

Optoelectrică

Curs 3

2021/2022

Disciplina 2021/2022

- ▶ 2C/1L Optoelectronicaă **OPTO**
- ▶ **Minim 7 prezente curs + laborator**
- ▶ Curs – conf. Radu Damian
 - an IV μE
 - Luni 08(:10)–10:00, online, Microsoft Teams
 - E – 70% din nota (50+20), online, rf-opto
 - **20% test (VP) la curs**, saptamana 4–6?
 - probleme + (? 1 subiect teorie) + (2p prez. curs)
 - **toate materialele permise**
- ▶ Laborator – sl. Daniel Matasaru
 - an IV μE
 - Marti 14-18 impar/par
 - Max. 7 prezente
 - L – 30% din nota (+Caiet de laborator)

Orar 2021/2022

► Curs

- Luni 8–10, online
- ~~2C \Rightarrow 3C~~
 - ~~$14 \cdot 2/3 \approx 9.33$~~
 - ~~$9 : 10 \text{ C} \approx 9\text{C} + \text{E}$~~

Online

- ▶ acces la **examene** necesita **parola** primita prin **email**

English | Romana |

Start Didactic Master Colectiv Cercetare Studenții Note Lista Studenti Examene Fotografii

POPESCU GOPO ION

Fotografia nu există

Date:

Grupa	5700 (2019/2020)
Specializarea	Inginerie electronica si telecomunicatii
Marca	7000021

Acceseaza ca acest student | [Ieșire acces la licență](#)

Note obtinute

Inca nu a fost notat.

Start Didactic Master Colectiv C

Note Lista Studenti Examene Fotografii

Identificare

Introduceti numele si adresa de email utilizata la inscriere

Nume
POPESCU GOPO

E-mail/Parola

Introduceti codul afisat mai jos

4db4457

Trimite

Online

- ▶ acces email/parola

Start Didactic Master Colectiv

Note Lista Studenti Examene Fotografii

POPESCU GOPO ION

Fotografia nu există

Date:

Grupa	5700 (2019/2020)
Specializarea	Inginerie electronică
Marca	7000021

Se acceseaza site-ul **ca acest student!**

Start Didactic Master Colectiv

Note Lista Studenti Examene Fotografii

POPESCU GOPO ION

Fotografia nu există

Date:

Grupa	5700 (2019/2020)
Specializarea	Inginerie electronica s
Marca	7000021

Se acceseaza site-ul **ca acest student (inclusiv examene)!**

Parola

► primita prin email

Important message from RF-OPTO

Inbox x

Radu-Florin Damian
to me, POPESCU

Romanian ▾ English ▾ Translate message

 Laboratorul de Microunde si Optoelectronica
Facultatea de Electronica, Telecomunicatii si Tehnologia Informatiei
Universitatea Tehnica "Gh. Asachi" Iasi

In atentia: POPESCU GOPO ION
Parola pentru a accesa examenele pe server-ul rf-opto este
Parola: [REDACTED]

Identificati-vă pe [server](#), cu parola, cat mai rapid, pentru confirmare.

Memorati acest mesaj intr-un loc sigur, pentru utilizare ulterioara

Attention: POPESCU GOPO ION
The password to access the exams on the rf-opto server is
Password: [REDACTED]

Login to the [server](#), with this password, as soon as possible, for confirmation.
Save this message in a safe place for later use

Reply Reply all Forward

Important message from RF-OPTO

Validation of MDCK exam from 02/05/2020

From Me <rdamian@etti.tuiasi.ro>
Subject: Important message from RF-OPTO

To [REDACTED]
Cc Me <rdamian@etti.tuiasi.ro>

 Laboratorul de Microunde si Optoelectronica
Facultatea de Electronica, Telecomunicatii si Tehnologia Informatiei
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Password: [REDACTED]

Login to the [server](#), with this password, as soon as possible, for confirmation.
Save this message in a safe place for later use

Manual examen online

- ▶ Aplicatia de examen online utilizata intens la:
 - curs (prezenta)
 - miniteste
 - examen

Materials

Other data

[Manual examen on-line \(pdf, 2.65 MB, ro, !\[\]\(9dfdaff1d86ba3c1f8353b4d1b61b8c5_img.jpg\)](#)

[Simulare Examen \(video\) \(mp4, 65.12 MB, ro, !\[\]\(83f22ed94ec5517769dd76d702c6bfd8_img.jpg\)](#)

Microwave Devices and Circuits (English)

Examen online

► intotdeauna **contratimp**

- perioada lunga (prezenta curs/rezultate laborator)
- perioada scurta (teste: 15min, examen: 2h)

Start Didactic Master Colectiv Cercetare **Studenti**

Note Lista Studenti **Examene** Fotografii

Anunț
17:28 (29/04/2020)

Material suport
17:30 (29/04/2020)

Subiecte
17:32 (29/04/2020)

Rezultate
17:35 (29/04/2020)

Finalizare
17:45 (29/04/2020)

Confirmare
17:45 (30/04/2020)

Ormatorul interval de timp in.
01 m 08 s
[Reincarca acum](#)

Anunț

In acest examen se verifica diverse actiuni ale studentilor pentru examen

Ora pe server

Roate examenele sunt bazate pe fusul orar al server-ului (ar putea sa fie diferit de timpul local). Pentru referinta ora pe server este acum:

29/04/2020 17:28:51

Introducere

Capitolul 1

Aplicatii majore

▶ Comunicatii

- Infrarosu (InGaAsP)

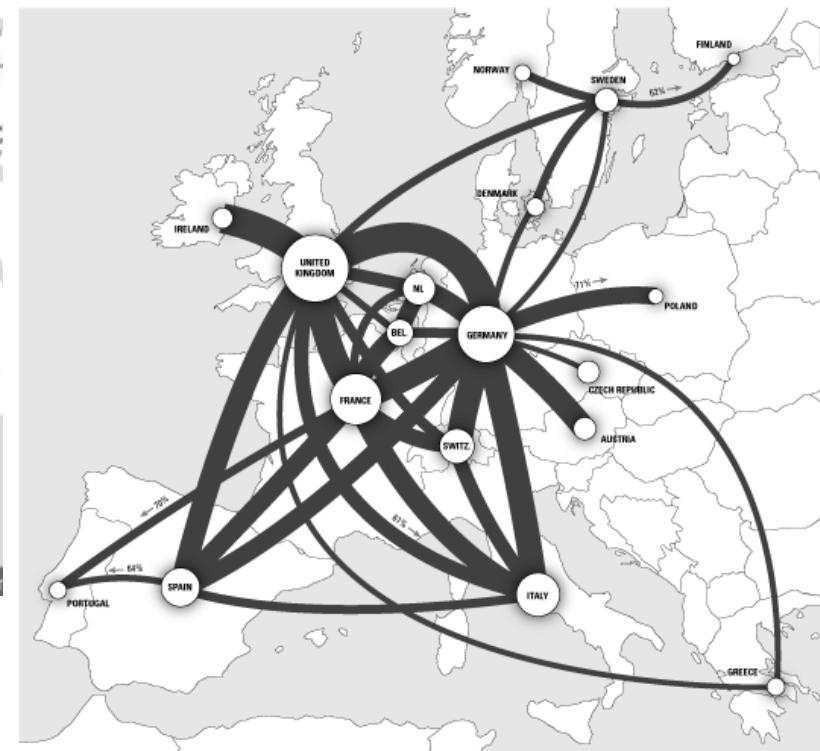
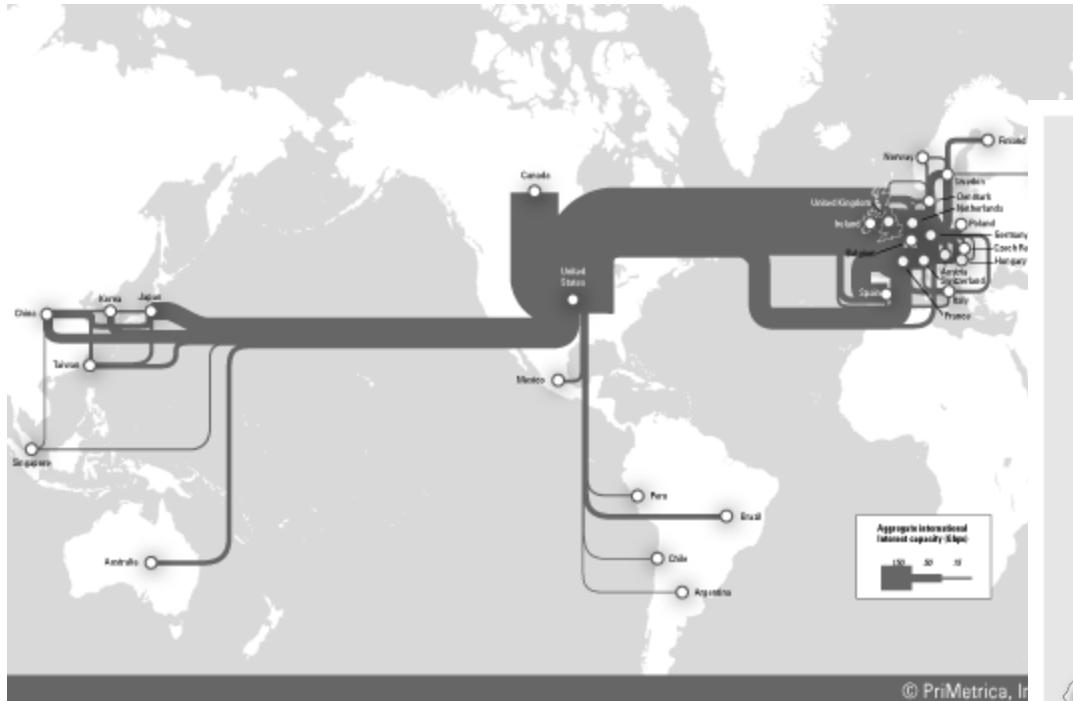
▶ Vizibil

- Spectru vizibil (GaAlAs)

▶ Iluminare

- Putere ridicata, lumina alba (GaN)

Internet Backbone



Key

All figures are given in millions of minutes of telecommunications traffic for the public telephone network.



The map shows all intra-European routes with a combined 2004 volume of more than 300 million minutes.



Each band is proportional to the total annual outgoing traffic from each country.

On routes where traffic in one direction accounts for more than 80 percent of the total, an arrow shows the direction most of the traffic flows.

Avantajele comunicațiilor prin fibra optică – 1

- ▶ Greutate și volum
- ▶ Costul materialelor primare
 - SiO_2/Cu
- ▶ Capacitate de transmisie a informației $f \sim 200\text{THz}$
 - 15.5 Tbit/s @ 7000 km, 69.1Tb/s @ 240km
 - 159 Tb/s @ 1045 km
 - Banda (Viteza) x Distanță [MHz · km] [? MHz/km]
- ▶ Lipsa conexiunilor electrice
 - Bucle de masă (1–2V/km)
 - Siguranță în exploatare
 - Imunitate la fulgere/lipsa scânteilor

Avantajele comunicării prin fibra optică – 2

- ▶ Imunitate la interferență electromagnetică
- ▶ Distanța între repetoare
 - 100km/2–5km
- ▶ Posibilitate de creștere a capacitatii de transmisie a informației
 - Teoretic extrem de mare (aproape infinită) $f \sim 200\text{THz}$
 - Reutilizarea cablurilor existente
- ▶ Securitate
 - Interceptare dificilă și detectabilă
 - Inserare de semnal practic imposibilă

Dezavantajele comunicațiilor prin fibra optică

- ▶ Conexiuni complexe și esențiale
 - Costul circuitelor integrate cresut considerabil de cuplarea luminii în fibra
- ▶ Curbarea cablurilor optice
- ▶ Dezvoltarea greoaie a standardelor
- ▶ Optica folosită strict pentru transmisie (aproape)
 - EDFA – Erbium Doped Fiber Amplifier
- ▶ Sensibilitate la radiații gama și câmpuri electrice intense
- ▶ Rozătoare și termite

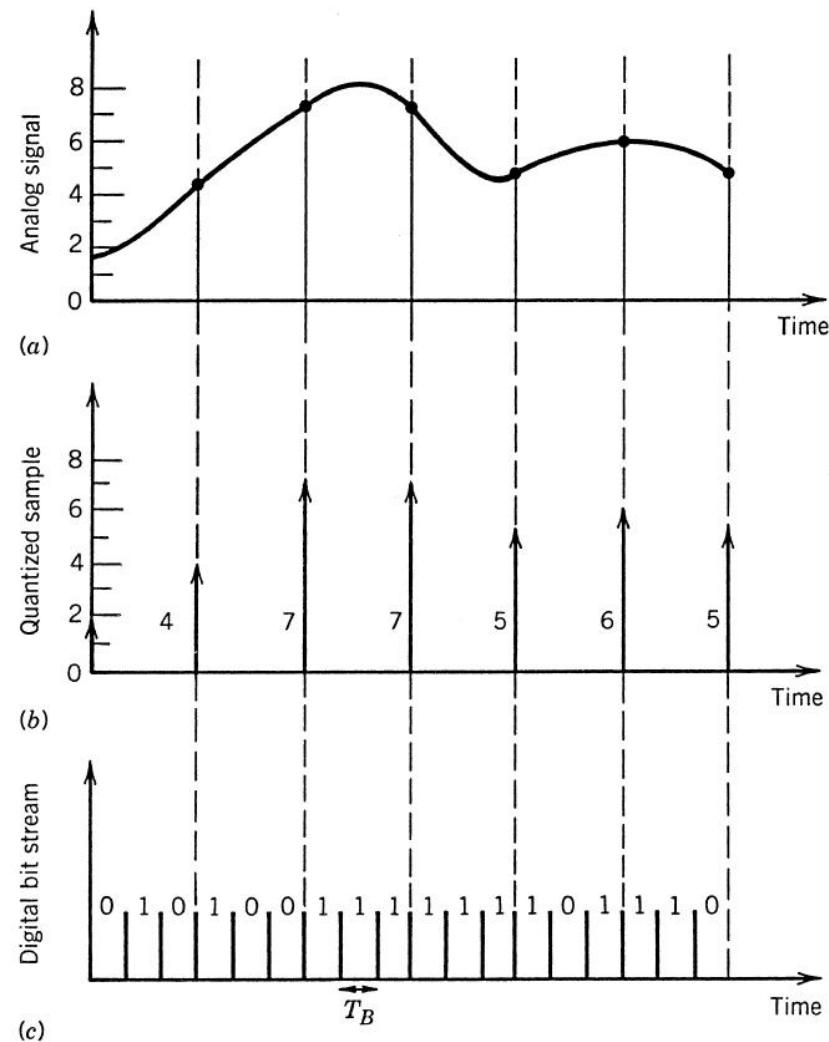
Esantionare

- ▶ pulse-position modulation
- ▶ pulse-duration modulation
- ▶ pulse-code modulation (PCM)
- ▶ esantionare (Nyquist)

$$f_s \geq 2 \cdot \Delta f$$

- ▶ cuantizare **M** intervale discrete
- ▶ zgomot de cuantizare
- ▶ minimizat

$$M \geq \frac{A_{\max}}{A_N}$$



Esantionare

- ▶ pulse-code modulation (PCM)
- ▶ cuantizare **M** intervale discrete, codificate cu **m** biți

$$M = 2^m$$

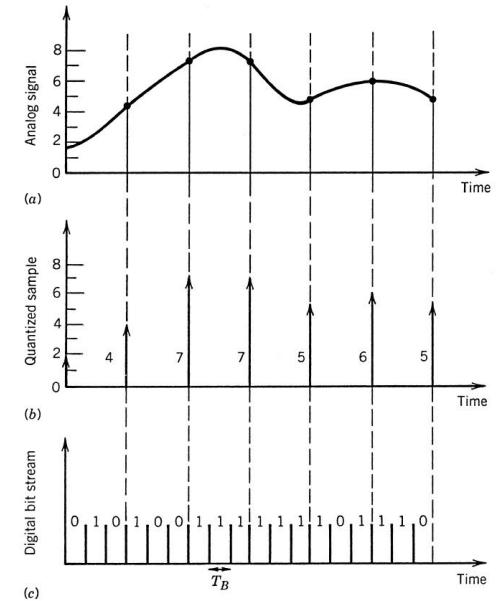
- ▶ viteza necesara (bit rate) [b/s]

$$B = m \cdot f_s \geq (2\Delta f) \cdot \log_2 M$$

$$M \geq \frac{A_{\max}}{A_N} \quad SNR [\text{dB}] = 10 \cdot \log_{10} \left(\frac{P_{\max}}{P_N} \right) = 20 \cdot \log_{10} \left(\frac{A_{\max}}{A_N} \right) \quad \log_2 10 \approx 3.33$$

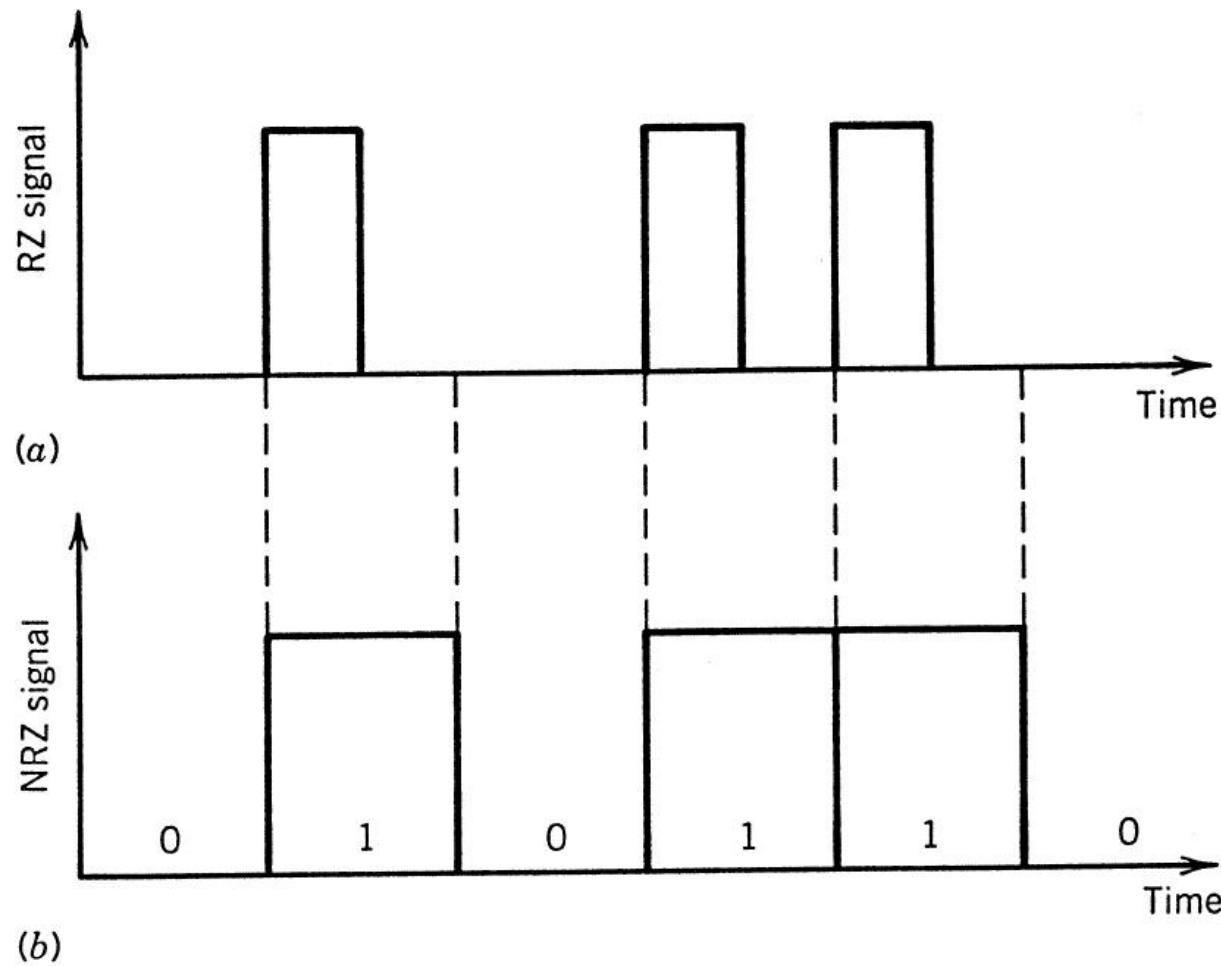
$$B > (\Delta f / 3) \cdot SNR$$

- ▶ telefonie: 3.1kHz @ SNR=30dB
 - ▶ B=31kb/s (64kb/s)
- ▶ televiziune: 4MHz @ SNR=50dB
 - ▶ B=66Mb/s (100Mb/s)

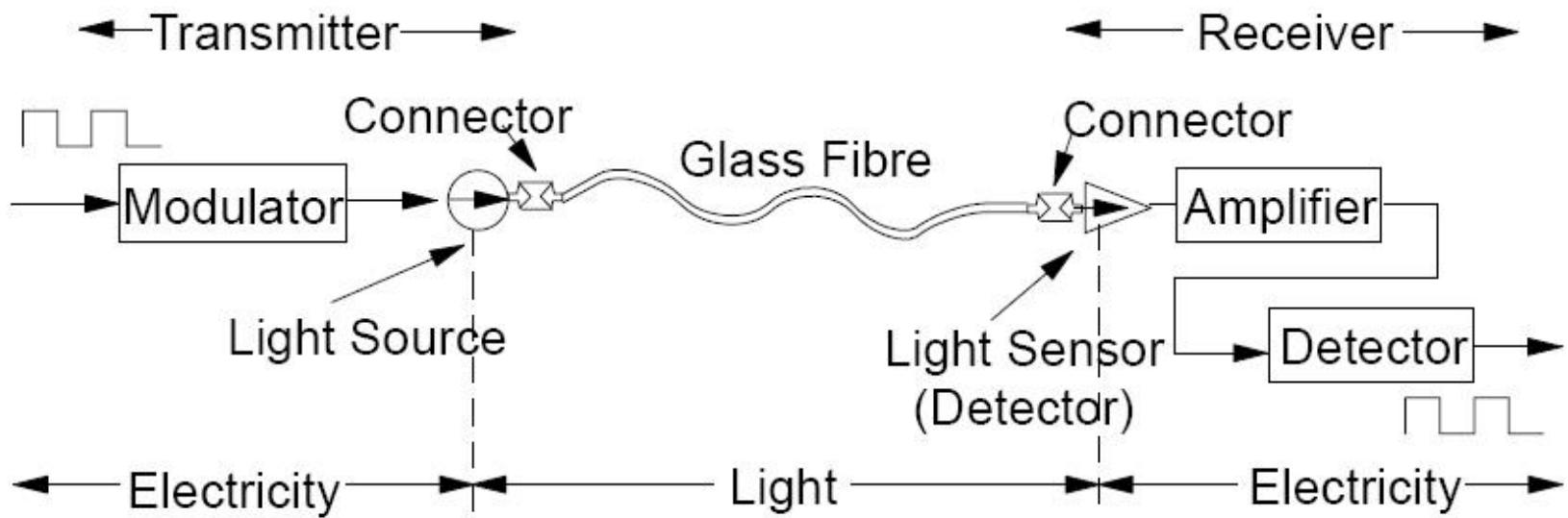


Modulare

- ▶ return-to-zero (RZ)
- ▶ nonreturn-to-zero (NRZ)

