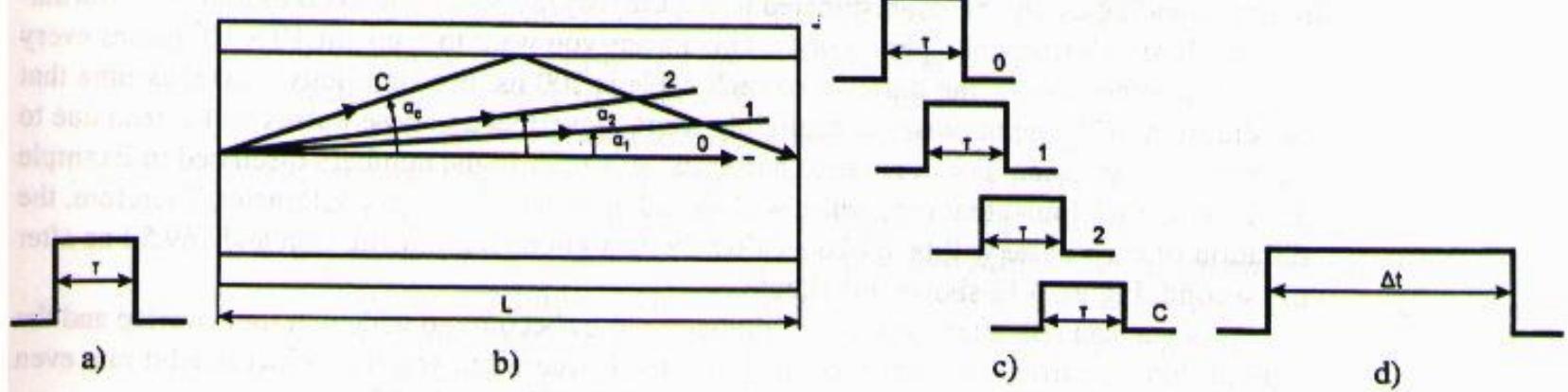
- ▶ Propagarea cu viteze diferite a radiatiilor cu lungimi de unda diferite
  - intermodala (modala – depinde de prezența modurilor)
  - intramodala (cromatică – depinde de lungimea de undă)
    - de material
    - de ghid



# Dispersia modala



# Dispersia modala



$$t_0 = \frac{L}{v}$$

$$t_C = \frac{L}{v \cdot \cos \alpha_C}$$

$$v = \frac{c}{n_2}$$

$$\cos \alpha_C = NA$$

$$\Delta t_{SI} = t_C - t_0 = \frac{L \cdot n_2}{c} \cdot \left( \frac{n_2 - n_1}{n_2} \right)$$

$$\Delta = \frac{n_2 - n_1}{n_1} \ll 1$$

$$\Delta t_{SI} = t_C - t_0 = \frac{L \cdot n_2}{c} \cdot \Delta$$

$$\Delta t_{SI} = t_C - t_0 \approx \frac{L}{2 \cdot c \cdot n_2} \cdot (NA)^2$$

# Dispersia modala

## ► salt de indice

$$dt = \frac{L \cdot n_2^2}{c \cdot n_1} \left( \frac{n_2 - n_1}{n_2} \right) \approx \frac{L \cdot NA^2}{2 \cdot c \cdot n_2}$$

intarzierea intre  
moduri cand

$$\Delta = \frac{n_2 - n_1}{n_1} \ll 1$$

$$\Delta \tau_{\text{mod}}^2 = \frac{1}{3} \left( \frac{dt}{2} \right)^2$$

$$\Delta \tau_{\text{mod}} \approx \frac{L \cdot n_2 \cdot \Delta}{2\sqrt{3} \cdot c} \approx \frac{L \cdot NA^2}{4\sqrt{3} \cdot c \cdot n_2}$$

## ► indice gradat

$$dt = \frac{L \cdot n_2 \cdot \Delta^2}{2c} \approx \frac{L \cdot NA^4}{8 \cdot c \cdot n_2^3}$$