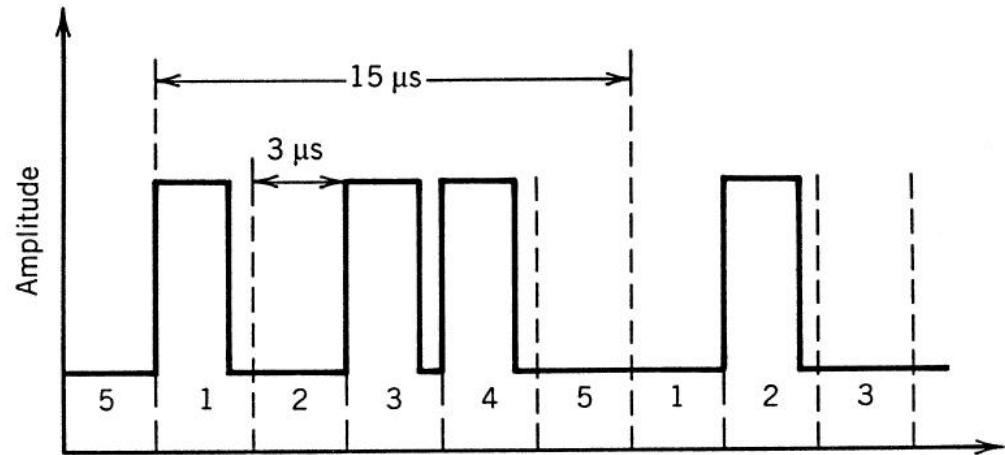


Transmision optica

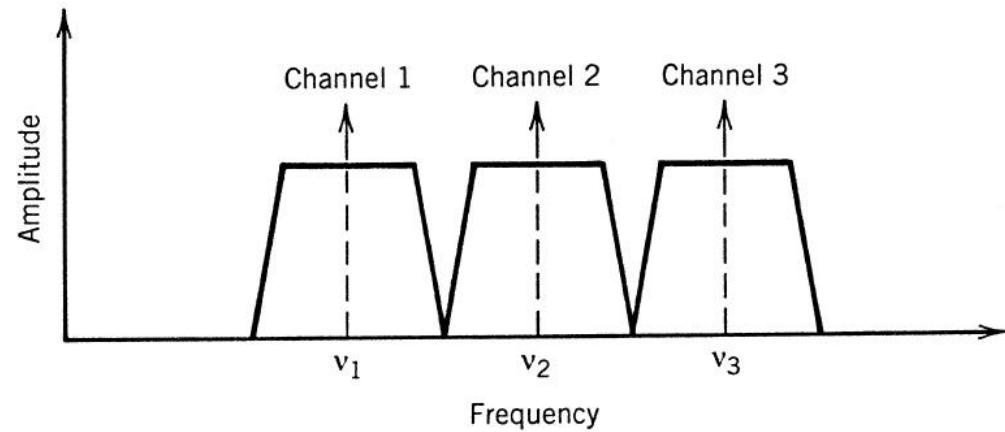


Multiplexare

- ▶ TDM
 - time-division multiplexing
- ▶ FDM
 - frequency-division multiplexing
- ▶ Realizabilă în domeniul **electric/optic**
- ▶ WDM
 - wavelength division multiplexing



(a)

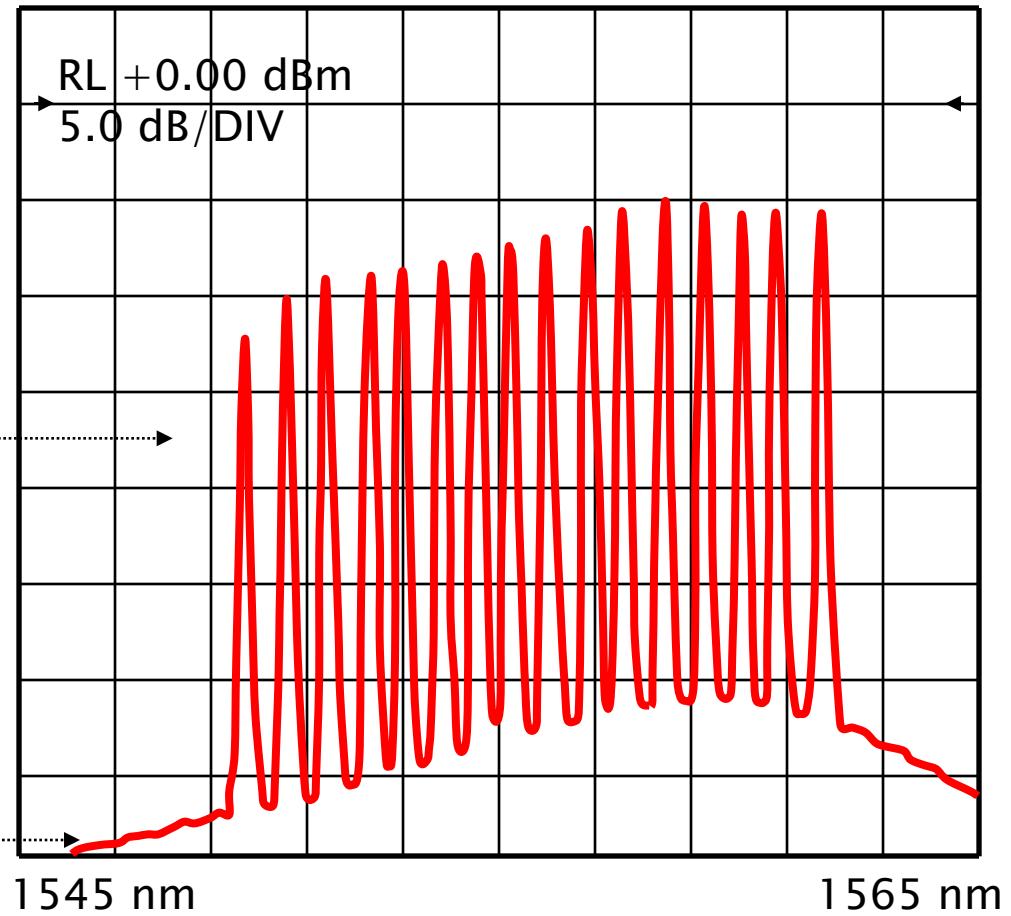


(b)

Spectral WDM – Wavelength Division Multiplexing

Canale: 16
Spatiere: 0.8 nm

Emisie spontană Amplificată (ASE)



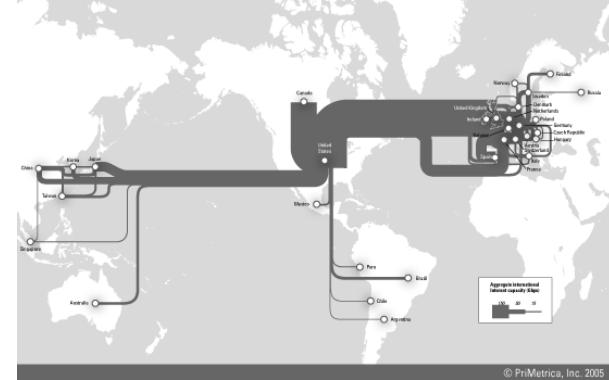
Standarde

▶ SUA, Japonia

SONET	SDH	B (Mb/s)	Channels
OC-1		51.84	672
OC-3	STM-1	155.52	2,016
OC-12	STM-4	622.08	8,064
OC-48	STM-16	2,488.32	32,256
OC-192	STM-64	9,953.28	129,024
OC-768	STM-256	39,813.12	516,096

- ▶ SONET – synchronous optical network
 - ▶ înlocuit de
- ▶ SDH – synchronous digital hierarchy

Standarde



► SUA

STS-1 and OC-1	51.840 Mb/s	
STS-3 and OC-3	155.52 Mb/s	same as STM-1
STS-9 and OC-9	466.56 Mb/s	
STS-12 and OC-12	622.08 Mb/s	same as STM-4
STS-18 and OC-18	933.12 Mb/s	
STS-24 and OC-24	1244.16 Mb/s	same as STM-8
STS-36 and OC-36	1866.24 Mb/s	
STS-48 and OC-48	2488.32 Mb/s	same as STM-16
STS-192 and OC-192	9953.28 Mb/s	same as STM-64
STS-256 and OC-256	13271.04 Mb/s	same as STM-86
STS-768 and OC-768	39813.12 Mb/s	same as STM-256
STS-3072 and OC-3072	159252.48 Mb/s	same as STM-1024
STS-12288 and OC-12288	639009.92 Mb/s	same as STM-4096

► Europa

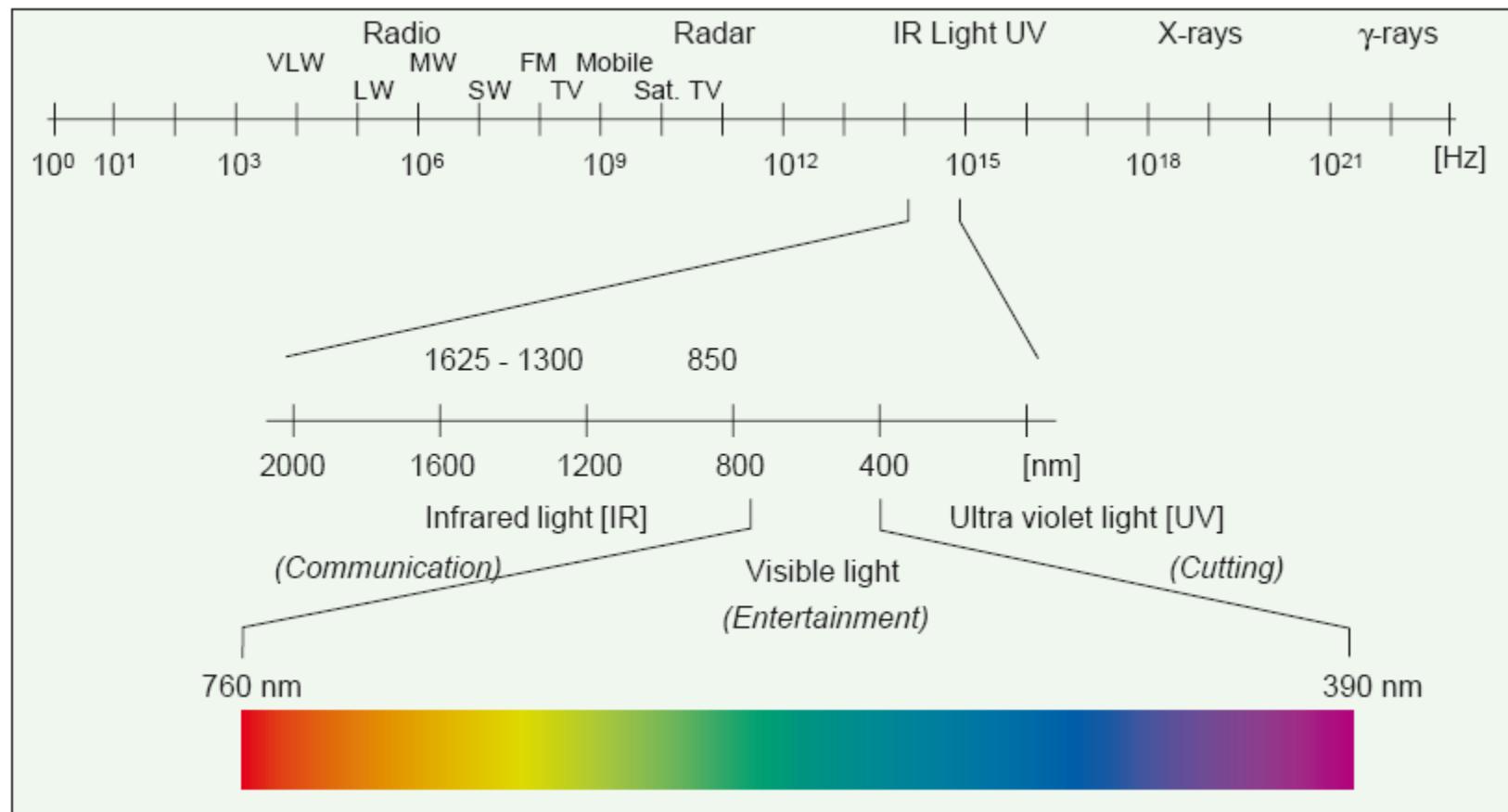
E0	64 Kb/s	
E1	2.048 Mb/s	
E2	8.448 Mb/s	4 E1s
E3	34.364 Mb/s	16 E1s
E4	139.264 Mb/s	64 E1s

1 mile=1760 yards

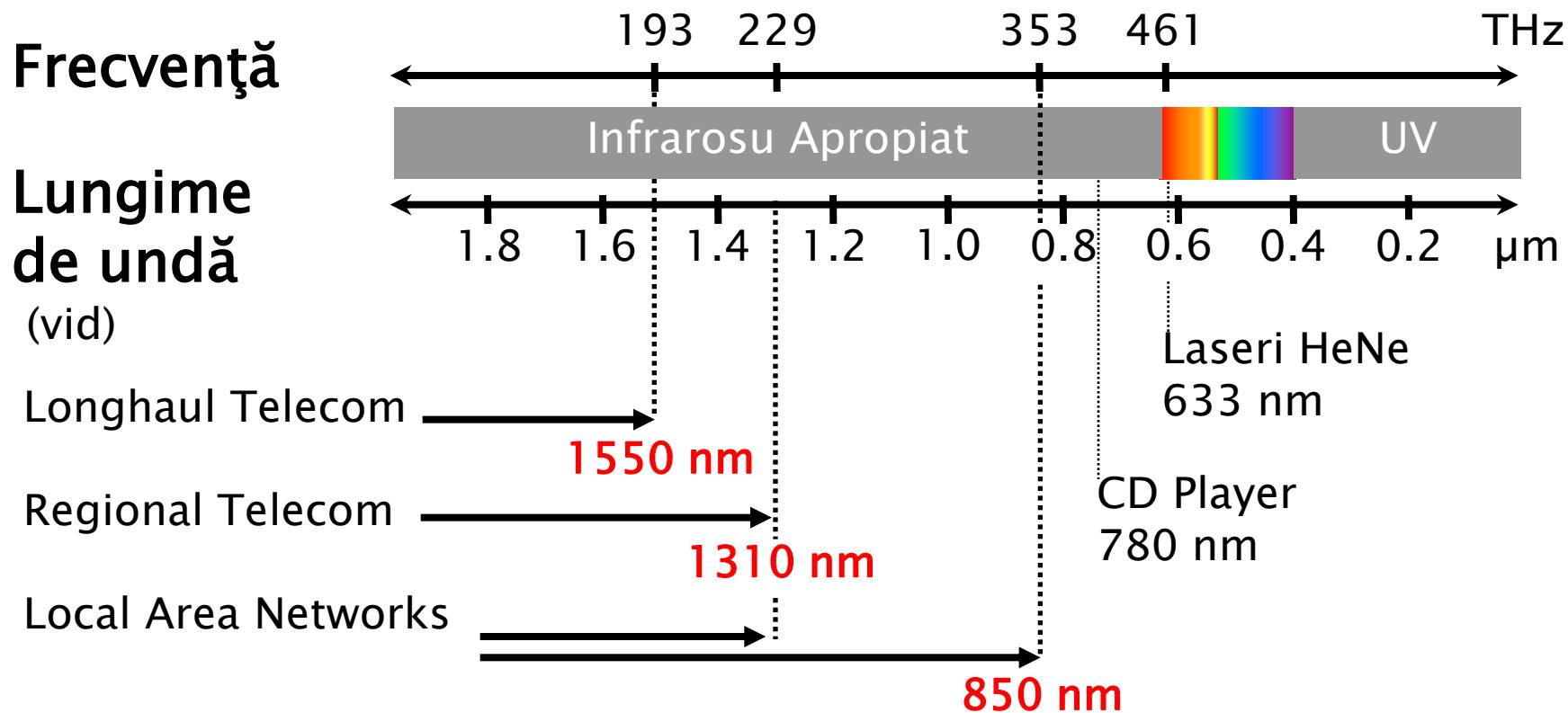
1 yards=3 feet

1 mile≈1609.34 m

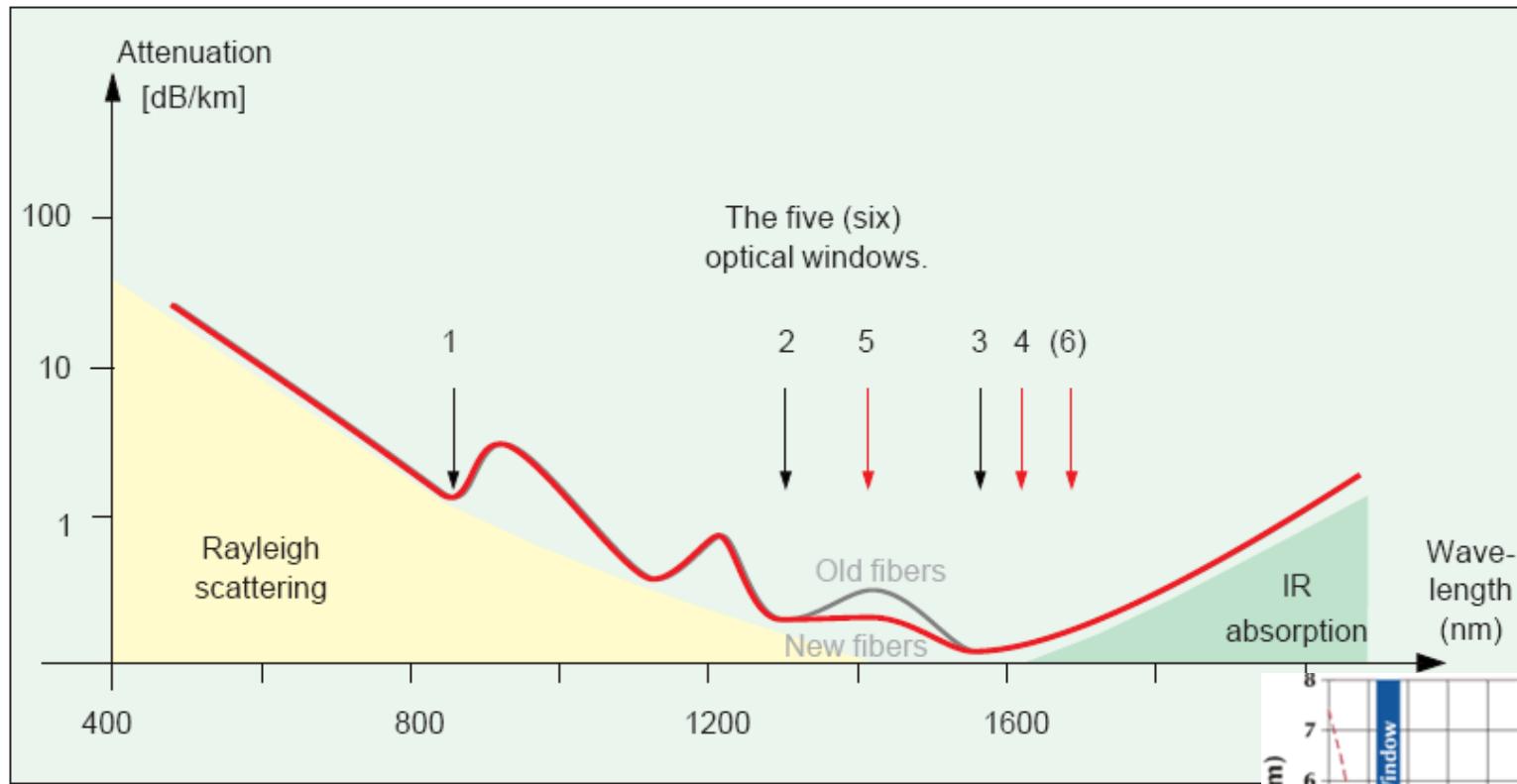
Spectrul electromagnetic



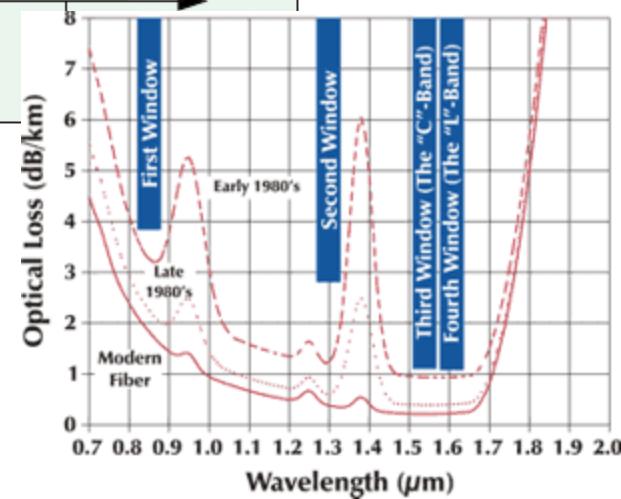
Benzi de lucru în comunicațiile optice



Atenuarea în fibra optică (SiO_2)