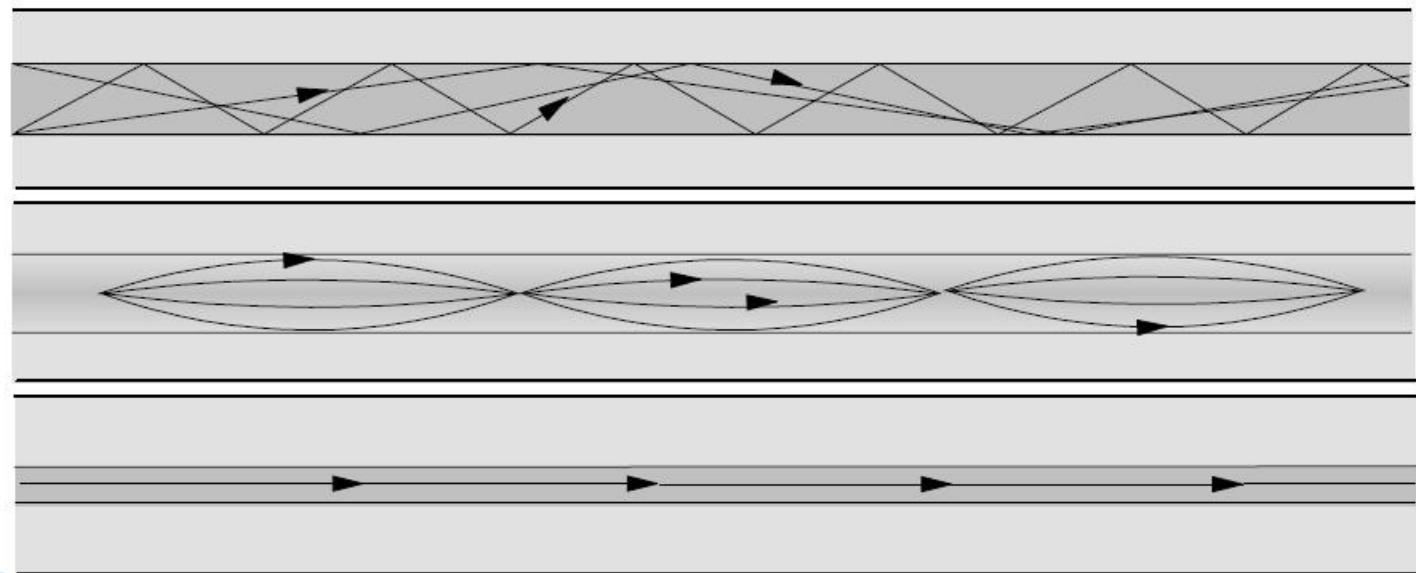
$$NA = 0.1 \div 0.2 < 1$$

$$\Delta \tau_{\text{mod}} \approx \frac{L \cdot n_2 \cdot \Delta^2}{4\sqrt{3} \cdot c}$$

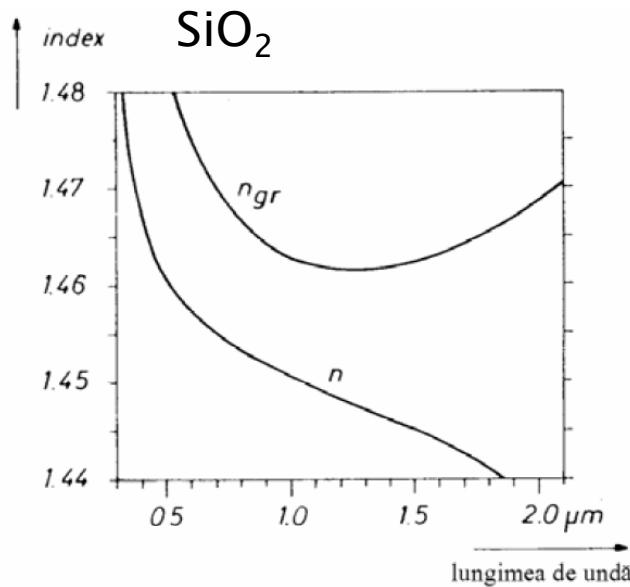
$n_2$  - miez  
 $n_1$  - teaca  
 $n_2 > n_1 !!$

# Dispersia modala

- ▶ Mai mare la fibre multimod cu salt de indice
- ▶ Mai mica la fibre multimod cu indice gradat
  - traseele mai lungi trec prin zone cu indice mai mic
- ▶ Inexistenta la fibrele monomod