850nm, 1310nm, 1550nm



Aplicatii majore

- ▶ Comunicatii
 - Infrarosu (InGaAsP)
- ▶ Vizibil
 - Spectru vizibil (GaAlAs)
- ▶ Illuminare
 - Putere ridicata, lumina alba (GaN)

Eficientă

- ▶ Bec cu incandescentă
 - 16 lm/W
- ▶ Tub fluorescent
 - 100 lm/W
- ▶ LED
 - curent: 250 lm/W
 - curand: 300 lm/W

Premiul Nobel, Fizica, 2014

Physics



The Nobel Prize in Physics 2014

Summary



The Nobel Prize in Physics 2014

Isamu Akasaki
Hiroshi Amano
Shuji Nakamura

Share this



© Nobel Media AB. Photo: A.
Mahmoud

Isamu Akasaki

Prize share: 1/3

© Nobel Media AB. Photo: A.
Mahmoud

Hiroshi Amano

Prize share: 1/3

© Nobel Media AB. Photo: A.
Mahmoud

Shuji Nakamura

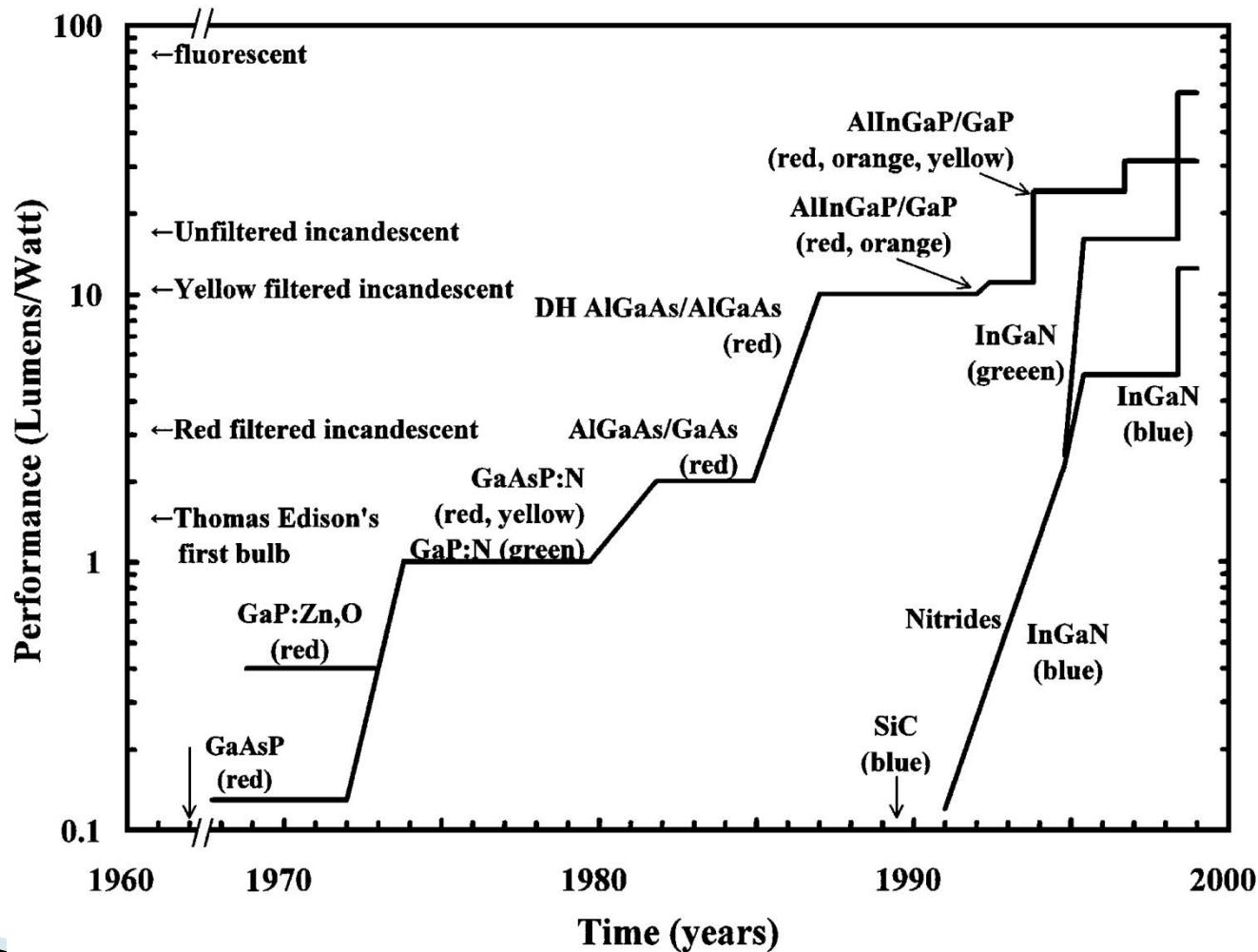
Prize share: 1/3

The Nobel Prize in Physics 2014 was awarded jointly to Isamu Akasaki, Hiroshi Amano and Shuji Nakamura "for the invention of efficient blue light-emitting diodes which has enabled bright and energy-saving white light sources."

To cite this section

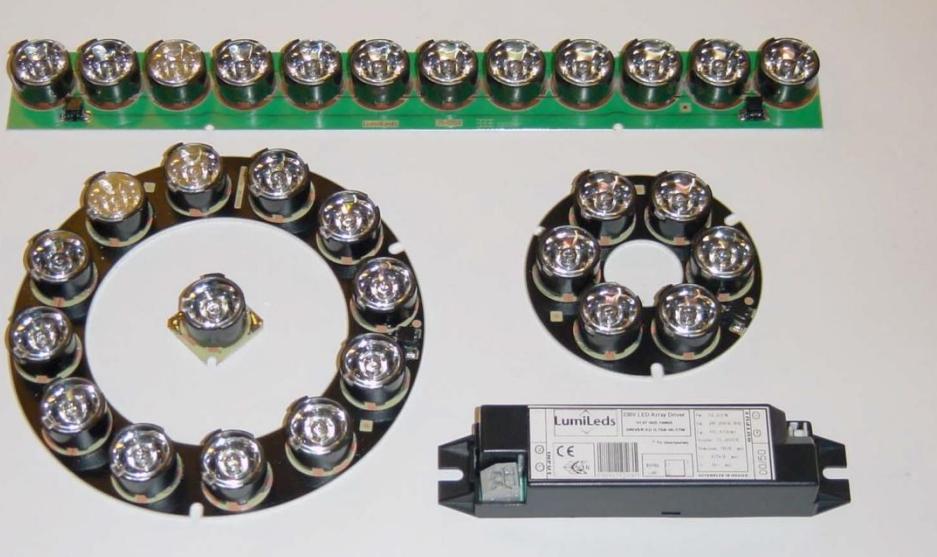
MLA style: The Nobel Prize in Physics 2014. NobelPrize.org. Nobel Media AB 2021. Tue, 2 Mar 2021.

Eficienta în timp



Aplicatii

▶ auto



Aplicatii

► casnic

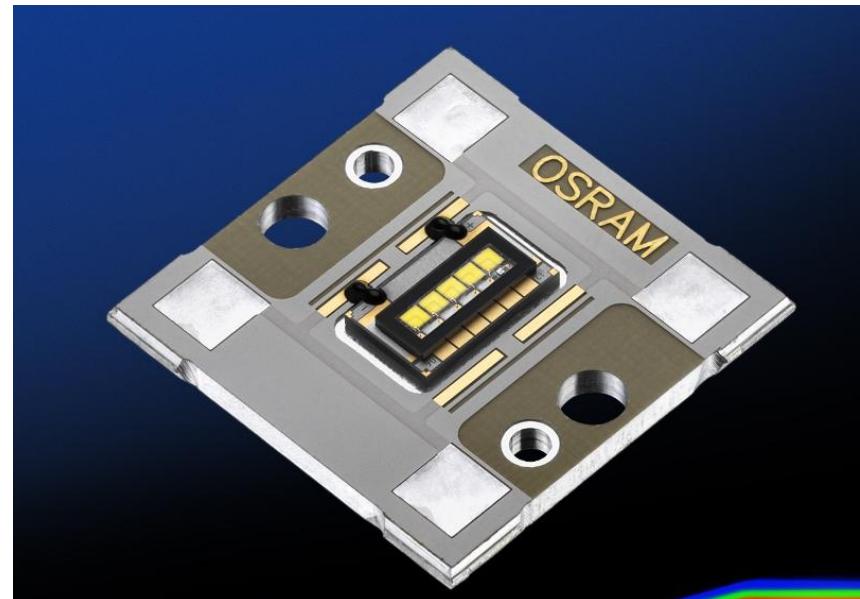


Aplicatii

- ▶ iluminat public



Aplicatii



Aplicatii majore

- ▶ Comunicatii
 - Infrarosu (InGaAsP)
- ▶ Vizibil
 - Spectru vizibil (GaAlAs)
- ▶ Iluminare
 - Putere ridicata, lumina alba (GaN)

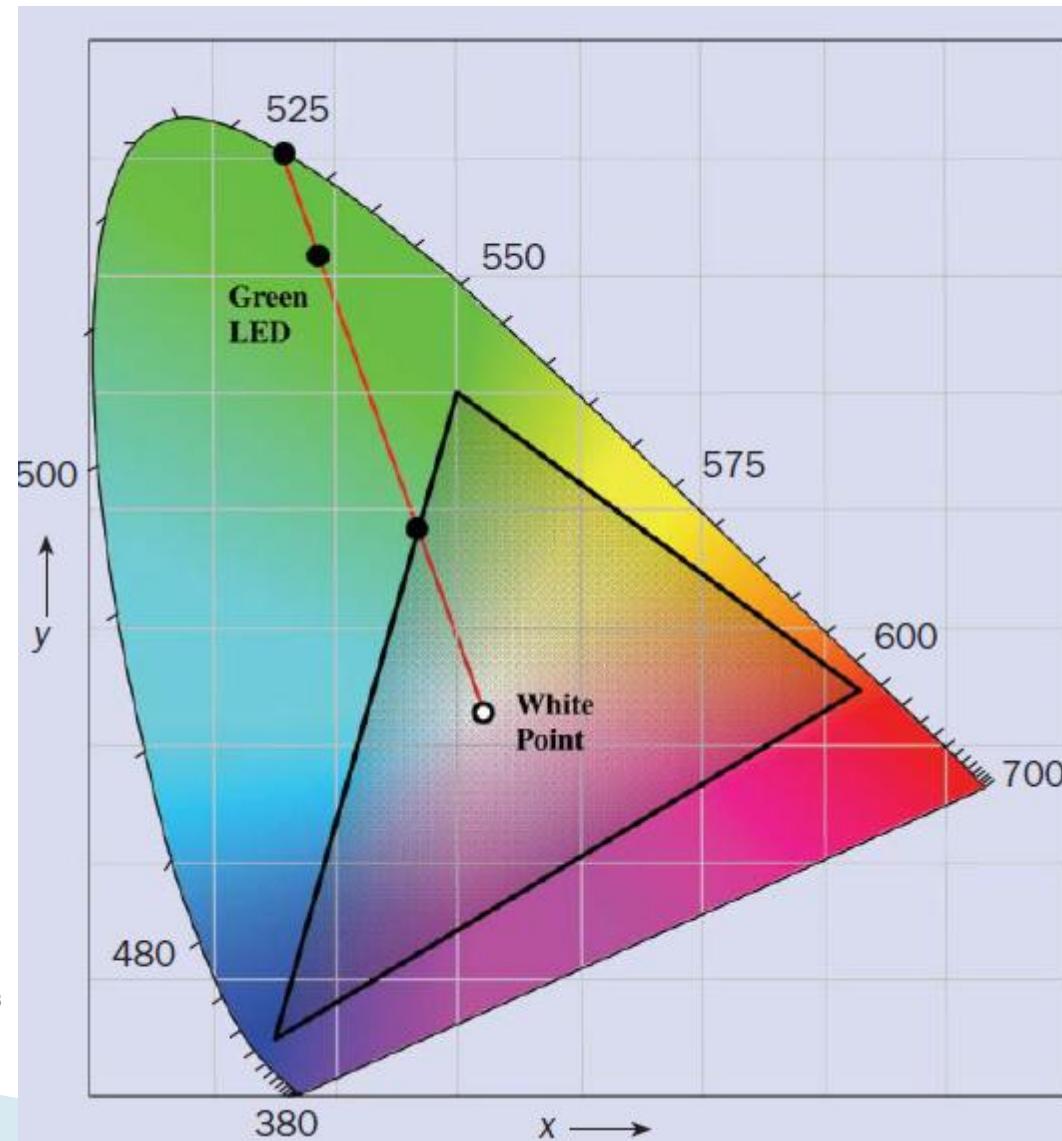
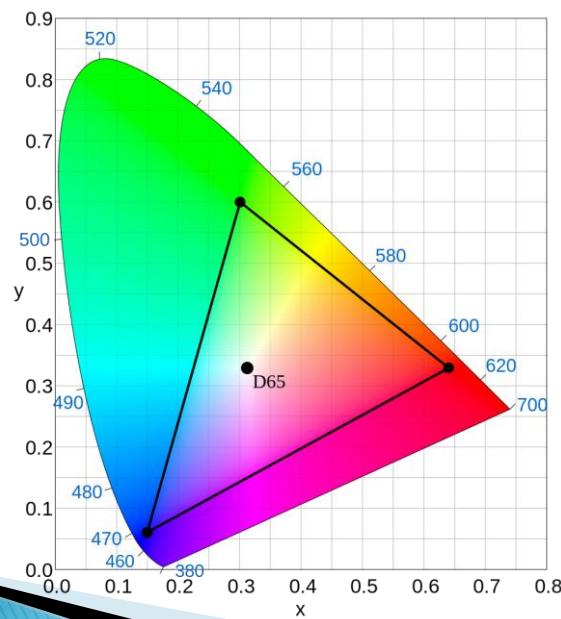
ITU-R BT.709



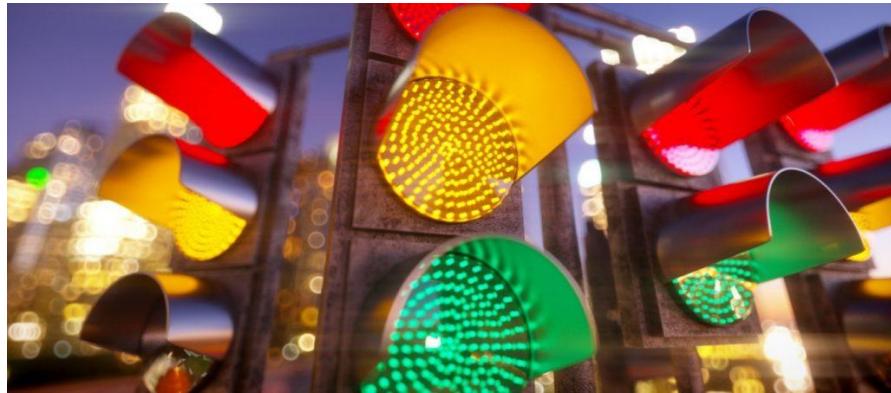
ITU-R BT.709 phosphor properties

Phosphor	x	y
Red	0.640	0.330
Green	0.300	0.600
Blue	0.150	0.060

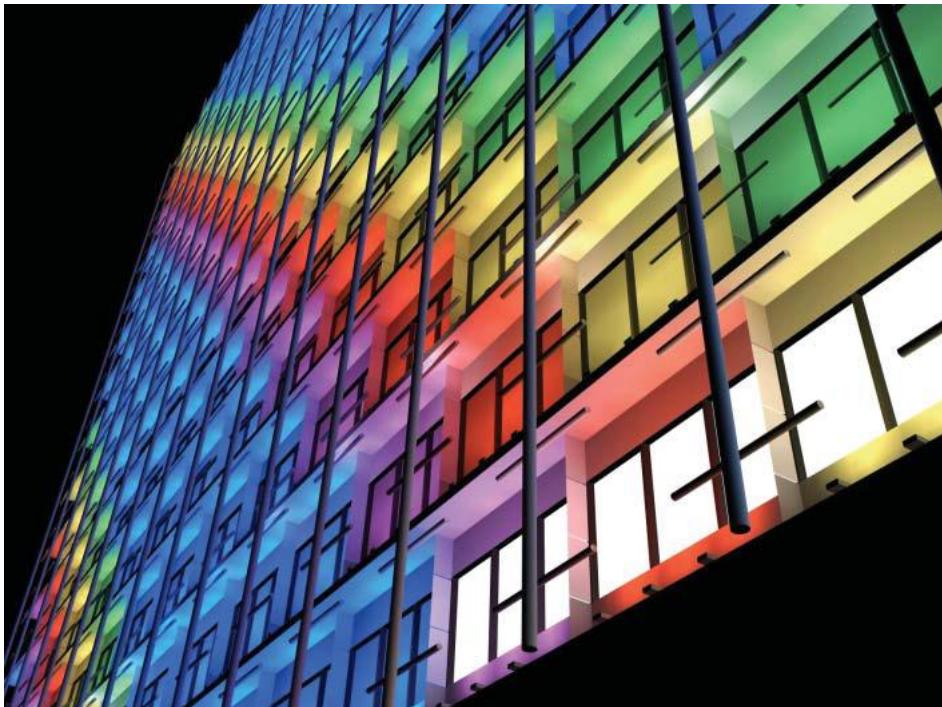
Data refers to xy chromaticity co-ordinates of ITU-R BT.709 phosphors which are used in most CRT displays [1].



Spectru vizibil



ITU-R BT.709



RGB values for Luxeon LEDs

LED color	Dominant wavelength λ_D (nm)	RGB values
Royal blue	455	0.05, 0.00, 0.95
Blue	470	0.00, 0.11, 0.89
Cyan	505	0.00, 0.63, 0.37
Green	530	0.00, 0.77, 0.23
Amber	590	0.70, 0.30, 0.00
Red-orange	615	0.97, 0.00, 0.03
Red	625	0.92, 0.00, 0.08