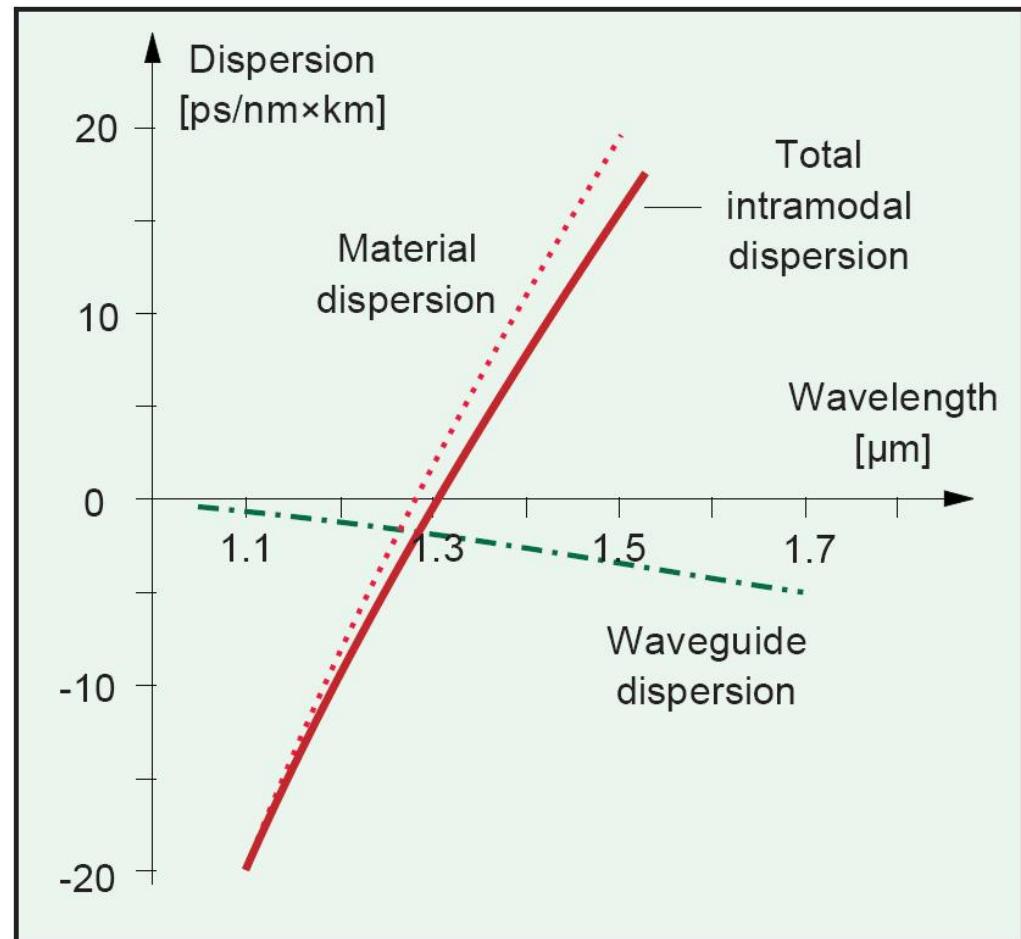


# Dispersia de material



$$n_{gr} = n - \lambda \frac{dn}{d\lambda}$$

$$\Delta\tau_{mat} = \frac{L \cdot \lambda \cdot \Delta\lambda}{c} \cdot \frac{d^2n}{d\lambda^2}$$

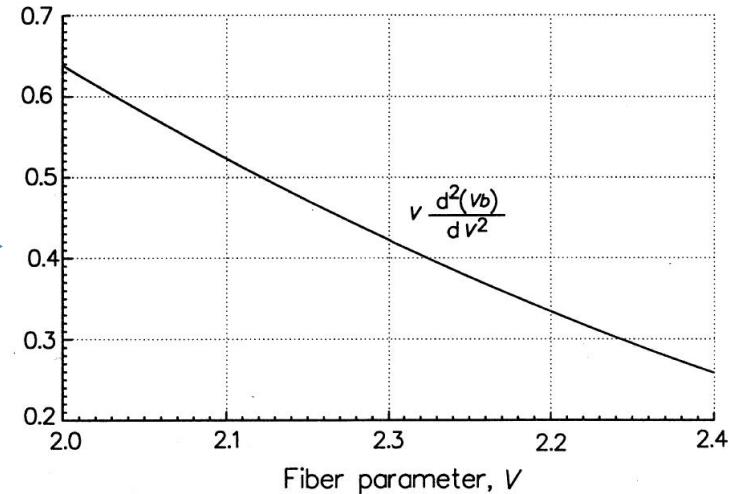
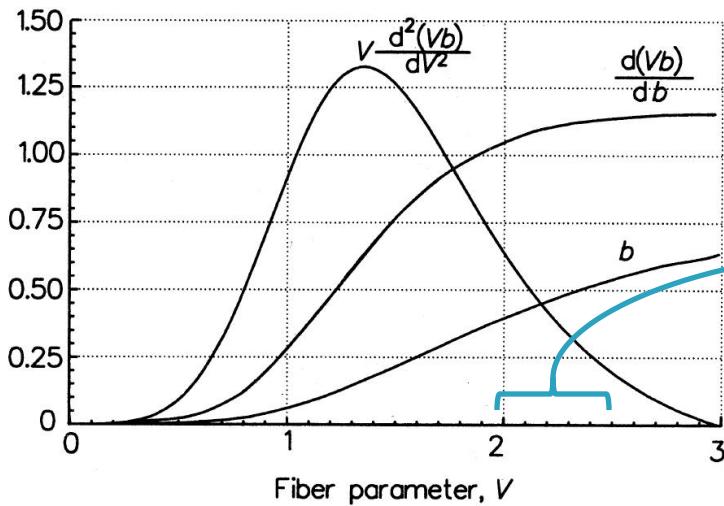