Reprezentare logarithmică

$$\text{dB} = 10 \cdot \log_{10} (P_2 / P_1)$$

$$\text{dBm} = 10 \cdot \log_{10} (P / 1 \text{ mW})$$

$$0 \text{ dB} = 1$$

$$+ 0.1 \text{ dB} = 1.023 (+2.3\%)$$

$$+ 3 \text{ dB} = 2$$

$$+ 5 \text{ dB} = 3$$

$$+ 10 \text{ dB} = 10$$

$$-3 \text{ dB} = 0.5$$

$$-10 \text{ dB} = 0.1$$

$$-20 \text{ dB} = 0.01$$

$$-30 \text{ dB} = 0.001$$

$$0 \text{ dBm} = 1 \text{ mW}$$

$$3 \text{ dBm} = 2 \text{ mW}$$

$$5 \text{ dBm} = 3 \text{ mW}$$

$$10 \text{ dBm} = 10 \text{ mW}$$

$$20 \text{ dBm} = 100 \text{ mW}$$

$$-3 \text{ dBm} = 0.5 \text{ mW}$$

$$-10 \text{ dBm} = 100 \mu\text{W}$$

$$-30 \text{ dBm} = 1 \mu\text{W}$$

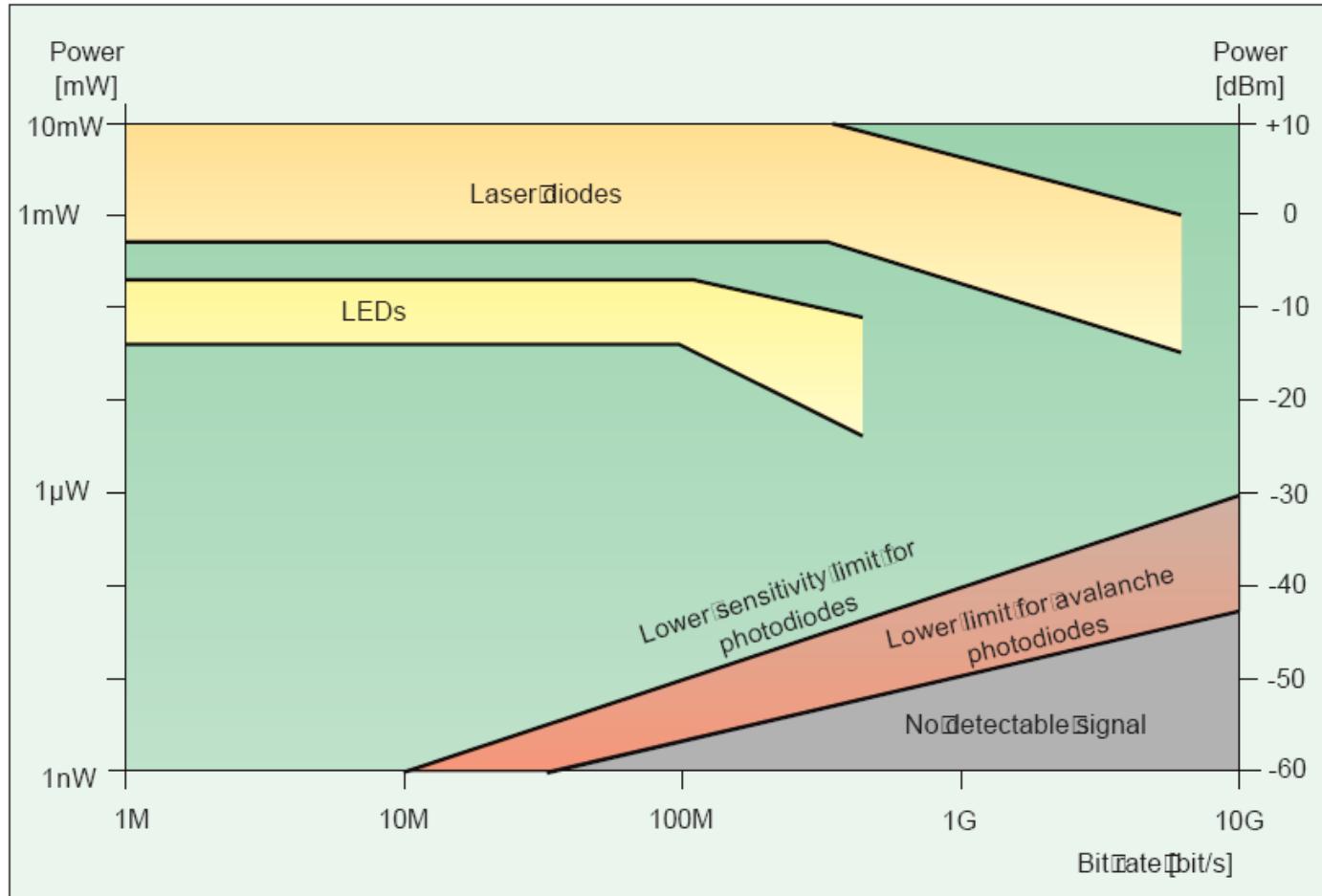
$$-60 \text{ dBm} = 1 \text{ nW}$$

$$[\text{dBm}] + [\text{dB}] = [\text{dBm}]$$

$$[\text{dBm}/\text{Hz}] + [\text{dB}] = [\text{dBm}/\text{Hz}]$$

$$[x] + [\text{dB}] = [x]$$

Limite putere/bandă a dispozitivelor optoelectronice

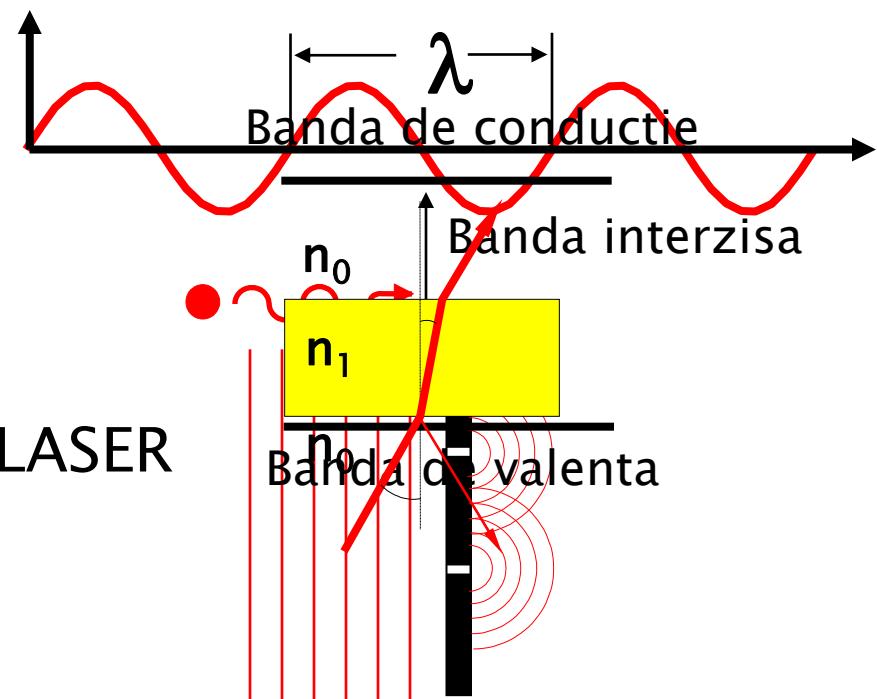


Modelarea luminii

(tot) Capitolul 1

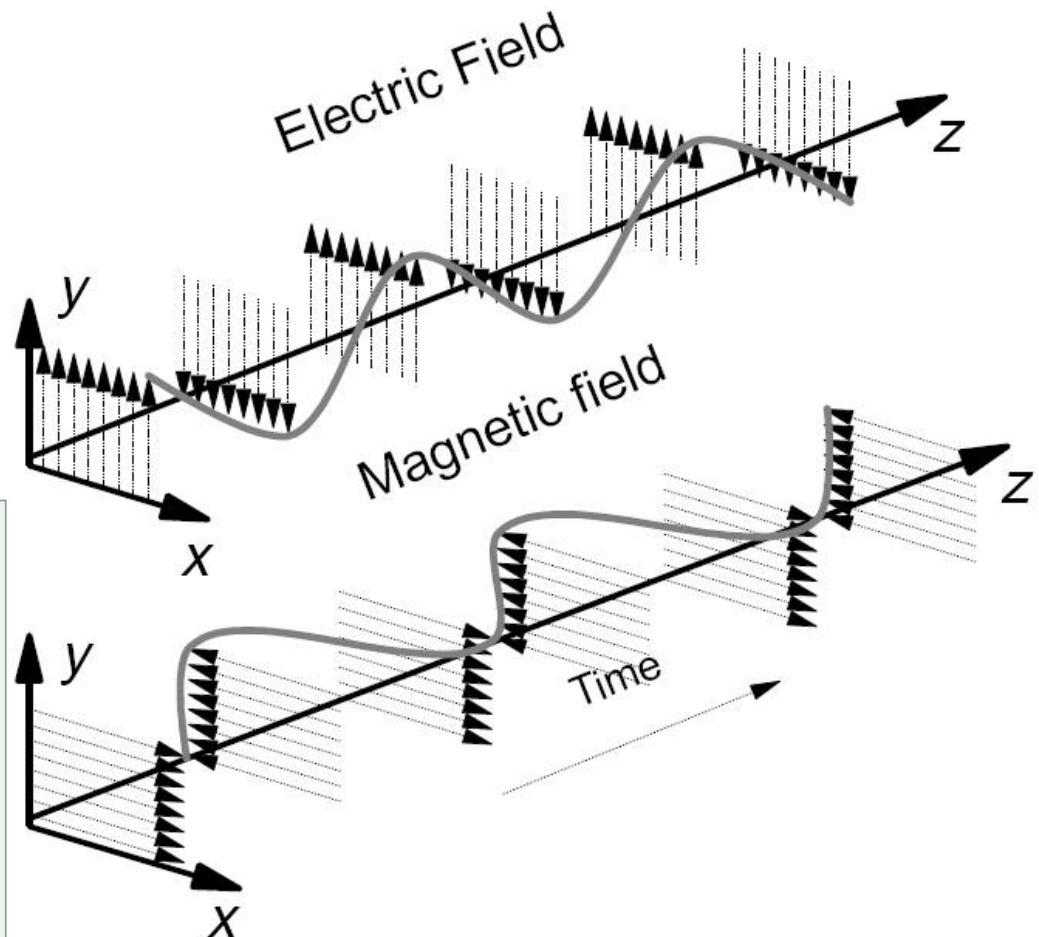
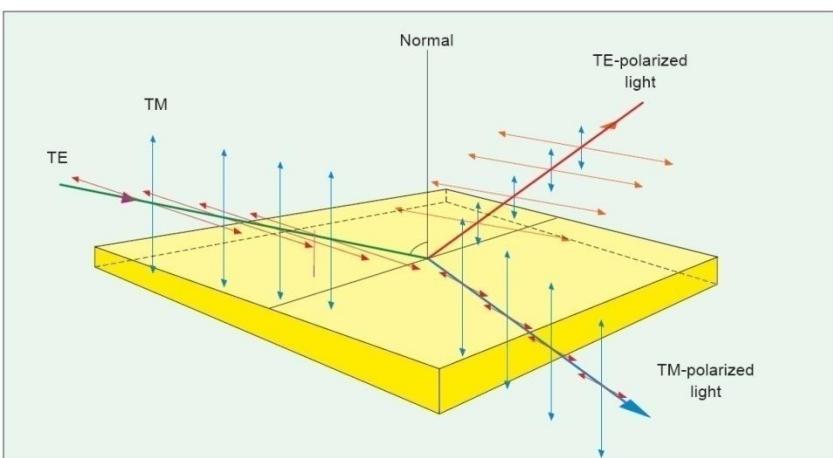
Modelarea luminii

- ▶ Undă electromagnetică
 - Ecuatiile lui Maxwell
 - λ , ϵ , ω , f
- ▶ Teoria cuantică
 - Benzi energetice $E = h \nu$
 - fotoni, emisie stimulată, LASER
- ▶ Optică geometrică
 - n , θ
 - raze de lumină
 - intuitivă

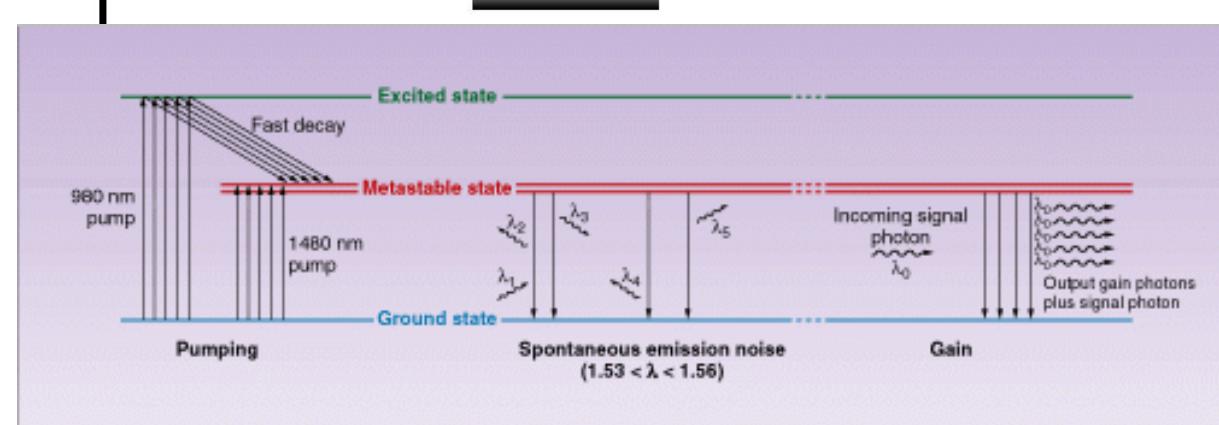
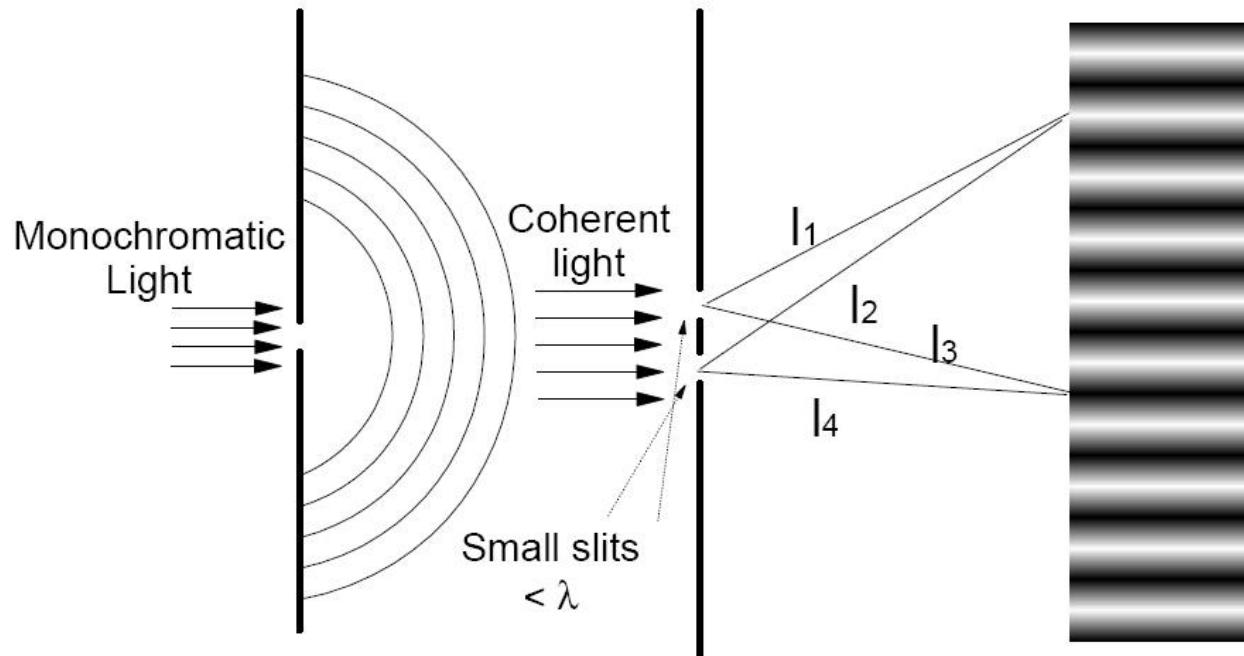


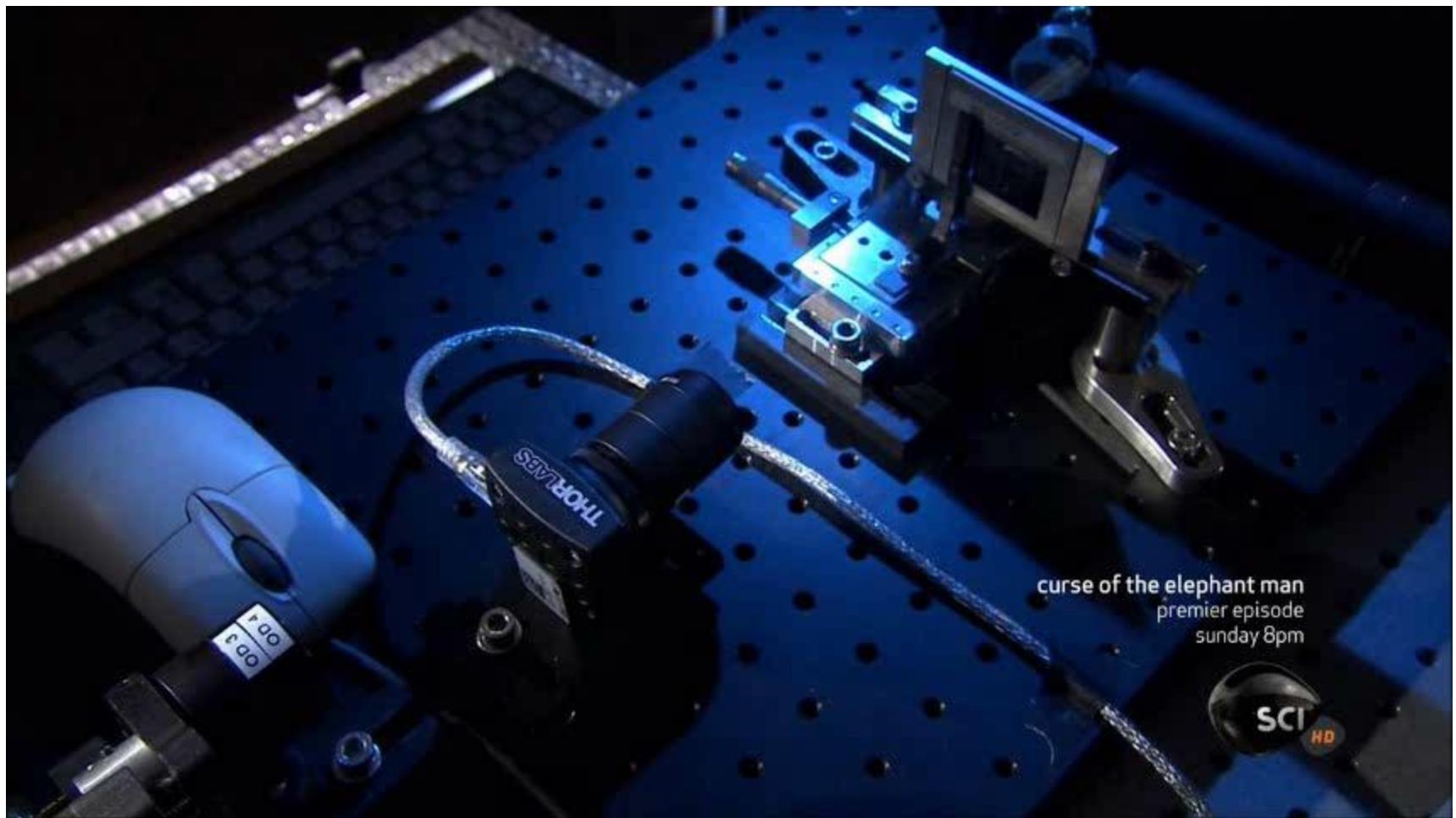
Unda electromagnetică

- ▶ Dispersie
- ▶ Fibre monomod
- ▶ Interferenta
- ▶ Polarizare



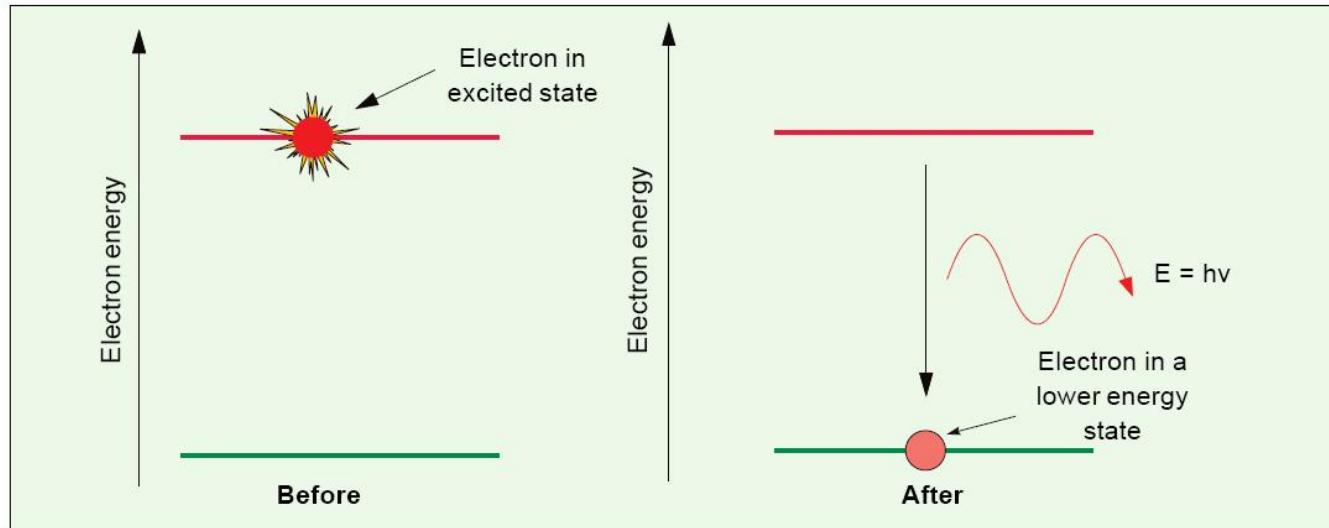
Fotoni/Unda





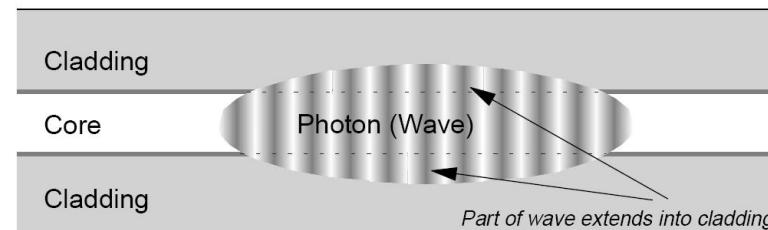
Through the Wormhole
S02E07 How Does the Universe Work

Model cuantic - foton



$$E_g = h\nu; \quad \lambda = \frac{hc}{E_g}; \quad \lambda[\mu\text{m}] = \frac{1.240}{E_g[\text{eV}]}$$

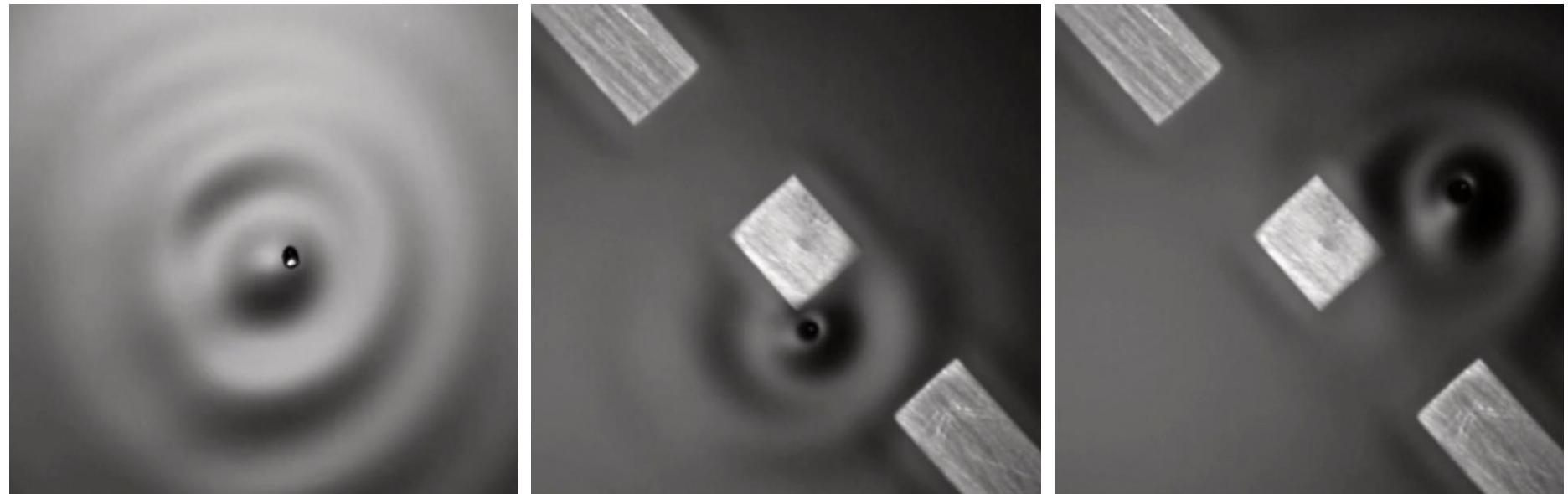
- ▶ **h constanta lui Planck**
 $6.62 \cdot 10^{-32} \text{ Ws}^2$
- ▶ **c viteza luminii in vid**
 $2.998 \cdot 10^8 \text{ m/s}$



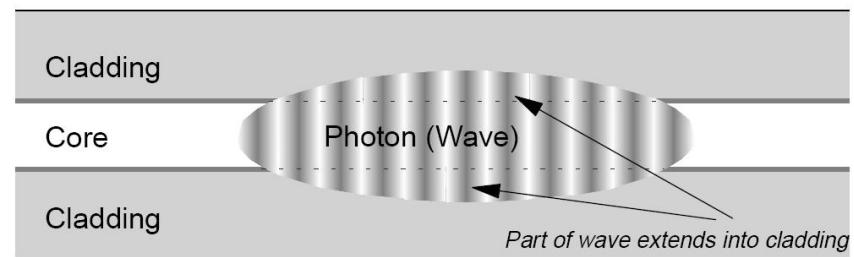


Through the Wormhole S02E07 How Does the Universe Work

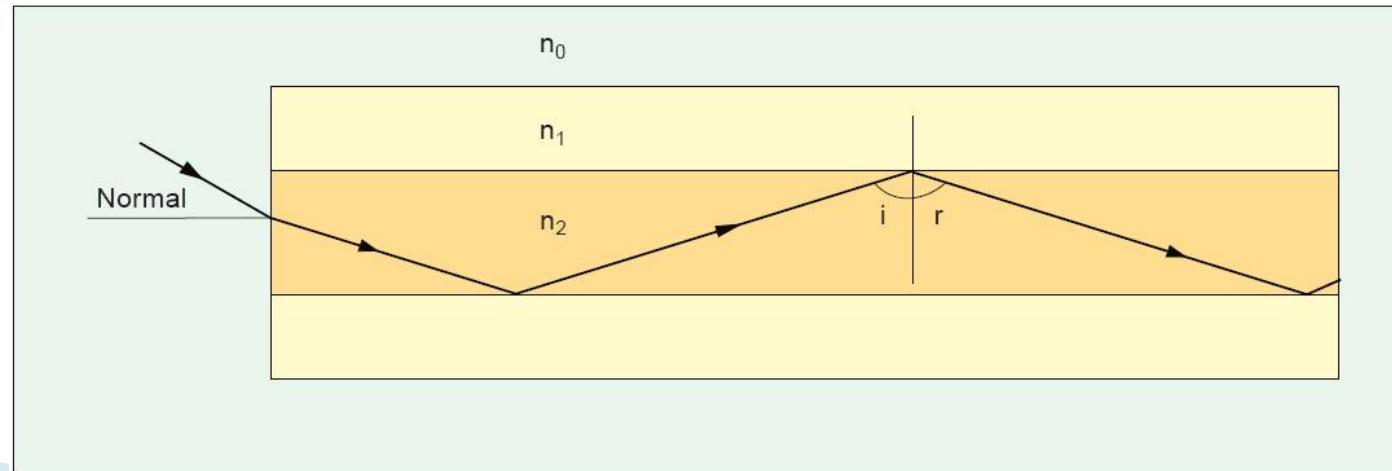
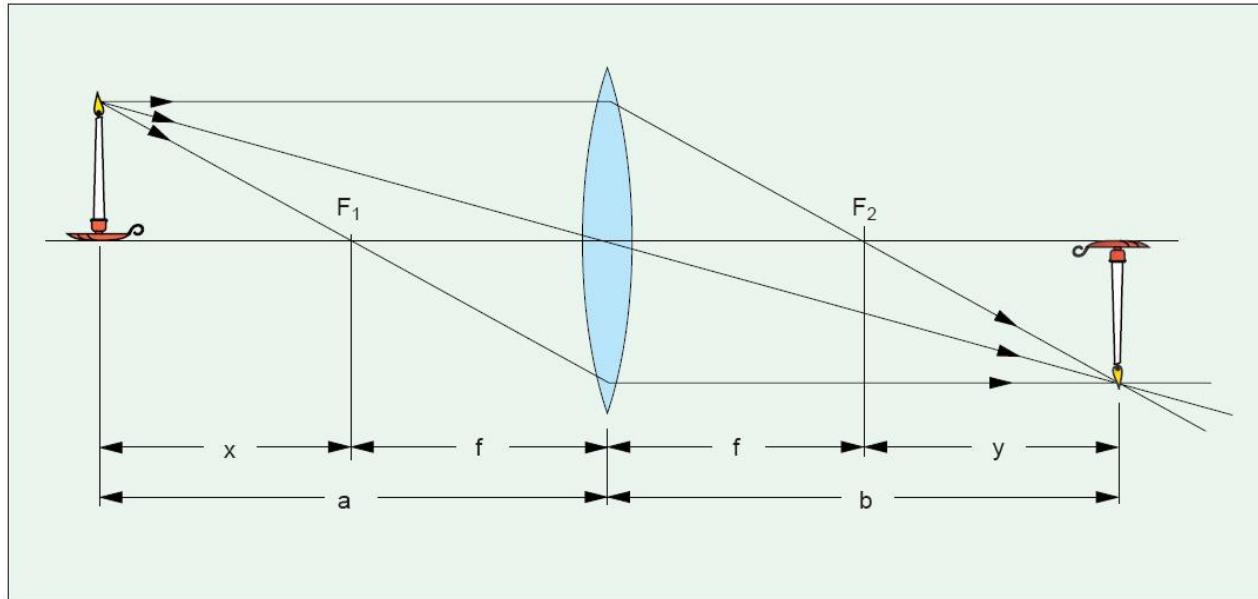
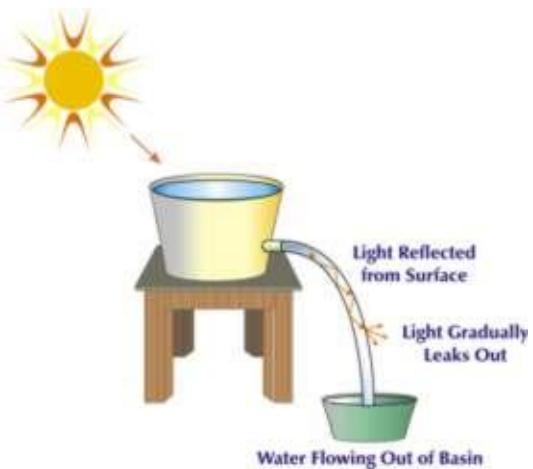
Modelare



Through the Wormhole
S02E07 How Does the Universe Work



Optica geometrica



Lumina ca undă electromagnetică

Capitolul 2

Cuprins

- ▶ **Lumina ca undă electromagnetică** (ecuațiile lui Maxwell, ecuația undelor, parametrii de propagare)
- ▶ **Elemente de fotometrie și radiometrie** (mărimi energetice/luminoase)
- ▶ **Fibra optică** (realizare, principiu de funcționare, atenuare, dispersie, banda de frecvență)
- ▶ **Cabluri optice** (tehnologie, conectori, lipire – splice)
- ▶ **Proiectare sistemică a legăturii pe fibra optică** (bandă de frecvență, balanță puterilor)
- ▶ **Emițătoare optice** (LED și dioda laser – realizare fizică și funcționare)
- ▶ **Receptoare optice** (dioda PIN, dioda cu avalanșă – realizare fizică și funcționare)
- ▶ **Amplificatoare transimpedanță** (parametri, scheme tipice, TIA în buclă deschisă, cu reacție, diferențiale, control automat al câștigului)
- ▶ **Realizarea circuitelor pentru controlul emițătoarelor optice** (parametri, scheme tipice, controlul puterii, multiplexoare)
- ▶ **Dispozitive de captare a energiei solare** (principiu de funcționare, utilizare, proiectare)

Ecuatiile lui Maxwell

$$\nabla \times E = -\frac{\partial B}{\partial t}$$

$$\nabla \times H = \frac{\partial D}{\partial t} + J$$

$$\nabla \cdot D = \rho$$

$$\nabla \cdot B = 0$$

$$\nabla \cdot J = -\frac{\partial \rho}{\partial t}$$

► Ecuatii constitutive

$$D = \epsilon \cdot E$$

$$B = \mu \cdot H$$

$$J = \sigma \cdot E$$

► In vid

$$\mu_0 = 4\pi \times 10^{-7} \text{ H/m}$$

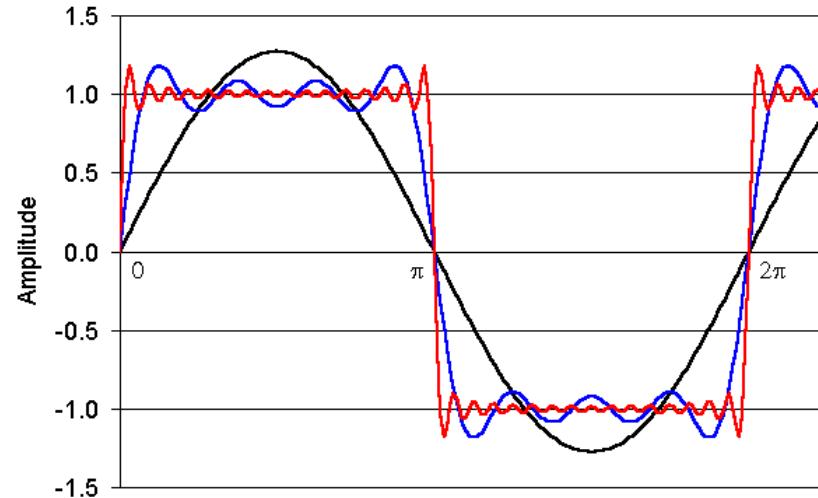
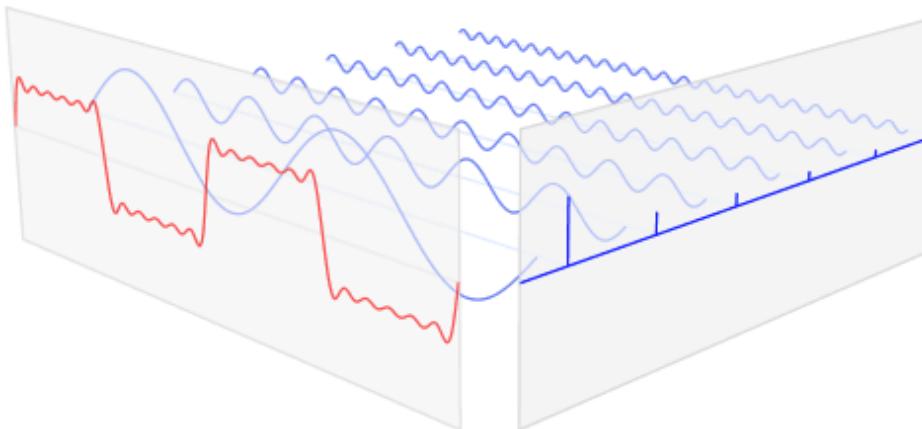
$$\epsilon_0 = 8,854 \times 10^{-12} \text{ F/m}$$

$$c_0 = \frac{1}{\sqrt{\epsilon_0 \cdot \mu_0}} = 2,99790 \cdot 10^8 \text{ m/s}$$

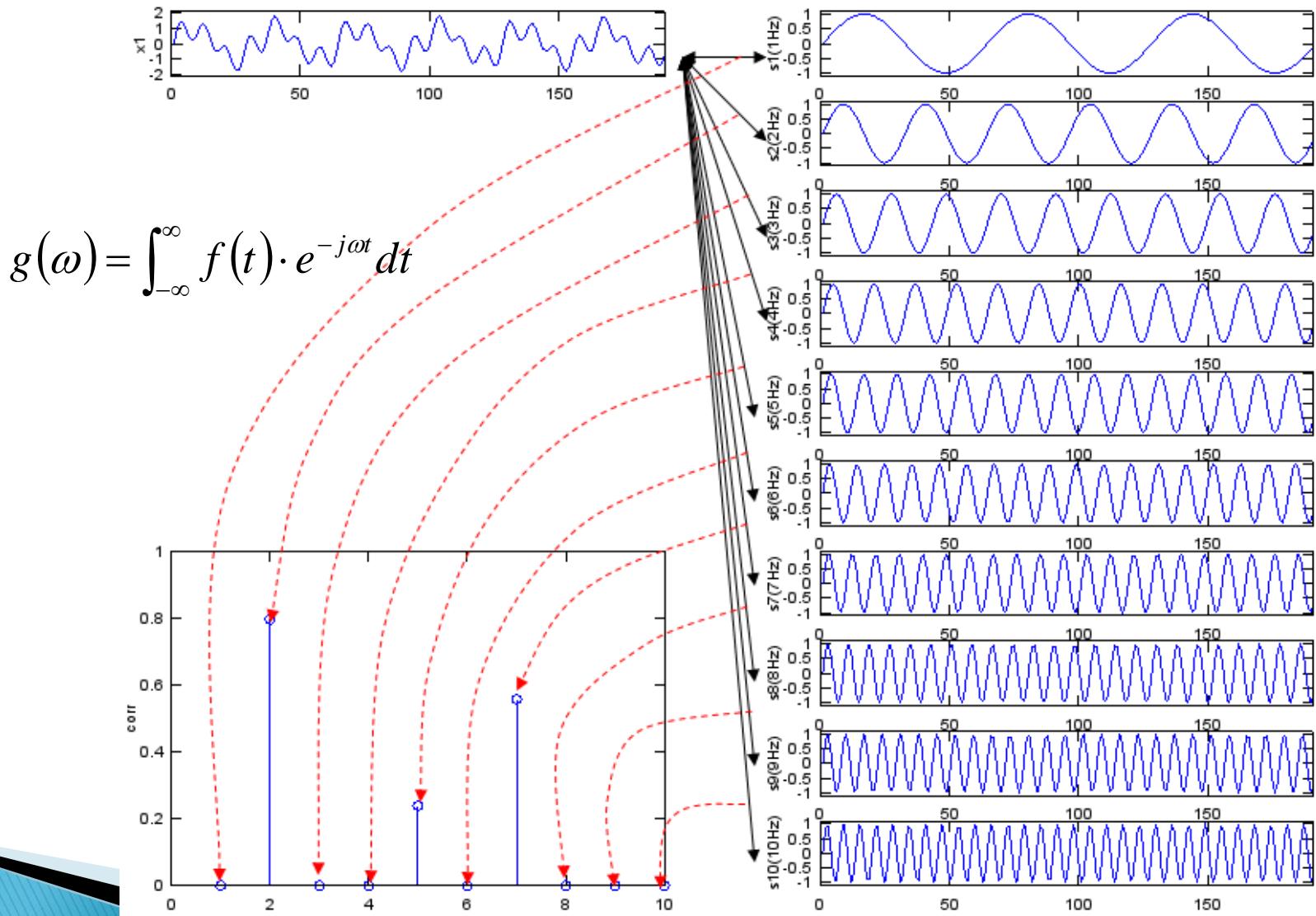
Modele matematice

- ▶ cazuri particulare în care există rezolvare analitică
 - semnale cu variație armonică în timp, transformata Fourier, spectru

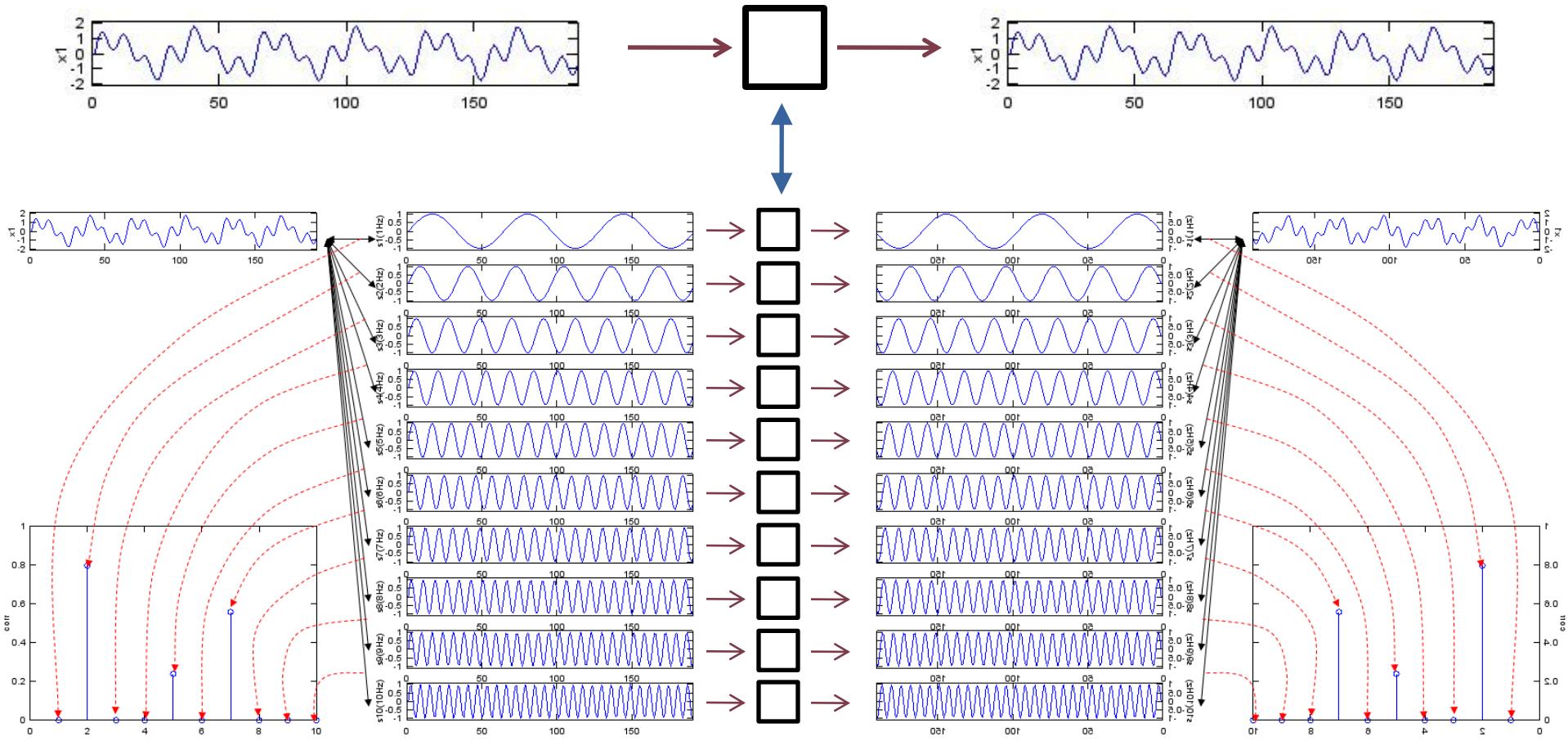
$$X = X_0 e^{j \cdot \omega \cdot t} \quad \frac{\partial X}{\partial t} = j \cdot \omega \cdot X \quad g(\omega) = \int_{-\infty}^{\infty} f(t) \cdot e^{-j\omega t} dt \quad f(t) = \int_{-\infty}^{\infty} g(\omega) \cdot e^{j\omega t} d\omega$$



Modele matematice



Modele matematice



$$F(\omega) = \int_{-\infty}^{\infty} f(t) \cdot e^{-j\omega t} dt$$

$$G(\omega)[F(\omega)]$$

$$g(t) = \int_{-\infty}^{\infty} G(\omega) \cdot e^{j\omega t} d\omega$$

Câmpuri electromagnetic cu variație armonică în timp

$$X = X_0 e^{j \cdot \omega t} \quad \frac{\partial X}{\partial t} = j \cdot \omega \cdot X$$

► Simplificarea ecuațiilor lui Maxwell

$$\nabla^2 E + \omega^2 \epsilon \mu E = j \omega \mu J + \frac{1}{\epsilon} \nabla \rho$$
$$\nabla^2 H + \omega^2 \epsilon \mu H = -\nabla \times J$$

$$\nabla \cdot E = \frac{\rho}{\epsilon}$$

$$\nabla \cdot H = 0$$

► Ecuatiile Helmholtz sau ecuațiile de propagare
Mediu lipsit de sarcini electrice

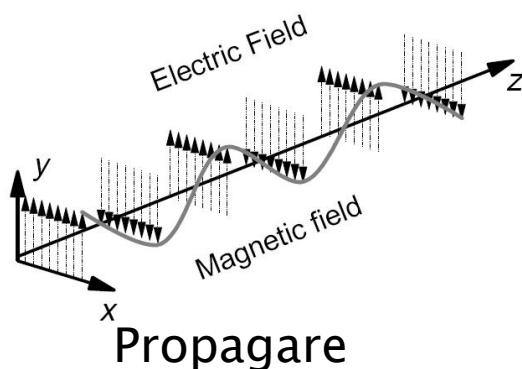
$$\nabla^2 E - \gamma^2 E = 0$$

$$\nabla^2 H - \gamma^2 H = 0$$

$$\gamma^2 = -\omega^2 \epsilon \mu + j \omega \mu \sigma$$

γ – Constanta de propagare

Solutia ecuatiilor de propagare



Camp electric dupa directia Oy, **← prin alegerea judicioasa**
propagare dupa directia Oz **← a sistemului de referinta**

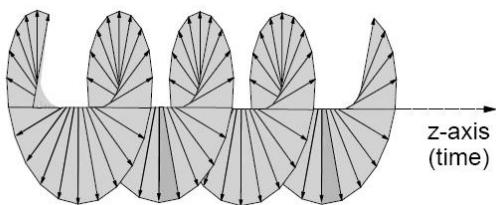
$$E_y = E_+ e^{-\gamma \cdot z} + E_- e^{\gamma \cdot z}$$

$$\gamma = \sqrt{-\omega^2 \epsilon \mu + j \omega \mu \sigma} = \alpha + j \cdot \beta$$

Exista numai unda progresiva $E_+ \Rightarrow A$

$$E_y = A e^{-(\alpha + j \cdot \beta) \cdot z}$$

Camp armonic



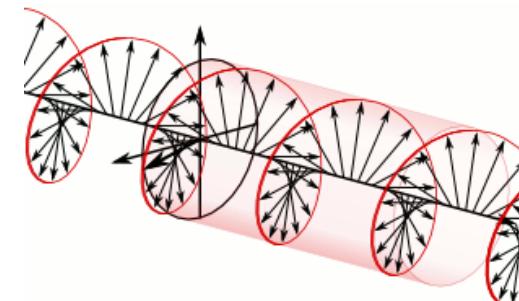
Polarizare circulara

$E_y = A \cdot e^{-\alpha \cdot z} \cdot e^{j(\omega t - \beta \cdot z)}$

Amplitudine

Atenuare

Propagare
(variatie in timp si spatiu)