# Dispersia de ghid

- ▶ Neglijabila in fibrele multimod fata de dispersia modală

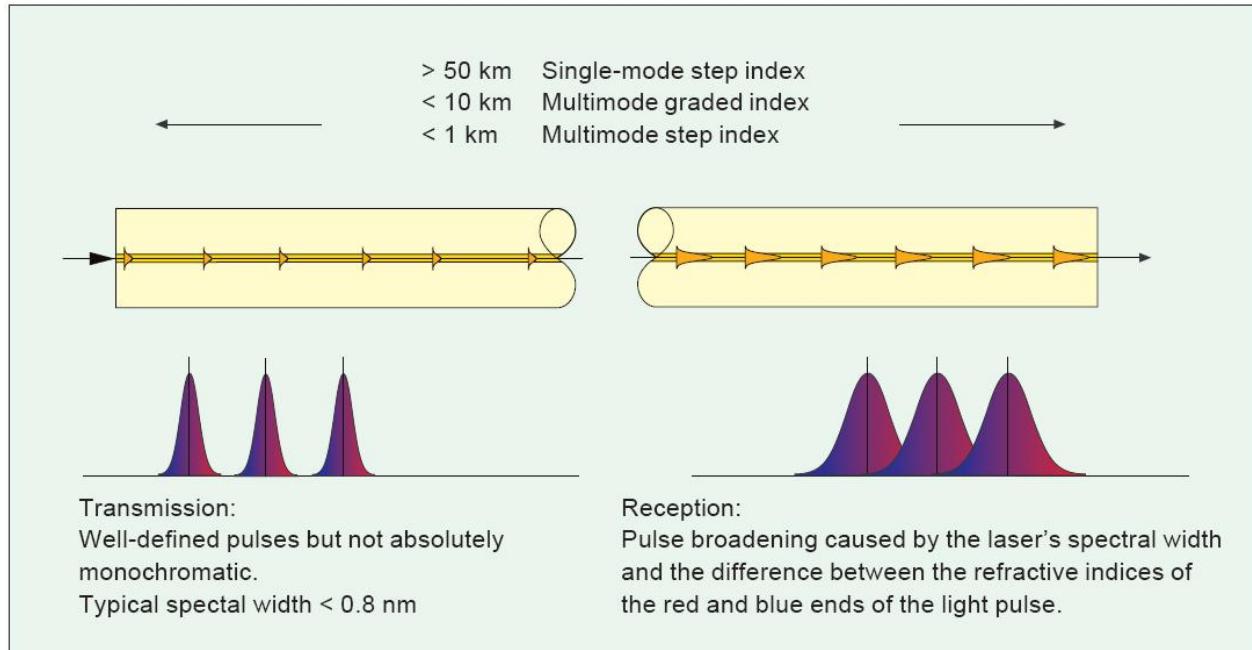
$$\Delta\tau_{gh} = \frac{n \cdot L \cdot \Delta}{c} \cdot \frac{\Delta\lambda}{\lambda} \cdot \left( V \frac{d^2(Vb)}{dV^2} \right)$$

b - constanta de propagare  
normalizata



$$V \leq V_C = 2.405$$

# Dispersia cromatica (gh+mat)



$$\Delta\tau_{cr} = D(\lambda) \cdot \Delta\lambda \cdot L$$

$$D(\lambda) = \frac{S_0}{4} \cdot \left( \lambda - \frac{\lambda_0^4}{\lambda^3} \right)$$

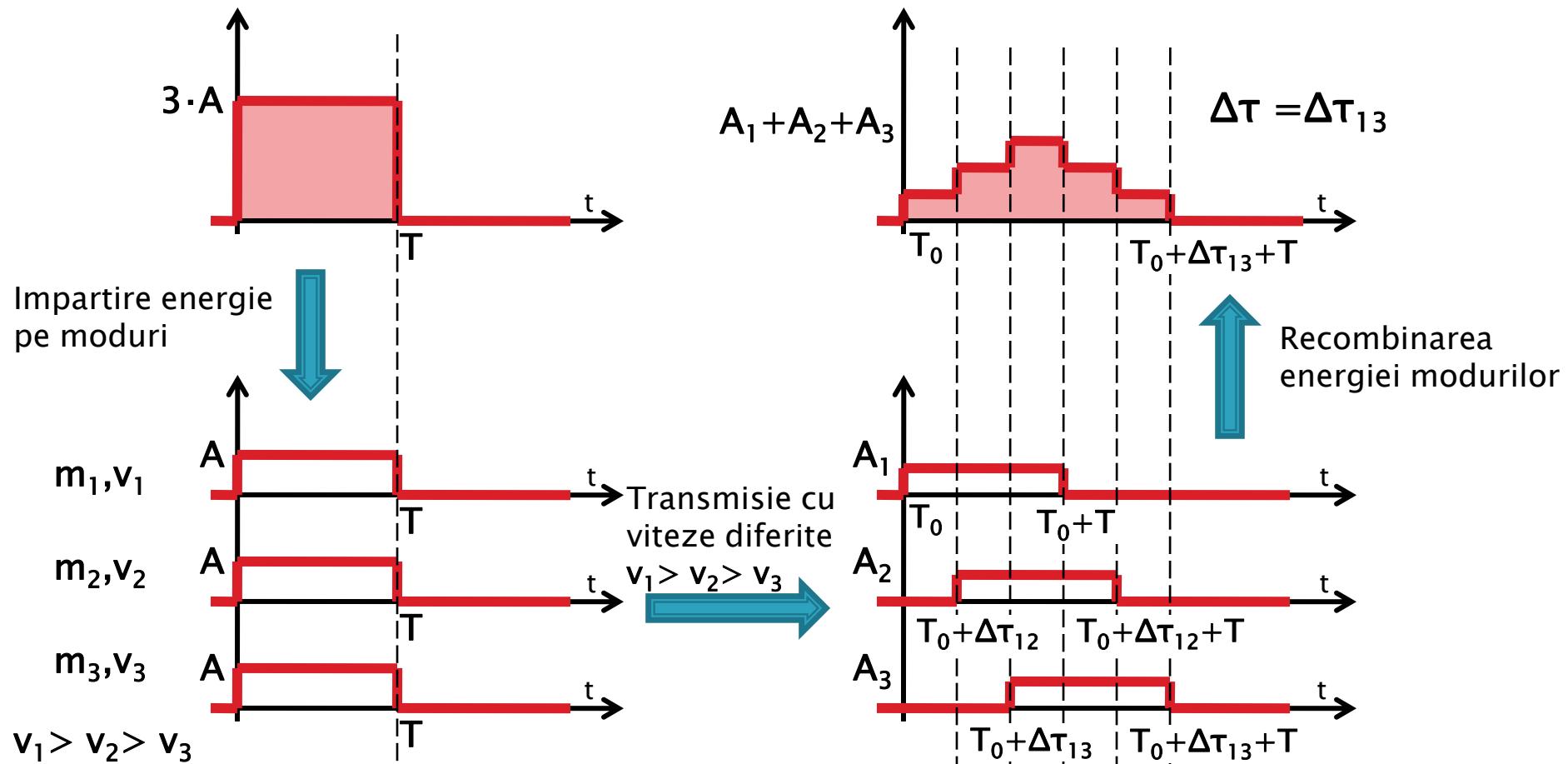
$S_0$  panta dispersiei –  
 $\text{ps}/\text{nm}^2/\text{km}$