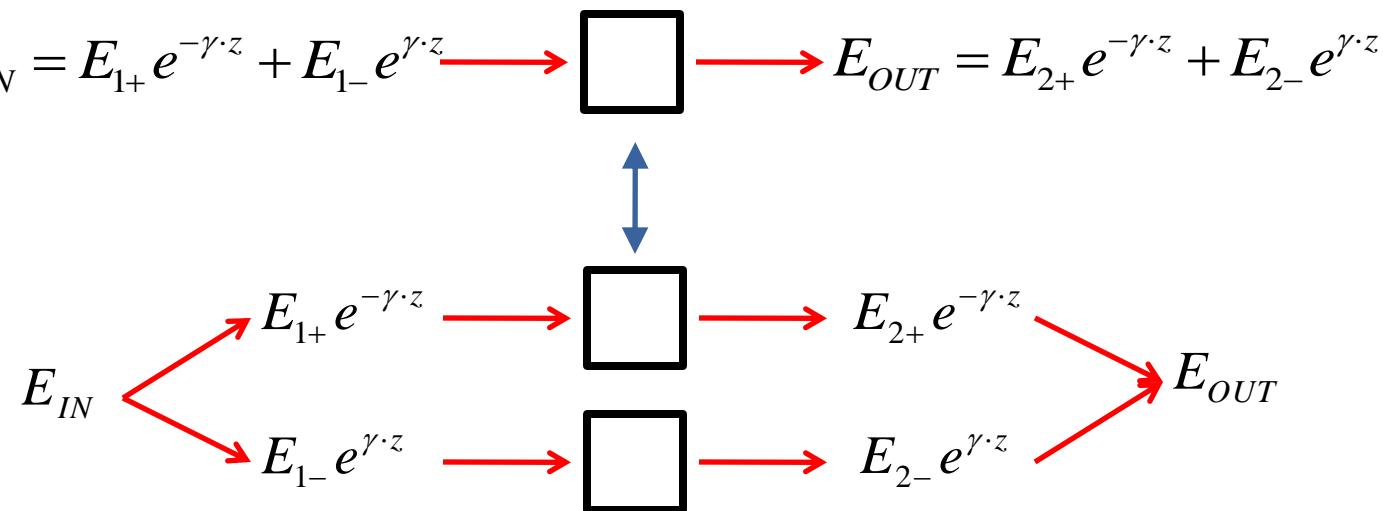


Modele matematice

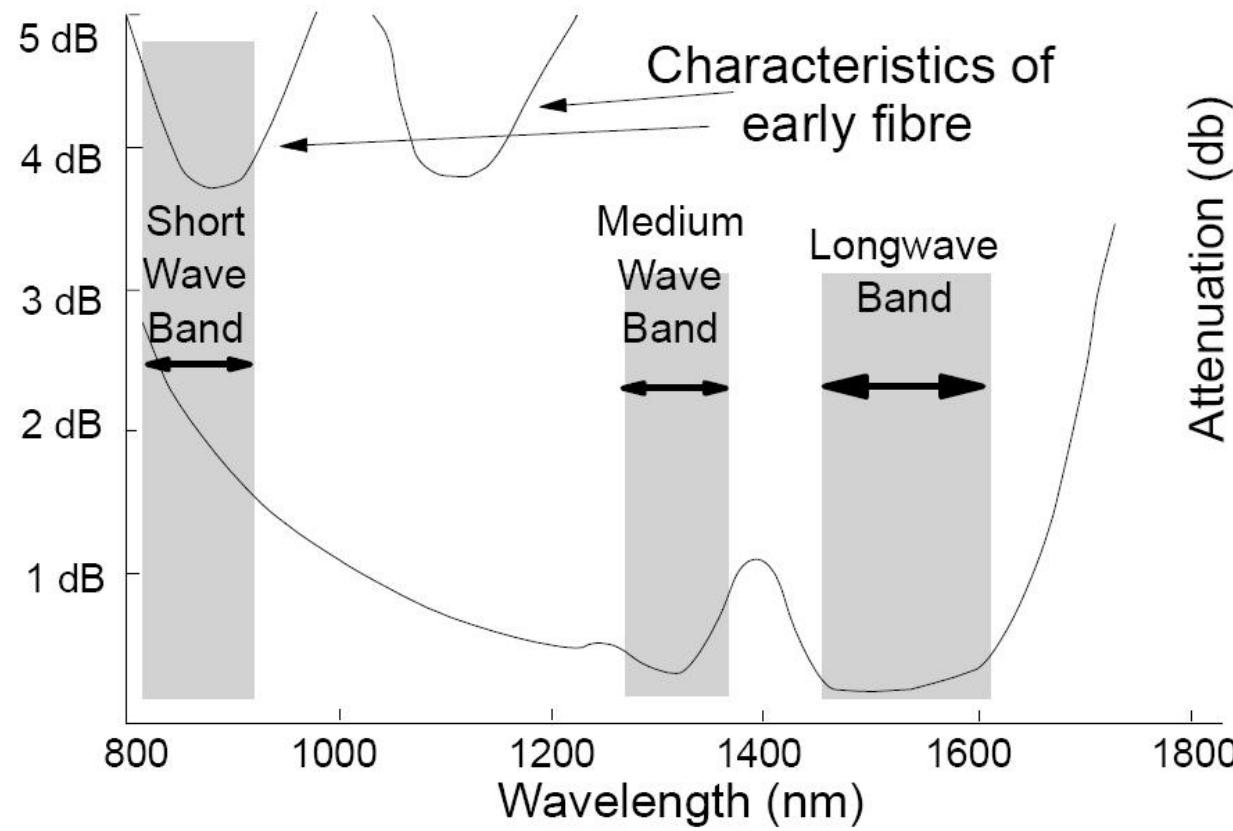
▶ cazuri particulare in care exista rezolvare analitica

- unda
 - incidenta
 - reflectata
- unda
 - directa
 - inversa

$$E_y = E^+ \cdot e^{-\alpha \cdot z} \cdot e^{j(\omega \cdot t - \beta \cdot z)} + E^- \cdot e^{-\alpha \cdot z} \cdot e^{j(\omega \cdot t + \beta \cdot z)}$$



Atenuarea pe 1 km în SiO₂



Atenuare

$$E_y(z_1) = Ct \cdot e^{-\alpha \cdot z_1} \cdot e^{j(\omega \cdot t - \beta \cdot z_1)}$$

$$E_y(z_2) = Ct \cdot e^{-\alpha \cdot z_2} \cdot e^{j(\omega \cdot t - \beta \cdot z_2)}$$

$$W, P \sim \int E^2$$

$$A = \frac{P_2}{P_1} = \frac{Ct^2 \cdot e^{-2\alpha \cdot z_2}}{Ct^2 \cdot e^{-2\alpha \cdot z_1}} = e^{-2\alpha \cdot (z_2 - z_1)}$$

$$A[dB] = 10 \log_{10} \frac{P_2}{P_1} = 10 \log_{10} [e^{-2\alpha \cdot (z_2 - z_1)}]$$

$$A[dB] = -20 \cdot \alpha \cdot (z_2 - z_1) \log_{10} e = -8.686 \cdot \alpha \cdot (z_2 - z_1)$$

$$A/L[dB/km] = -8.686 \cdot \alpha < 0$$

- ▶ Atenuarea se exprima de obicei in **dB/km**
 - ▶ de obicei valori pozitive
 - ▶ semnul = **implicit**

Reprezentare logarithmică

$$\text{dB} = 10 \cdot \log_{10} (P_2 / P_1)$$

$$\text{dBm} = 10 \cdot \log_{10} (P / 1 \text{ mW})$$

$$0 \text{ dB} = 1$$

$$+ 0.1 \text{ dB} = 1.023 (+2.3\%)$$

$$+ 3 \text{ dB} = 2$$

$$+ 5 \text{ dB} = 3$$

$$+ 10 \text{ dB} = 10$$

$$-3 \text{ dB} = 0.5$$

$$-10 \text{ dB} = 0.1$$

$$-20 \text{ dB} = 0.01$$

$$-30 \text{ dB} = 0.001$$

$$0 \text{ dBm} = 1 \text{ mW}$$

$$3 \text{ dBm} = 2 \text{ mW}$$

$$5 \text{ dBm} = 3 \text{ mW}$$

$$10 \text{ dBm} = 10 \text{ mW}$$

$$20 \text{ dBm} = 100 \text{ mW}$$

$$-3 \text{ dBm} = 0.5 \text{ mW}$$

$$-10 \text{ dBm} = 100 \mu\text{W}$$

$$-30 \text{ dBm} = 1 \mu\text{W}$$

$$-60 \text{ dBm} = 1 \text{ nW}$$

$$[\text{dBm}] + [\text{dB}] = [\text{dBm}]$$

$$[\text{dBm}/\text{Hz}] + [\text{dB}] = [\text{dBm}/\text{Hz}]$$

$$[x] + [\text{dB}] = [x]$$

Calculul atenuarii

$$\text{Pierderi} = \frac{P_{out}}{P_{in}} < 1$$

$$\text{Pierderi[dB]} = 10 \cdot \log_{10} \left(\frac{P_{out}}{P_{in}} \right) < 0$$

$$\text{Pierderi/Atenuare[dB]} = [-] 10 \cdot \log_{10} \left(\frac{P_{out}}{P_{in}} \right)$$

$$\text{Castig} = \frac{P_{out}}{P_{in}} > 1$$

$$\text{Castig[dB]} = 10 \cdot \log_{10} \left(\frac{P_{out}}{P_{in}} \right) > 0$$

$$\text{Atenuare[dB/km]} = \frac{\text{Pierderi[d B]}}{\text{lungime[km]}}$$

Calculul atenuarii

$$\text{Pierderi} = \frac{P_{out}}{P_{in}}$$

$$\text{Pierderi[dB]} = [-] 10 \cdot \log_{10} \left(\frac{P_{out}}{P_{in}} \right)$$

$$\text{Pierderi[dB]} = [-] 10 \cdot \log_{10} \left(\frac{P_{out}}{P_0} \cdot \frac{P_0}{P_{in}} \right) = [-] 10 \cdot \left[\log_{10} \left(\frac{P_{out}}{P_0} \right) - \log_{10} \left(\frac{P_{in}}{P_0} \right) \right]$$

$$\text{Pierderi [dB]} = [-] (P_{out} [\text{dBm}] - P_{in} [\text{dBm}])$$



=



-



Calculul atenuarii

Pierderi/A tenuare $\rightarrow P_{out} < P_{in} \rightarrow P_{out} [\text{dBm}] < P_{in} [\text{dBm}]$

$$P_{out} [\text{dBm}] = P_{in} [\text{dBm}] - \text{Pierderi/A tenuare [dB]}$$


Castig/Amplicare $\rightarrow P_{out} > P_{in} \rightarrow P_{out} [\text{dBm}] > P_{in} [\text{dBm}]$

$$P_{out} [\text{dBm}] = P_{in} [\text{dBm}] + \text{Castig/Amplicare [dB]}$$


Reprezentare logaritmică

$$\text{dB} = 10 \cdot \log_{10} (P_2 / P_1)$$

$$\text{dBm} = 10 \cdot \log_{10} (P / 1 \text{ mW})$$

$$0 \text{ dB} = 1$$

$$+ 0.1 \text{ dB} = 1.023 (+2.3\%)$$

$$+ 3 \text{ dB} = 2$$

$$+ 5 \text{ dB} = 3$$

$$+ 10 \text{ dB} = 10$$

$$-3 \text{ dB} = 0.5$$

$$-10 \text{ dB} = 0.1$$

$$-20 \text{ dB} = 0.01$$

$$-30 \text{ dB} = 0.001$$

$$0 \text{ dBm} = 1 \text{ mW}$$

$$3 \text{ dBm} = 2 \text{ mW}$$

$$5 \text{ dBm} = 3 \text{ mW}$$

$$10 \text{ dBm} = 10 \text{ mW}$$

$$20 \text{ dBm} = 100 \text{ mW}$$

$$-3 \text{ dBm} = 0.5 \text{ mW}$$

$$-10 \text{ dBm} = 100 \mu\text{W}$$

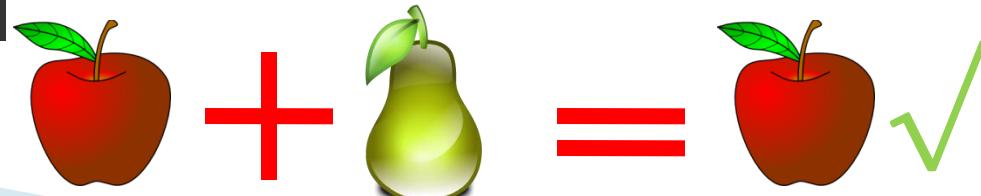
$$-30 \text{ dBm} = 1 \mu\text{W}$$

$$-60 \text{ dBm} = 1 \text{ nW}$$

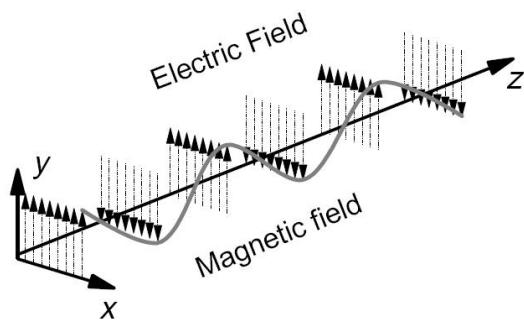
$$[\text{dBm}] + [\text{dB}] = [\text{dBm}]$$

$$[x] + [\text{dB}] = [x]$$

$$[\text{dBm}/\text{Hz}] + [\text{dB}] = [\text{dBm}/\text{Hz}]$$



Parametri de propagare



$$\nabla \times E = -j\omega\mu \cdot H$$

$$H_x = \frac{j\gamma \cdot E_y}{\omega\mu}$$

Mediu fara pierderi, $\sigma = 0$ $\gamma = j\omega \cdot \sqrt{\epsilon\mu}$

$$\eta = \frac{E_y}{H_x} = \sqrt{\frac{\mu}{\epsilon}} \quad \text{Impedanta intrinseca a mediului}$$

$$E_y = A \cdot e^{-\alpha \cdot z} \cdot e^{j(\omega \cdot t - \beta \cdot z)} \quad \text{punctele de faza constante: } (\omega \cdot t - \beta \cdot z) = \text{const}$$

Viteza de faza $v = \frac{dz}{dt} = \frac{\omega}{\beta} = \frac{1}{\sqrt{\epsilon\mu}}$

Viteza de grup $v_g = \frac{dz}{dt} = \frac{d\omega}{d\beta}$ in medii dispersive unde $\beta = \beta(\omega)$

Parametri de propagare

► In vid

$$\eta_0 = \sqrt{\frac{\mu_0}{\epsilon_0}} = 377\Omega \quad v = v_g = c_0 \quad c_0 = \frac{1}{\sqrt{\epsilon_0 \cdot \mu_0}} = 2,99790 \cdot 10^8 \text{ m/s}$$

$$\lambda_0 = \frac{2\pi}{\beta} = \frac{c_0}{f} \quad T = \frac{2\pi}{\omega} = \frac{1}{f}$$

Periodicitate in spatiu

Periodicitate in timp

► In mediu nedispersiv ϵ_r

$$c = \frac{1}{\sqrt{\epsilon \cdot \mu_0}} = \frac{1}{\sqrt{\epsilon_0 \epsilon_r \cdot \mu_0}} = \frac{c_0}{\sqrt{\epsilon_r}} \quad v = v_g = c$$

$$n = \sqrt{\epsilon_r} \quad \text{Indice de refractie al mediului} \quad c = \frac{c_0}{n}$$

$$T = \frac{2\pi}{\omega} = \frac{1}{f} \quad \lambda = \frac{2\pi}{\beta} = \frac{c}{f} \quad \lambda = \frac{c_0}{n \cdot f} = \frac{\lambda_0}{n}$$



Parametri, dependenta de mediu

$$\eta_0 = \sqrt{\frac{\mu_0}{\epsilon_0}} = 377\Omega$$

$$c_0 = \frac{1}{\sqrt{\epsilon_0 \cdot \mu_0}} = 2,99790 \cdot 10^8 \text{ m/s}$$

$n=1$

$$T = \frac{2\pi}{\omega} = \frac{1}{f}$$

$$\lambda_0 = \frac{2\pi}{\beta} = \frac{c_0}{f}$$

$$\eta = \frac{\eta_0}{n}$$

$$c = \frac{c_0}{n}$$

$n = \sqrt{\epsilon_r}$

$$T = \frac{2\pi}{\omega} = \frac{1}{f}$$

$$\lambda = \frac{c_0}{n \cdot f} = \frac{\lambda_0}{n}$$

$$\lambda = \lambda(n)$$

$f = \text{indep.}$

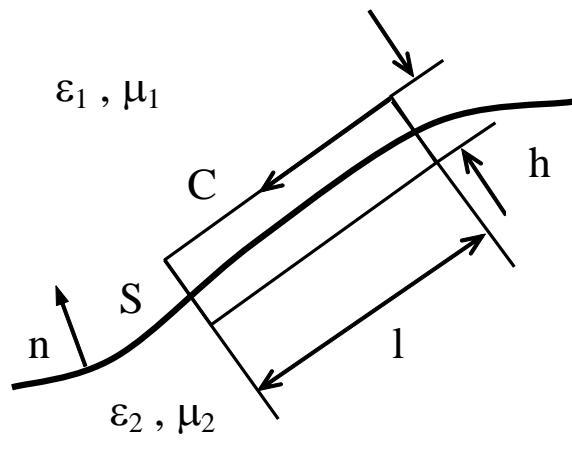
ITU G.692

"the allowed channel frequencies are based on a 50 GHz grid with the reference frequency at 193.10 THz"

SI

"a source that emits monochromatic radiation of frequency $540 \cdot 10^{12}$ Hz"

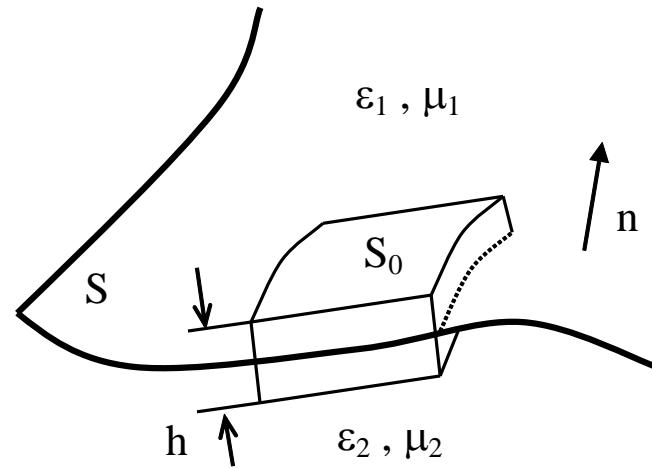
Condiții la limita de separație între două medii



a)

$$n \times (E_1 - E_2) = 0$$

$$n \times (H_1 - H_2) = J_s$$



b)

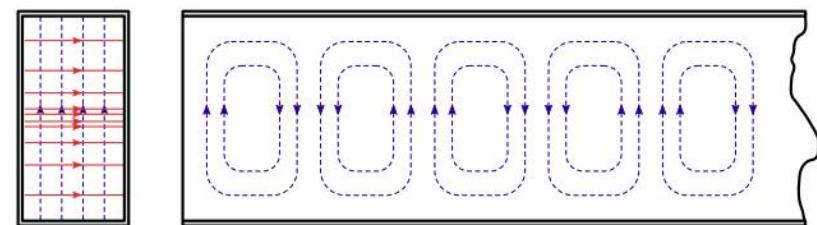
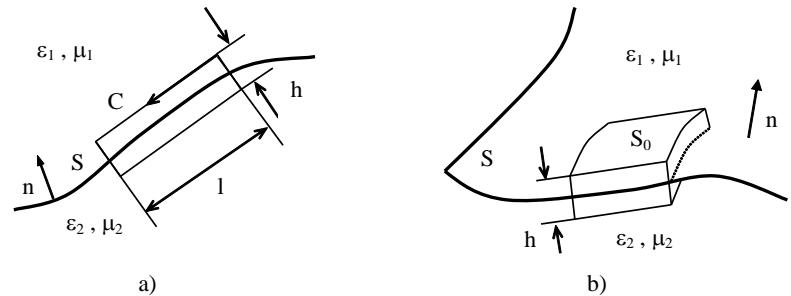
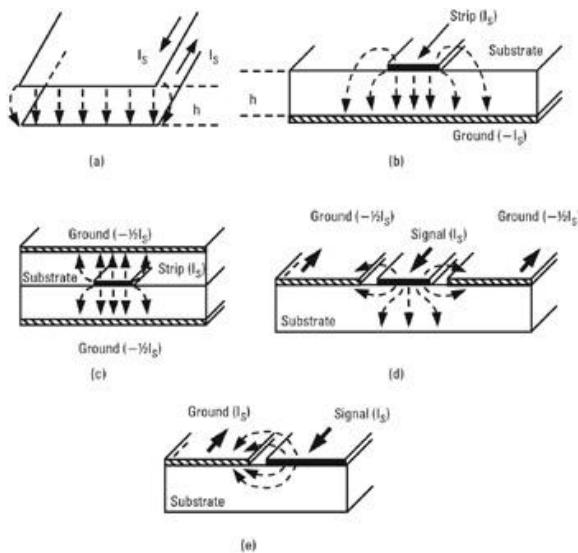
$$n \cdot (D_1 - D_2) = \rho_s$$

$$n \cdot (B_1 - B_2) = 0$$

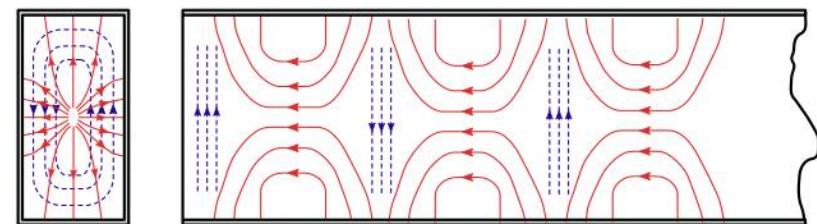
- ▶ Daca un mediu este metal ideal toate campurile se anuleaza in interior

Moduri in medii delimitate

- ▶ Campul electric **trebuie** sa fie perpendicular pe un perete metalic sau nul
- ▶ Campul magnetic **trebuie** sa fie tangent la un perete metalic sau nul