$$D(\lambda_0) = 0$$

- ▶  $D(\lambda) \approx 100 + 0.4 (850 - \lambda)$  [ps/nm/km]  
pentru  $800 < \lambda < 900$  nm
- ▶  $D(\lambda) \leq 3,5$  ps/nm/km  
pentru  $1285 < \lambda < 1330$  nm
- ▶  $D(\lambda) \leq 17$  ps/nm/km  
pentru  $1525 < \lambda < 1575$  nm

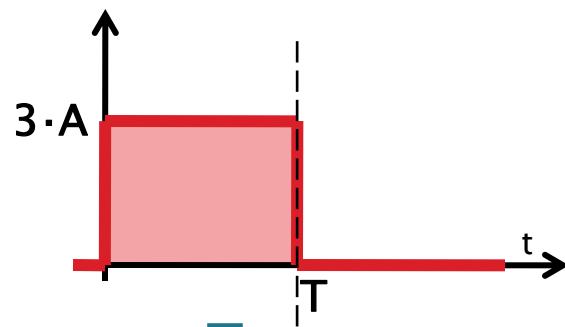
$$D(\lambda) = \frac{S_0}{4} \cdot \left( \lambda - \frac{\lambda_0^4}{\lambda^3} \right)$$

# Dispersia modala

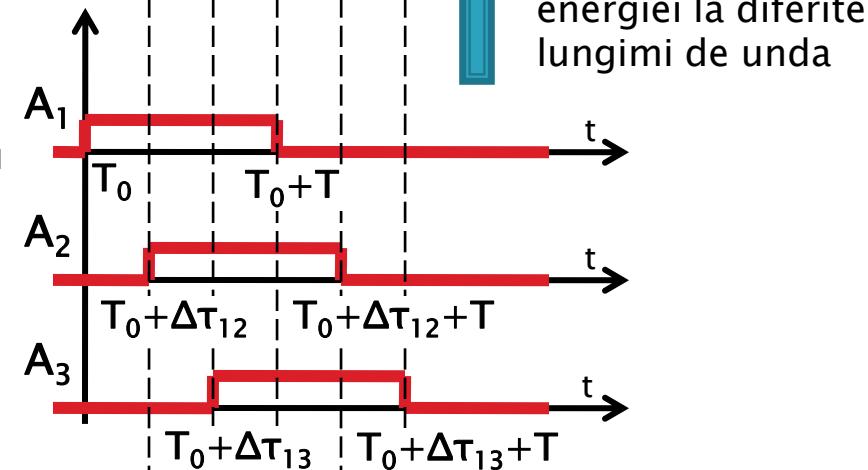
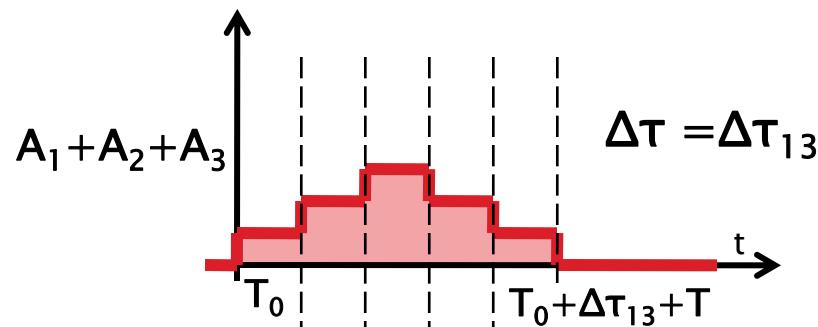
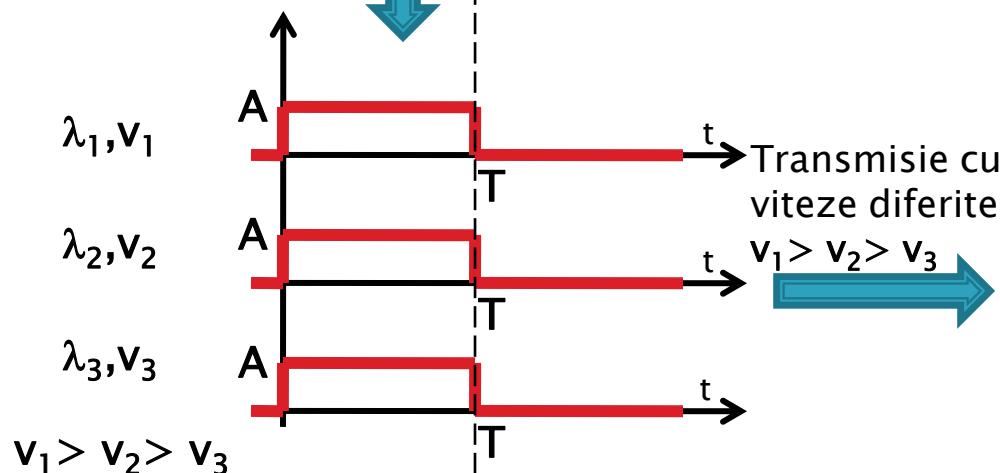


Conceptual  $\rightarrow f(t) = \int_{-\infty}^{\infty} g(\omega) \cdot e^{j\omega t} d\omega$

# Dispersia cromatică (gh+mat)

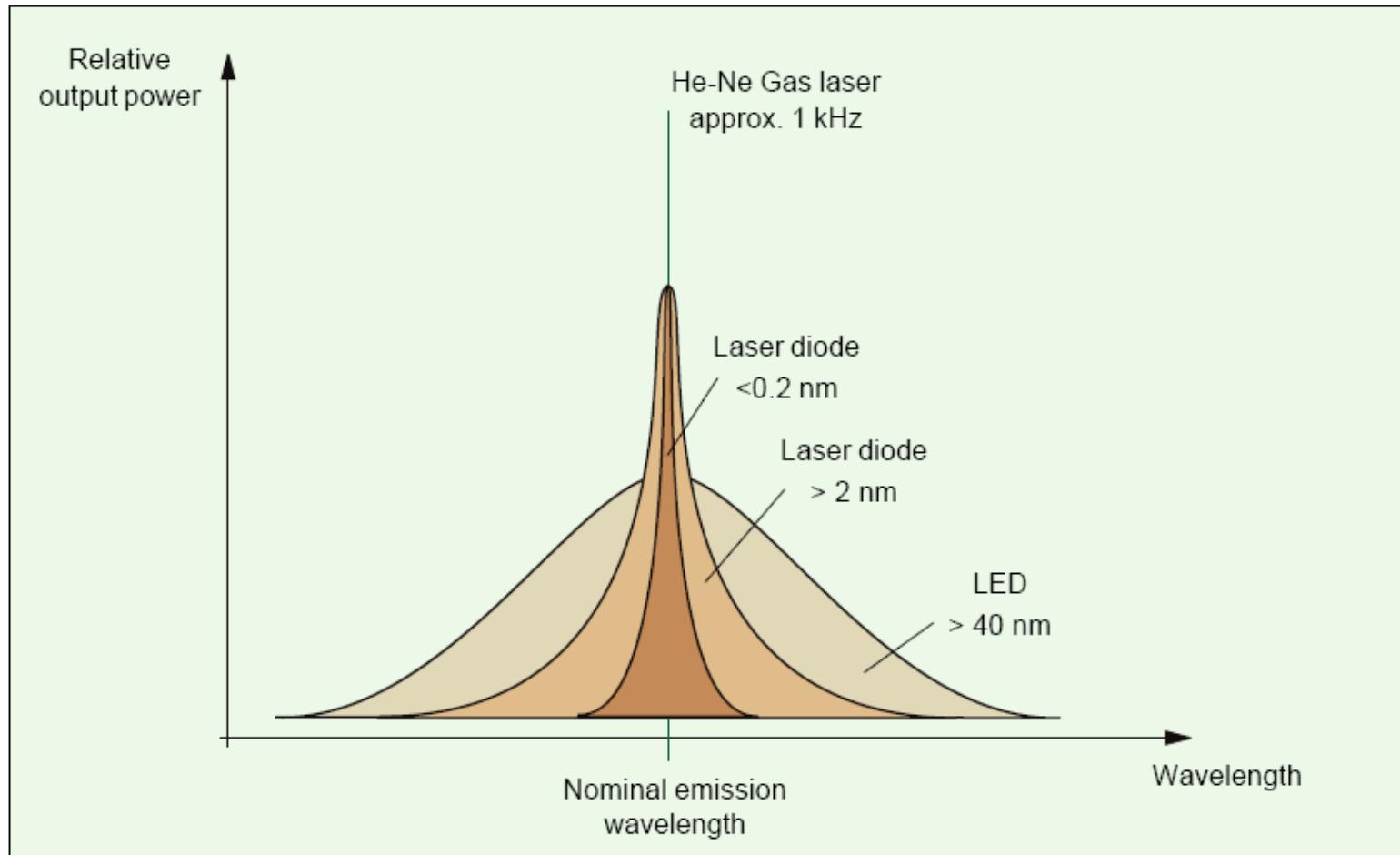


Impartire energie pe lungimi de unda



Efectiv →  $f(t) = \int_{-\infty}^{\infty} g(\omega) \cdot e^{j\omega t} d\omega$