TE_{10}



TM_{11}

Moduri in medii delimitate

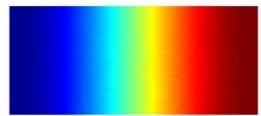
- ▶ Câmpuri electromagnetice cu variație armonică în timp
 - simplificarea ecuațiilor lui Maxwell

$$X = X_0 e^{j \cdot \omega \cdot t} \quad \frac{\partial X}{\partial t} = j \cdot \omega \cdot X \quad g(\omega) = \int_{-\infty}^{\infty} f(t) \cdot e^{-j \omega t} dt \quad f(t) = \int_{-\infty}^{\infty} g(\omega) \cdot e^{j \omega t} d\omega$$

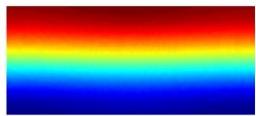
- ▶ În medii delimitate solutiile ecuațiilor lui Maxwell trebuie să verifice condițiile la limită
 - solutiile trebuie să respecte anumite condiții suplimentare

Moduri in medii delimitate

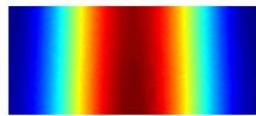
TE10



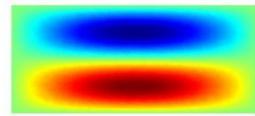
TE01



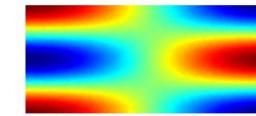
TE20



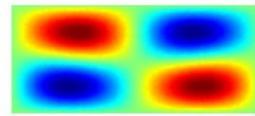
TM12



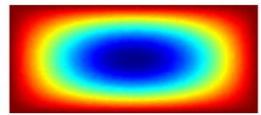
TE12



TM22



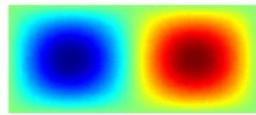
TM11



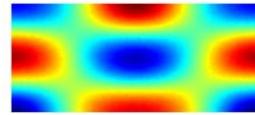
TE11



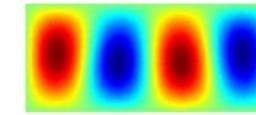
TM21



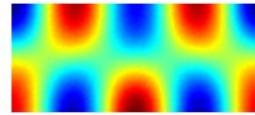
TE22



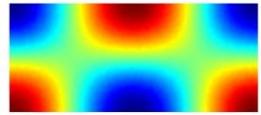
TM41



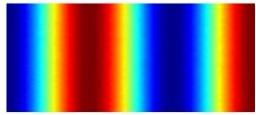
TE41



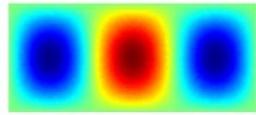
TE21



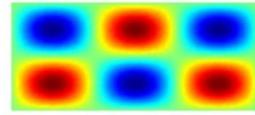
TE30



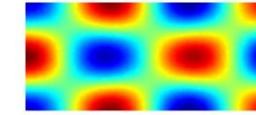
TM31



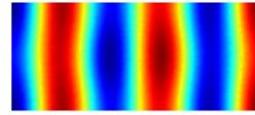
TM32



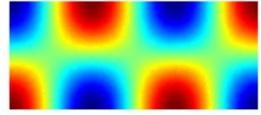
TE32



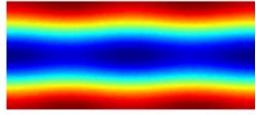
TE50



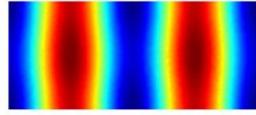
TE31



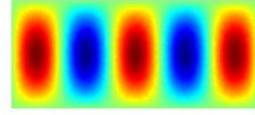
TE02



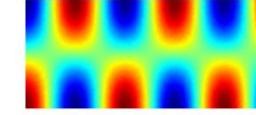
TE40



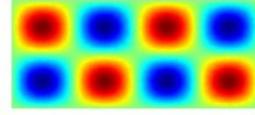
TM51



TE51



TM42



► Similar cu transformata Fourier

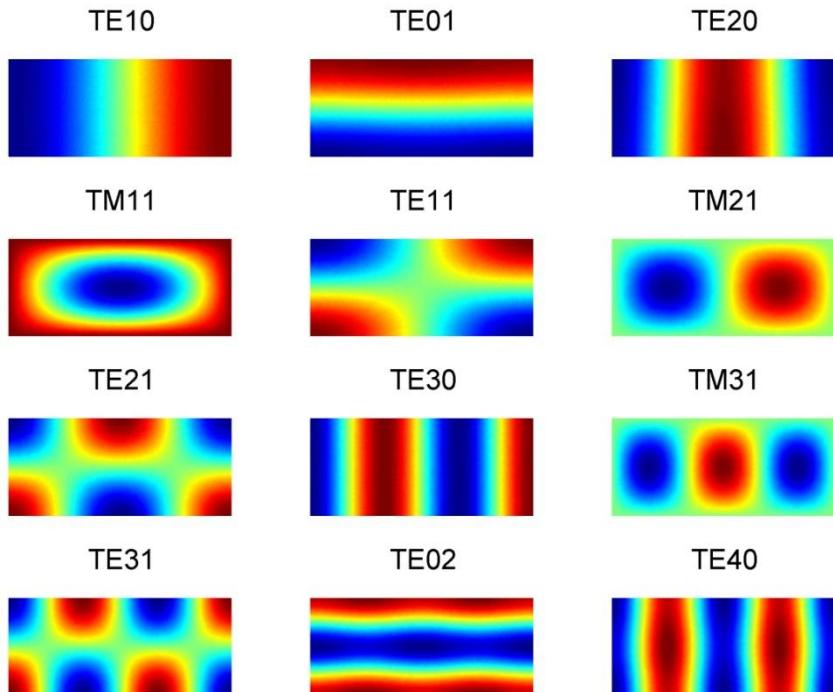
$$g(\omega) = \int_{-\infty}^{\infty} f(t) \cdot e^{-j\omega t} dt \quad f(t) = \int_{-\infty}^{\infty} g(\omega) \cdot e^{j\omega t} d\omega$$

$$E^+, E^- = \sum_1^\infty A_i \cdot Mod_i$$

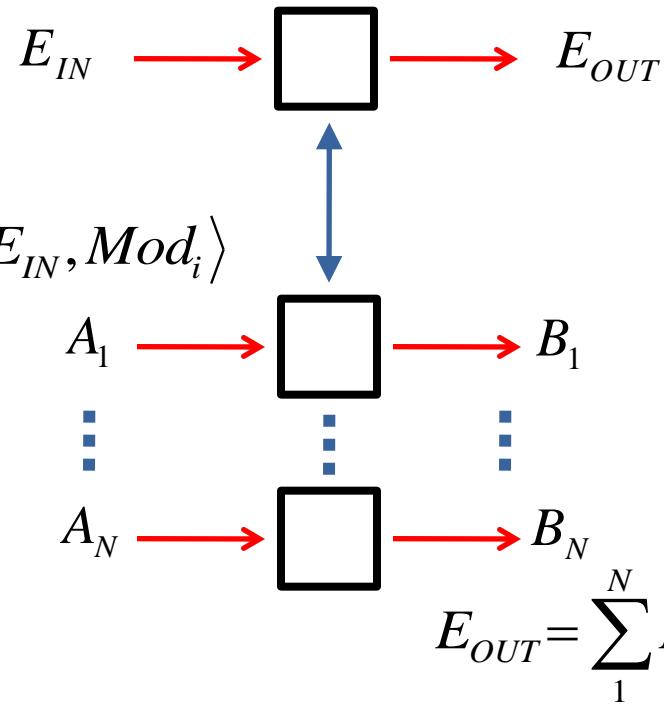
$$A_i = \langle E, Mod_i \rangle$$

Modele matematice

- ▶ cazuri particulare in care exista rezolvare analitica
 - moduri in medii delimitate



$$E = \sum_1^{\infty} A_i \cdot Mod_i \quad A_i = \langle E, Mod_i \rangle$$



Ghid cilindric dielectric

► Ecuațiile lui Maxwell în coordonate cilindrice

$$\frac{\partial^2 U}{\partial r^2} + \frac{1}{r} \frac{\partial U}{\partial r} + \frac{1}{r^2} \frac{\partial^2 U}{\partial \phi^2} + \frac{\partial^2 U}{\partial z^2} + n^2 k_o^2 U = 0 \quad \begin{matrix} a - \text{raza miezului} \\ U - E(r) \text{ sau } H(r) \end{matrix}$$

$$U(r, \phi, z) = u(r)e^{-jl\phi}e^{-j\beta z}, \quad l = 0, \pm 1, \pm 2, \dots$$

$$\frac{d^2 u}{dr^2} + \frac{1}{r} \frac{du}{dr} + \left(n^2(r) k_o^2 - \beta^2 - \frac{l^2}{r^2} \right) u = 0$$

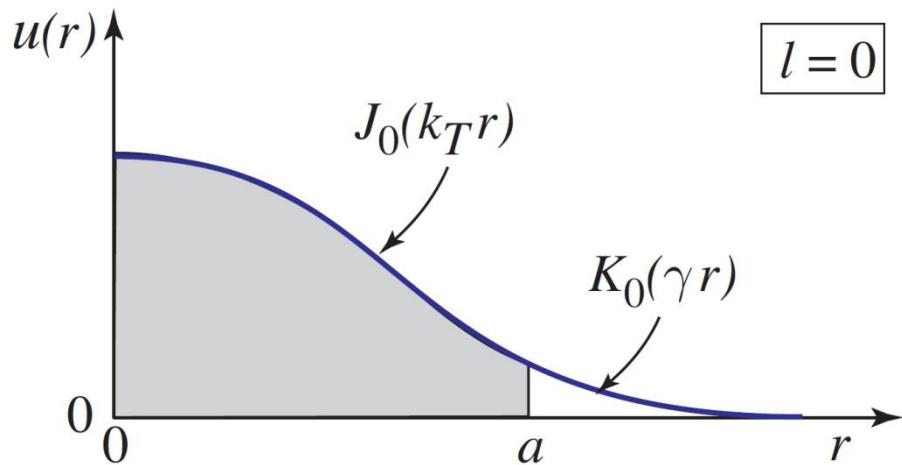
$$\frac{d^2 u}{dr^2} + \frac{1}{r} \frac{du}{dr} + \left(k_T^2 - \frac{l^2}{r^2} \right) u = 0, \quad r < a$$

$$\frac{d^2 u}{dr^2} + \frac{1}{r} \frac{du}{dr} - \left(\gamma^2 + \frac{l^2}{r^2} \right) u = 0, \quad r > a$$

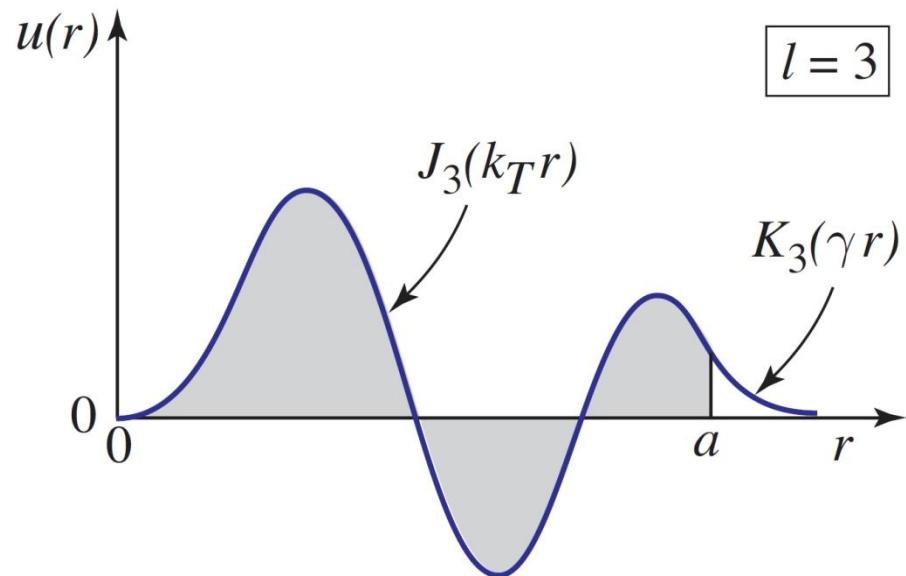
Ghid cilindric dielectric

- ▶ soluții proportionale cu funcții Bessel

$$u(r) \propto \begin{cases} J_l(k_T r), & r < a \quad (\text{core}) \\ K_l(\gamma r), & r > a \quad (\text{cladding}) \end{cases}$$



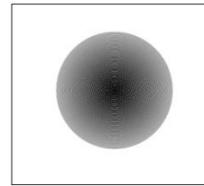
$l = 0$



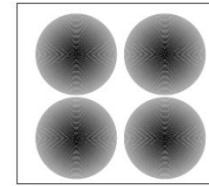
$l = 3$

Moduri in fibra

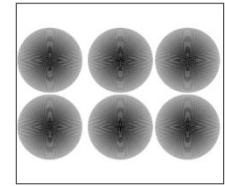
- ▶ Moduri in ghid rectangular



TEM₀₀

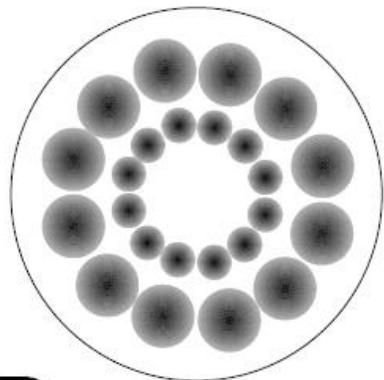


TEM₁₁

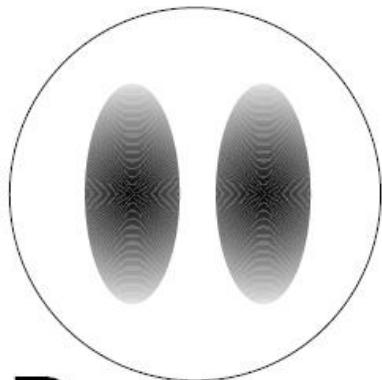


TEM₂₁

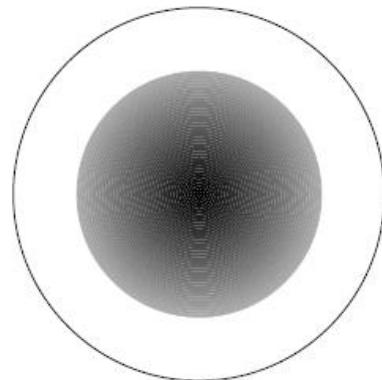
- ▶ Moduri linear polarizate in fibra



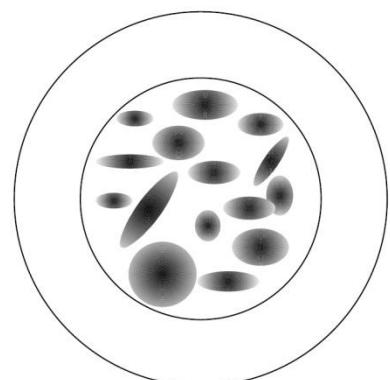
LP₆₂



LP₁₁



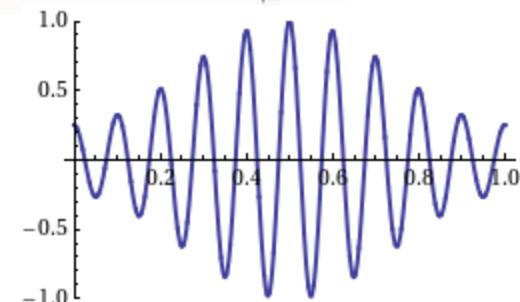
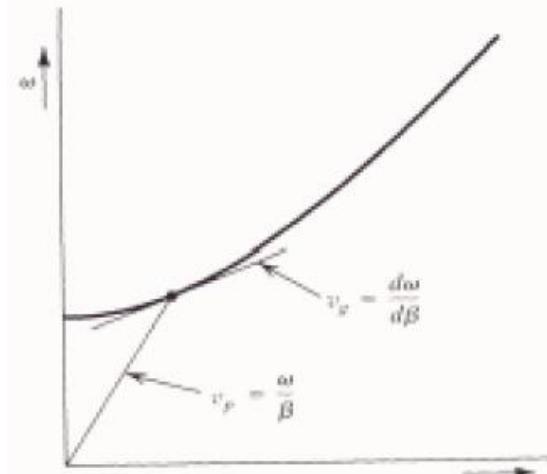
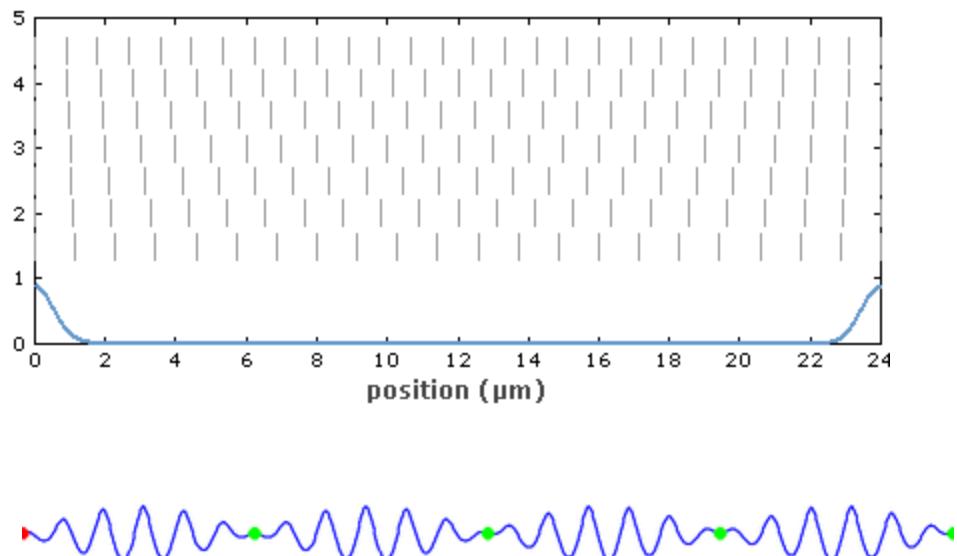
LP₀₁



"Sparkle" pattern

Viteze de grup si faza

- ▶ Viteza de faza – viteza virtuală cu care circula punctul cu o anumita fază
- ▶ Viteza de grup – viteza cu care circula informația (energia) – în medii cu dispersie normală



Dispersia

- ▶ În medii disperensive $\beta = \beta(\omega)$, $n = n(\omega)$, $v_g = \frac{d\omega}{d\beta} = \frac{1}{\left(\frac{d\beta}{d\omega}\right)}$
- ▶ Timpul în care o radiatie ajunge la distanta L

$$\tau = \frac{L}{v_g} = L \cdot \frac{d\beta}{d\omega} = L \cdot \frac{d}{d\omega} \left(\frac{\omega \cdot n}{c} \right) = \frac{L}{c} \left(n + \omega \frac{dn}{d\omega} \right)$$

- ▶ Se preferă exprimarea în funcție de lungimea de undă

$$\lambda = \frac{c}{f} = \frac{2\pi \cdot c}{\omega} \rightarrow \frac{d\lambda}{d\omega} = -\frac{2\pi \cdot c}{\omega^2} = -\frac{\lambda}{\omega} \rightarrow d\omega = -\frac{\omega}{\lambda} \cdot d\lambda$$

$$\tau = \frac{L}{c} \left(n + \omega \frac{dn}{d\omega} - \frac{\omega}{\lambda} \cdot d\lambda \right) = \frac{L}{c} \left(n - \lambda \cdot \frac{dn}{d\lambda} \right)$$

Dispersia

► $n = n(\omega)$ $\tau = \frac{L}{c} \left(n - \lambda \cdot \frac{dn}{d\lambda} \right)$

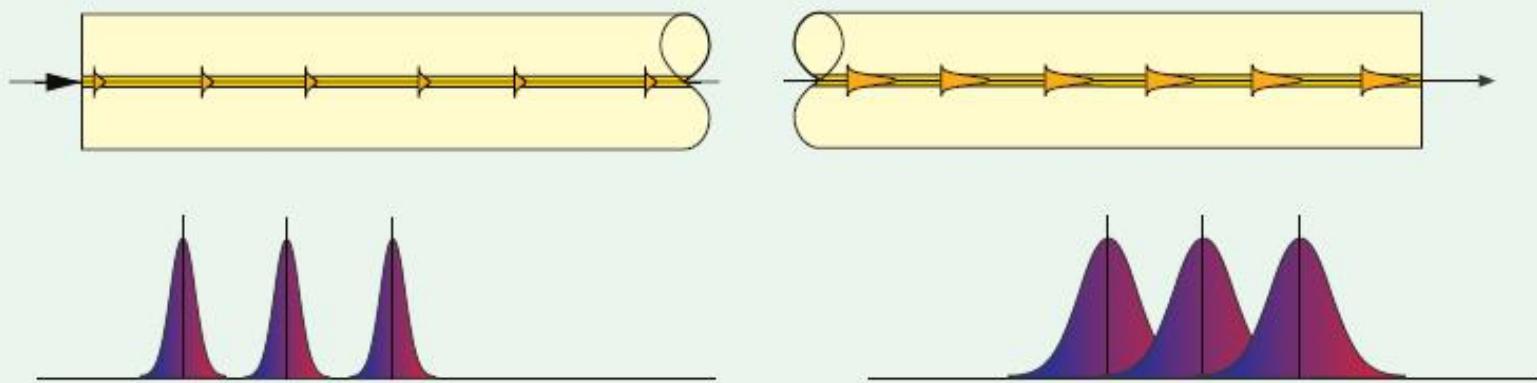
$$\frac{d\tau}{d\lambda} = \frac{L}{c} \left(\frac{dn}{d\lambda} - \lambda \frac{d^2n}{d\lambda^2} - \frac{dn}{d\lambda} \right) = -\frac{L}{c} \cdot \lambda \cdot \frac{d^2n}{d\lambda^2}$$
$$D \stackrel{not}{=} -\frac{\lambda}{c} \cdot \frac{d^2n}{d\lambda^2} \quad (s/m^2)$$

- Dispersia **D** se exprima de obicei in **ps/nm/km** si permite aflarea intarzierilor aparute intre "moduri" (latirea impulsurilor) pentru o anumita latime spectrala $\Delta\lambda$ si o anumita distanta parcursa L

$$\Delta\tau = D \cdot \Delta\lambda \cdot L$$

Dispersie

> 50 km Single-mode step index
< 10 km Multimode graded index
< 1 km Multimode step index



Transmission:

Well-defined pulses but not absolutely monochromatic.