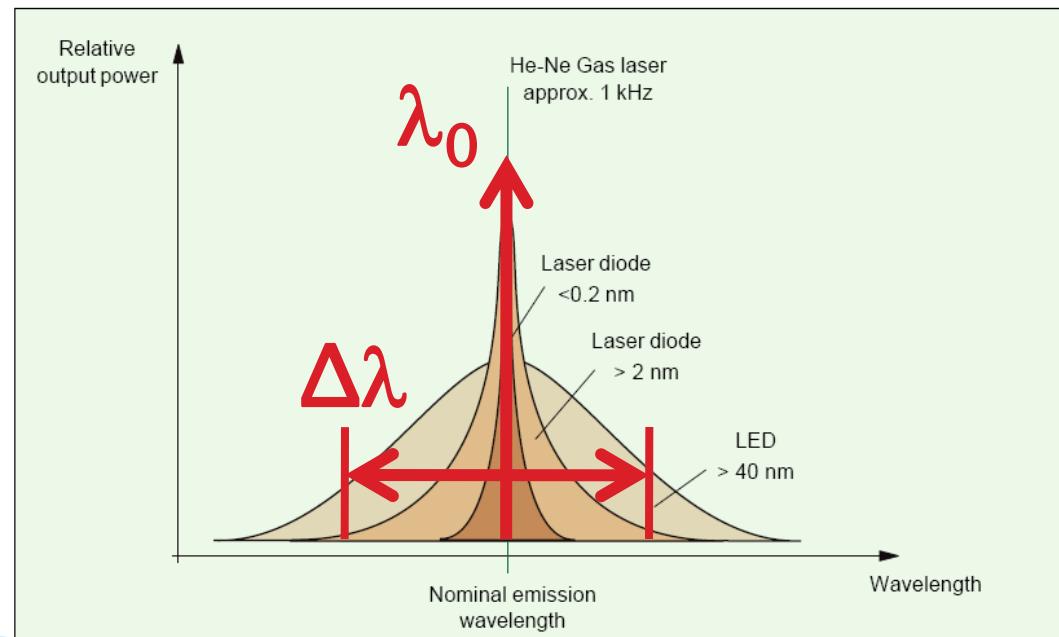
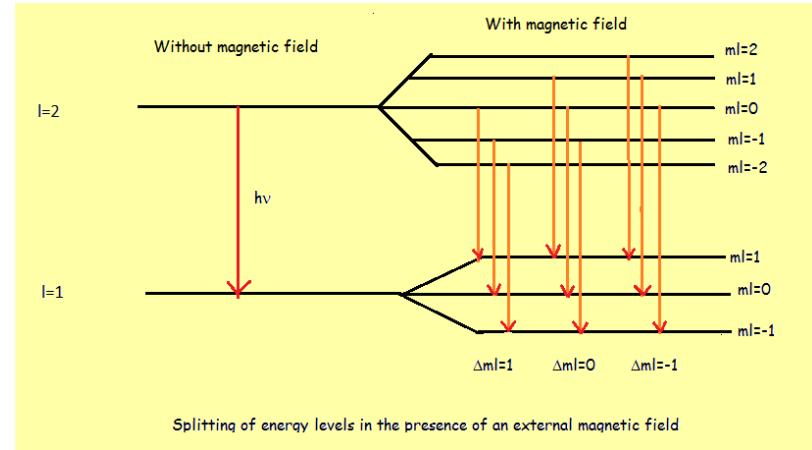
# Calitatea spectrală a emițătorilor optici



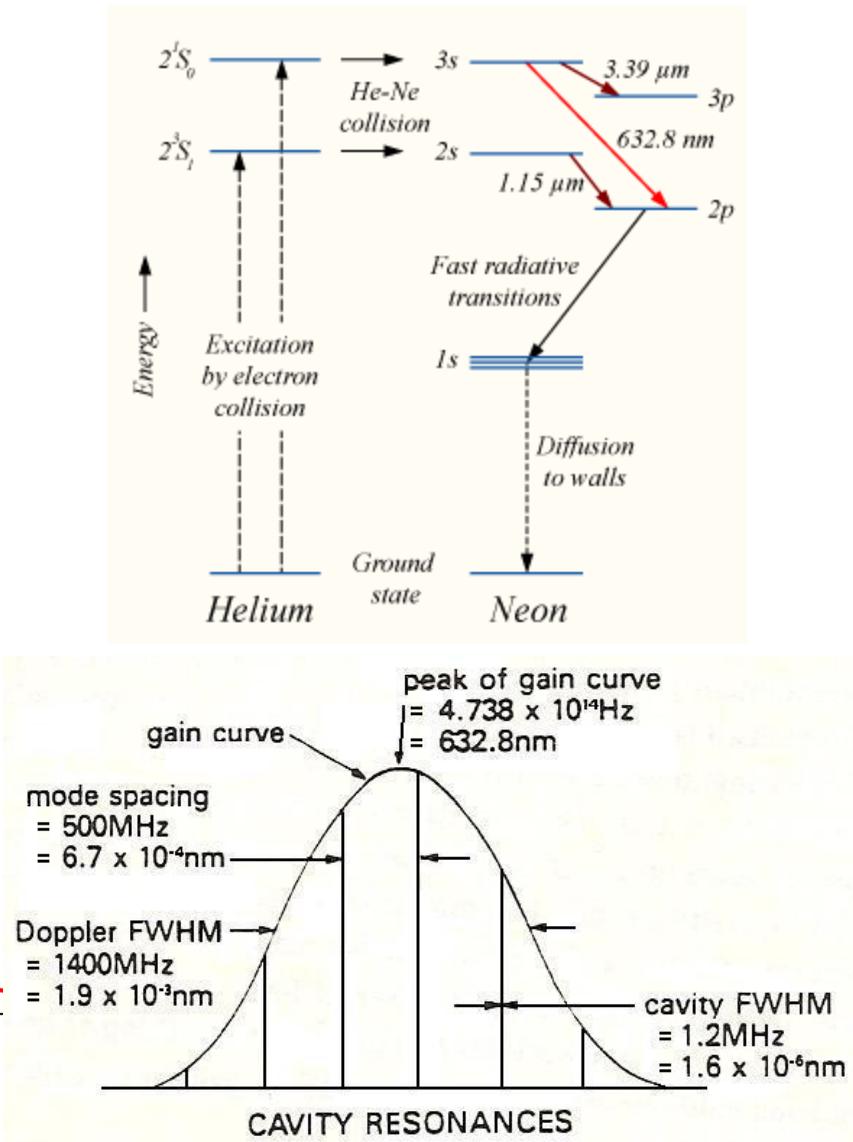
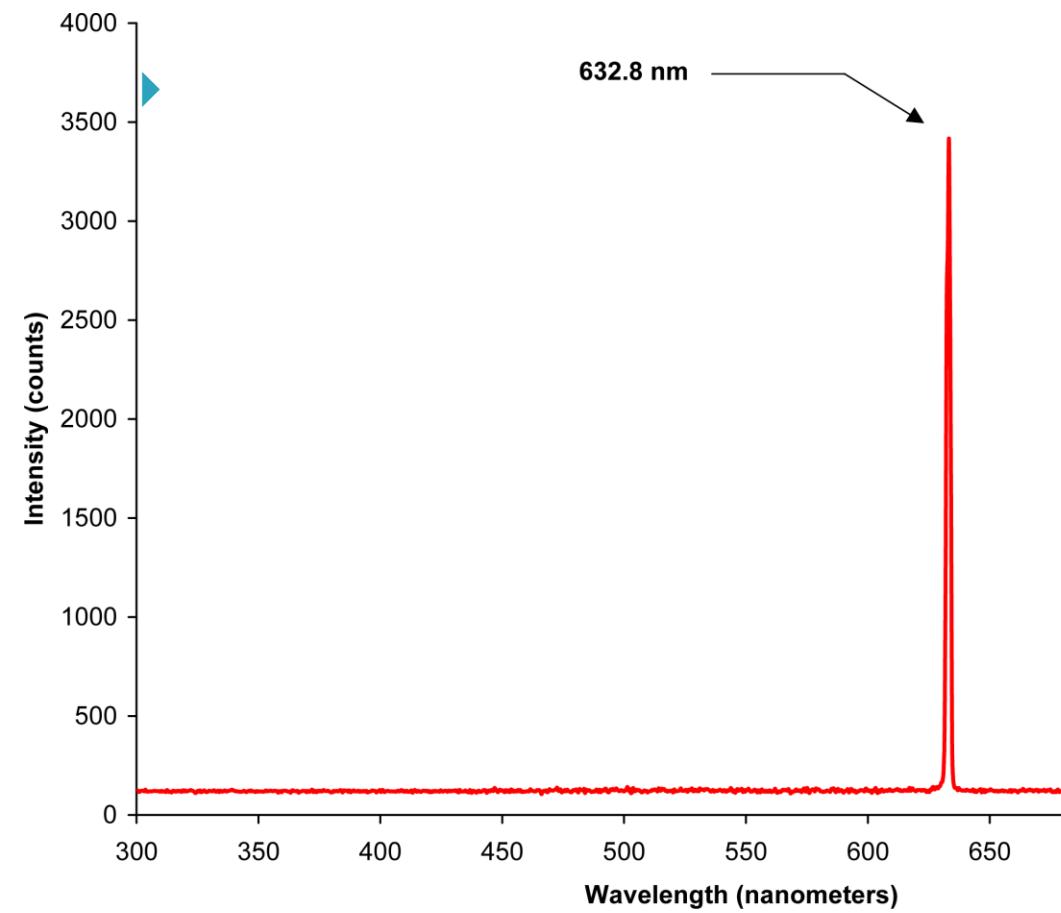
# Calitatea spectrală a emițătorilor optici

- ▶ degenerarea nivelelor energetice duce la aparitia benzilor energetice
- ▶ Multitudinea de tranzitii posibile intre cate doua nivele situate in benzi energetice diferite duce la largirea caracteristicii spectrale a surselor

$$\lambda_0 \rightarrow \left[ \lambda_0 - \frac{\Delta\lambda}{2}, \lambda_0 + \frac{\Delta\lambda}{2} \right]$$



# He-Ne Laser



$$\Delta\lambda = 0.002 \text{ nm}$$

# Contact

- ▶ Laboratorul de microunde si optoelectronica
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- ▶ [rdamian@etti.tuiasi.ro](mailto:rdamian@etti.tuiasi.ro)