Typical spectral width < 0.8 nm

Reception:

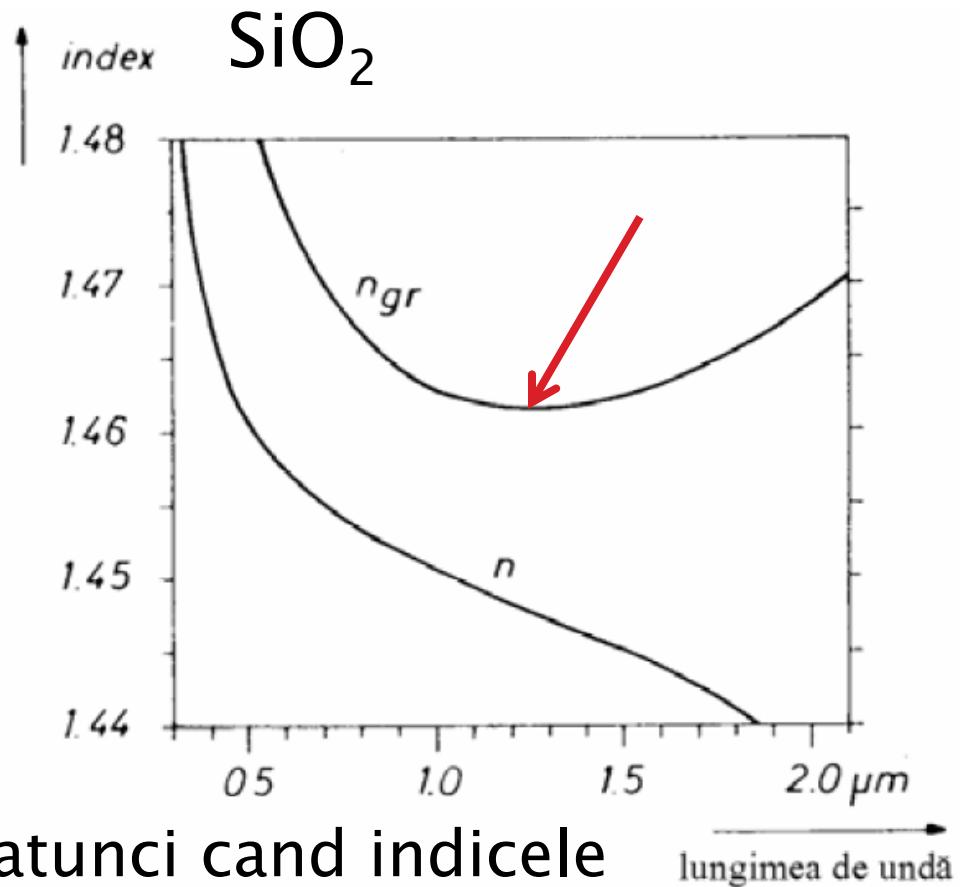
Pulse broadening caused by the laser's spectral width and the difference between the refractive indices of the red and blue ends of the light pulse.

Dispersie normală

$$\tau = \frac{L}{v_g} = \frac{L}{c} \left(n - \lambda \cdot \frac{dn}{d\lambda} \right)$$

$$v_g = \frac{c}{n_{gr}} \quad n_{gr} = n - \lambda \frac{dn}{d\lambda}$$

$$D = \frac{1}{L} \cdot \frac{d\tau}{d\lambda} = \frac{1}{c} \cdot \frac{dn_{gr}}{d\lambda}$$

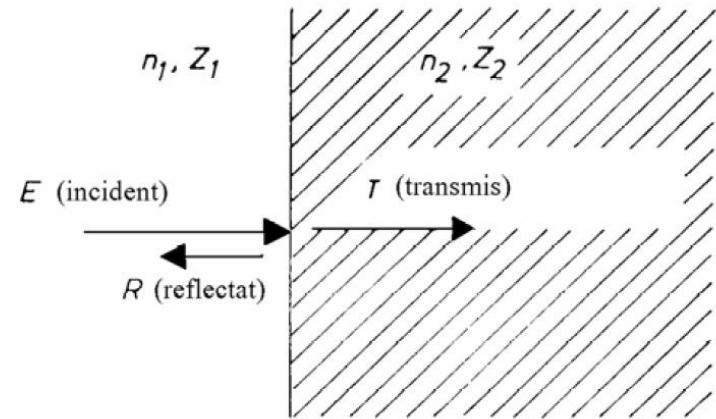


- ▶ Dispersia este **0** atunci cand indicele de refractie de grup este minim
- ▶ Pentru sticla $\lambda_0 \sim 1310$ nm

Transmisia puterii intre medii

- ▶ incidenta normală
- ▶ reflexia în amplitudine

$$Z = \frac{Z_0}{n} \quad \Gamma = \frac{Z_2 - Z_1}{Z_2 + Z_1} = \frac{n_1 - n_2}{n_1 + n_2}$$



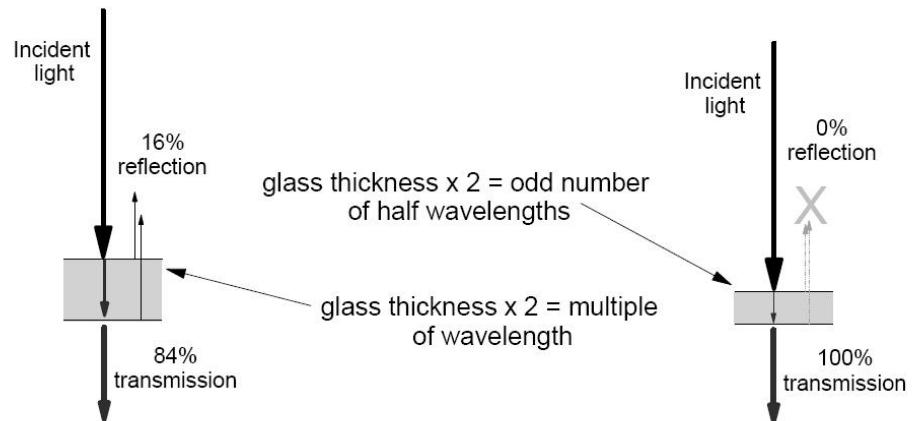
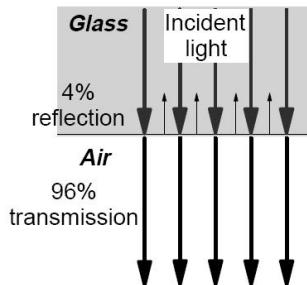
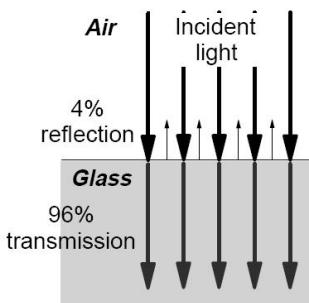
- ▶ densitatea de putere proporțională cu patratul amplitudinii câmpului

$$r = \left(\frac{n_1 - n_2}{n_1 + n_2} \right)^2 \quad t = \left(\frac{2n_1}{n_1 + n_2} \right)^2$$

- ▶ interfata aer-sticla ($n_1 = 1$, $n_2 = 1.5$)

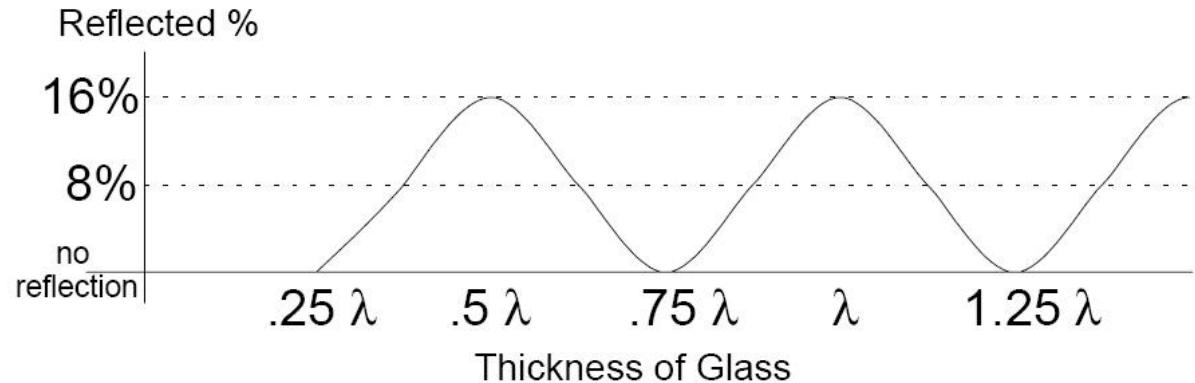
$$\Gamma = \frac{1.5 - 1}{1.5 + 1} = 0.2; \quad r = \Gamma^2 = 0.04 = 4\%$$

Transmisia printr-o lamela



$$\Gamma = \frac{1.5 - 1}{1.5 + 1} = 0.2; \quad r = \Gamma^2 = 0.04 = 4\% \quad \Gamma_{\max} = 0.2 + 0.2; \quad r_{\max} = \Gamma_{\max}^2 = 0.16 = 16\%$$

- ▶ apare interferenta intre diversele unde reflectate
- ▶ se aduna câmpurile nu puterile
- ▶ lamele antireflexive



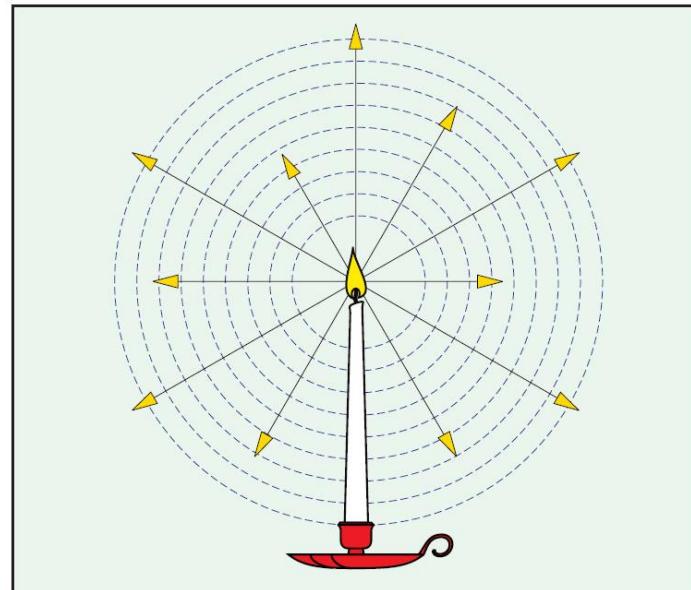
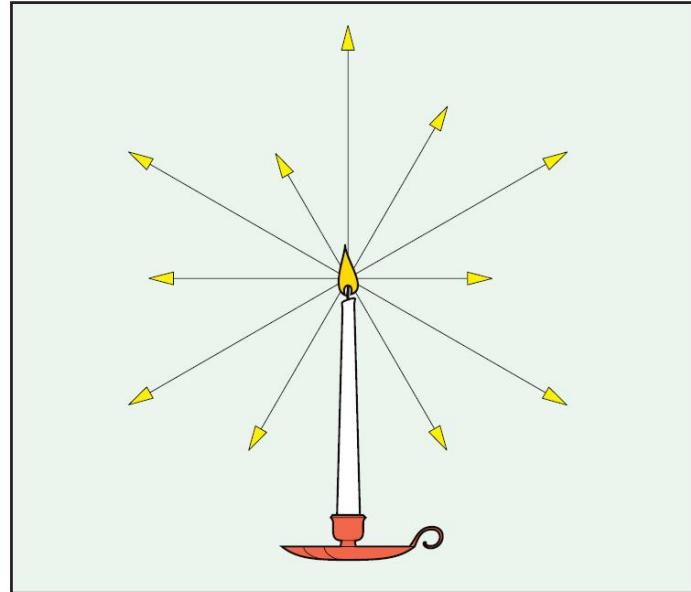
Optică geometrică

(tot) Capitolul 2

Raze de lumina

- ▶ Lumina este constituită din raze care se propagă în linie dreaptă în medii omogene
- ▶ Sursa omnidirecțională: emite similar în toate direcțiile
- ▶ Densitatea de energie luminoasă descrește invers proporțional cu pătratul distanței față de sursă (energia se împarte uniform pe suprafața întregii sfere)

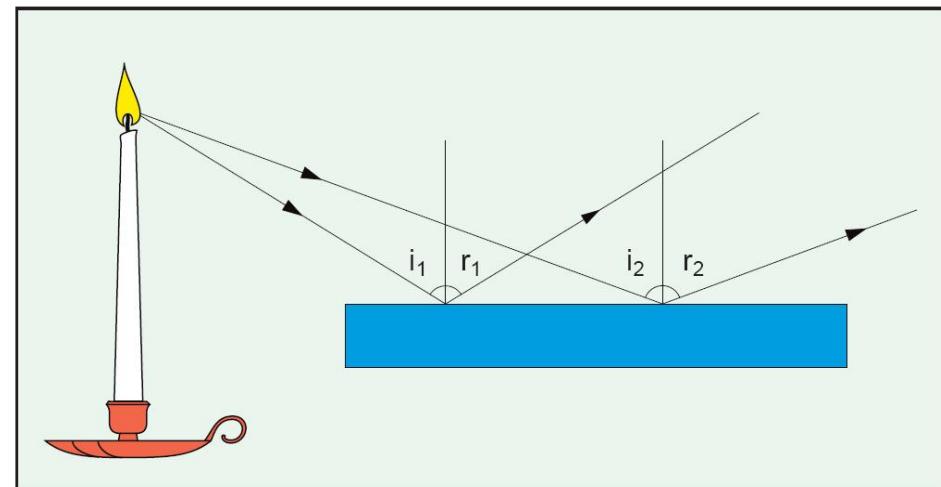
$$P = \frac{P_0}{r^2}$$



Reflexia luminii

- ▶ la suprafata de separatie dintre doua medii, (o parte din) lumina se intoarce in mediul de incidenta
 - ▶ unghiul dintre raza incidenta si normala (ϕ_i) este egal cu unghiul dintre raza reflectata si normala (ϕ_r)
- ▶ Legea reflexiei

$$\phi_i = \phi_r$$



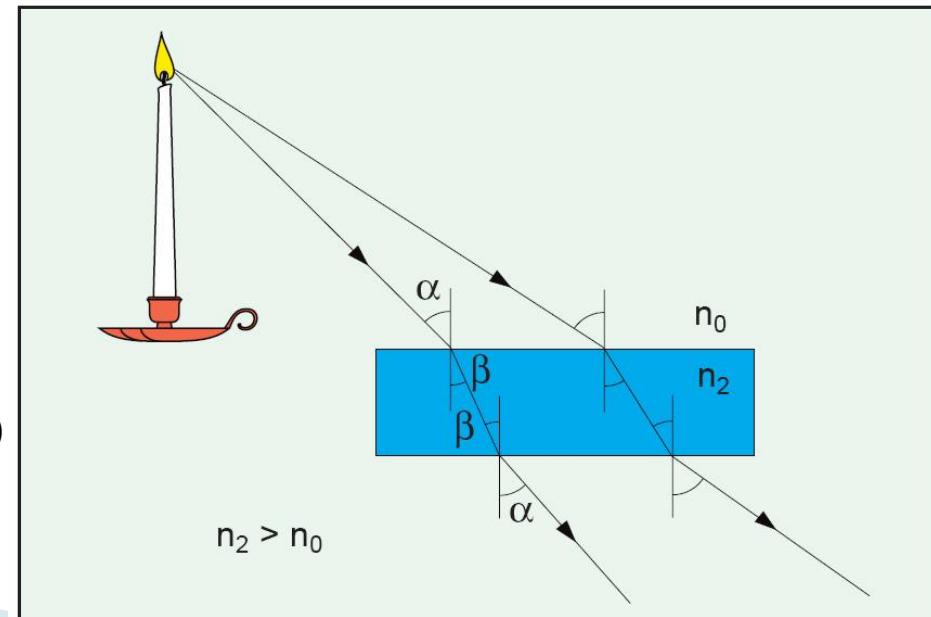
Refractia luminii

- ▶ la suprafața de separație dintre două medii, (o parte din) lumina se (poate) propaga în mediul de transmisie sub un unghi diferit de unghiul incident
 - ▶ la trecerea în medii mai “dense” (optic) lumina se apropie de normală
 - ▶ la trecerea în medii mai “puțin dense” (optic) lumina se depărtează de normală
- ▶ Legea lui Snell
(a refacției)

$$n_1 \cdot \sin \phi_i = n_2 \cdot \sin \phi_R$$

ϕ_i - unghi incident (în n_1)

ϕ_R - unghi de refacție (în n_2)



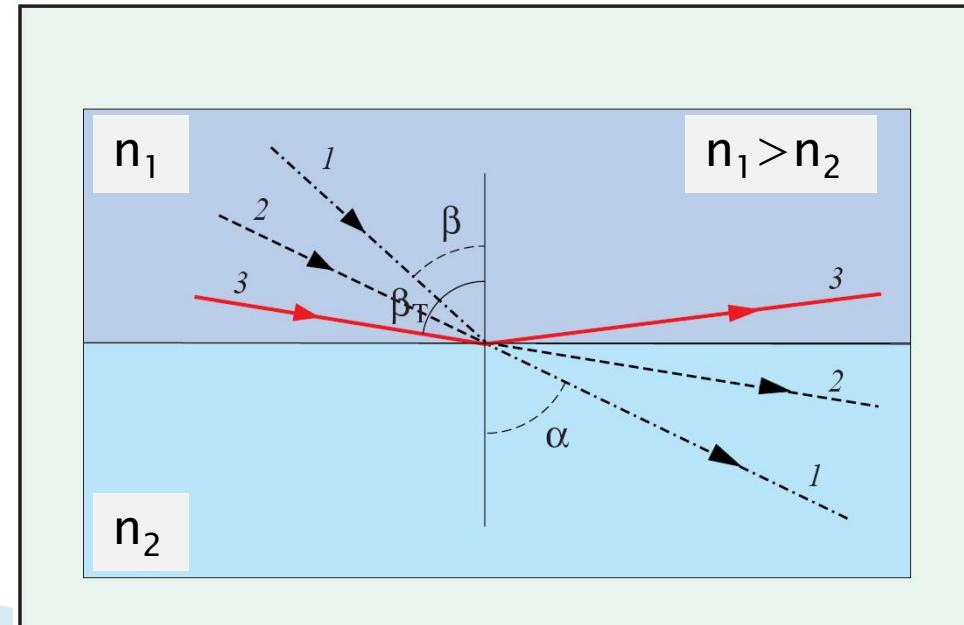
Reflexia totală

- ▶ Apare **numai când** lumina se propaga dintr-un mediu mai dens optic intr-un mediu mai puțin dens
- ▶ La intersecția luminii cu suprafața de separație a două medii se întâlnesc în general raze reflectate **și** raze refractate
- ▶ Pentru un unghi de incidenta numit **unghi critic**, raza refractată se obține în lungul suprafeței de separație
- ▶ Pentru orice unghi mai mare decât unghiul critic există numai raza reflectată

$$n_1 > n_2; \quad \phi_R = 90^\circ$$

$$n_1 \cdot \sin \phi_C = n_2$$

$$\phi_C = \arcsin\left(\frac{n_2}{n_1}\right)$$

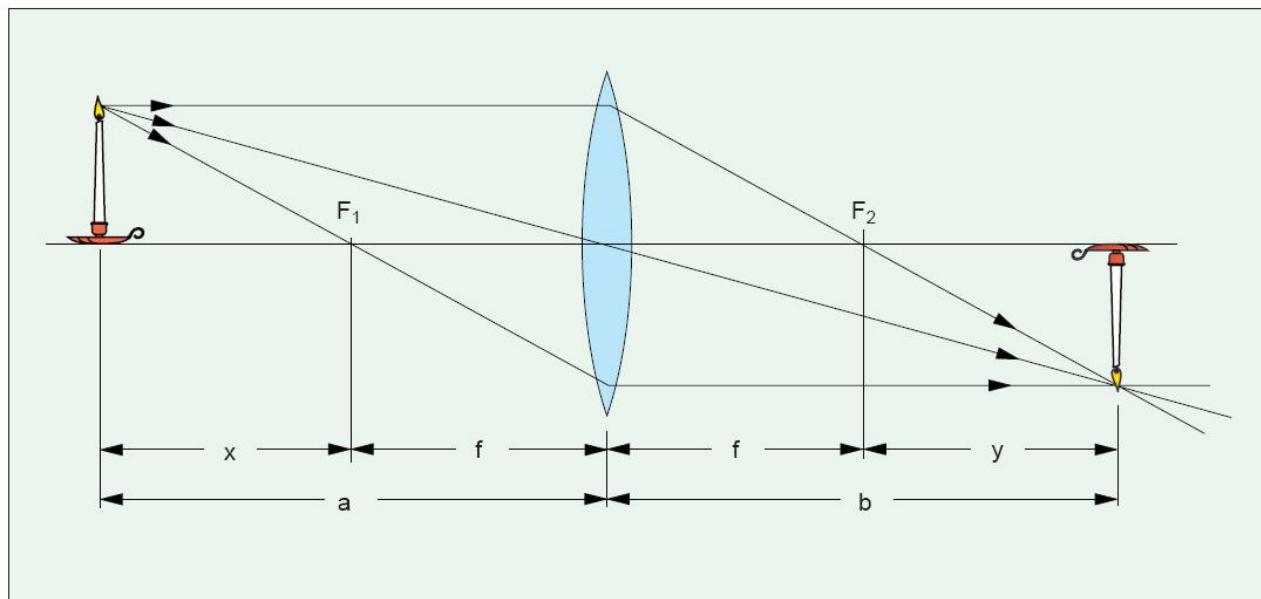


Lentile

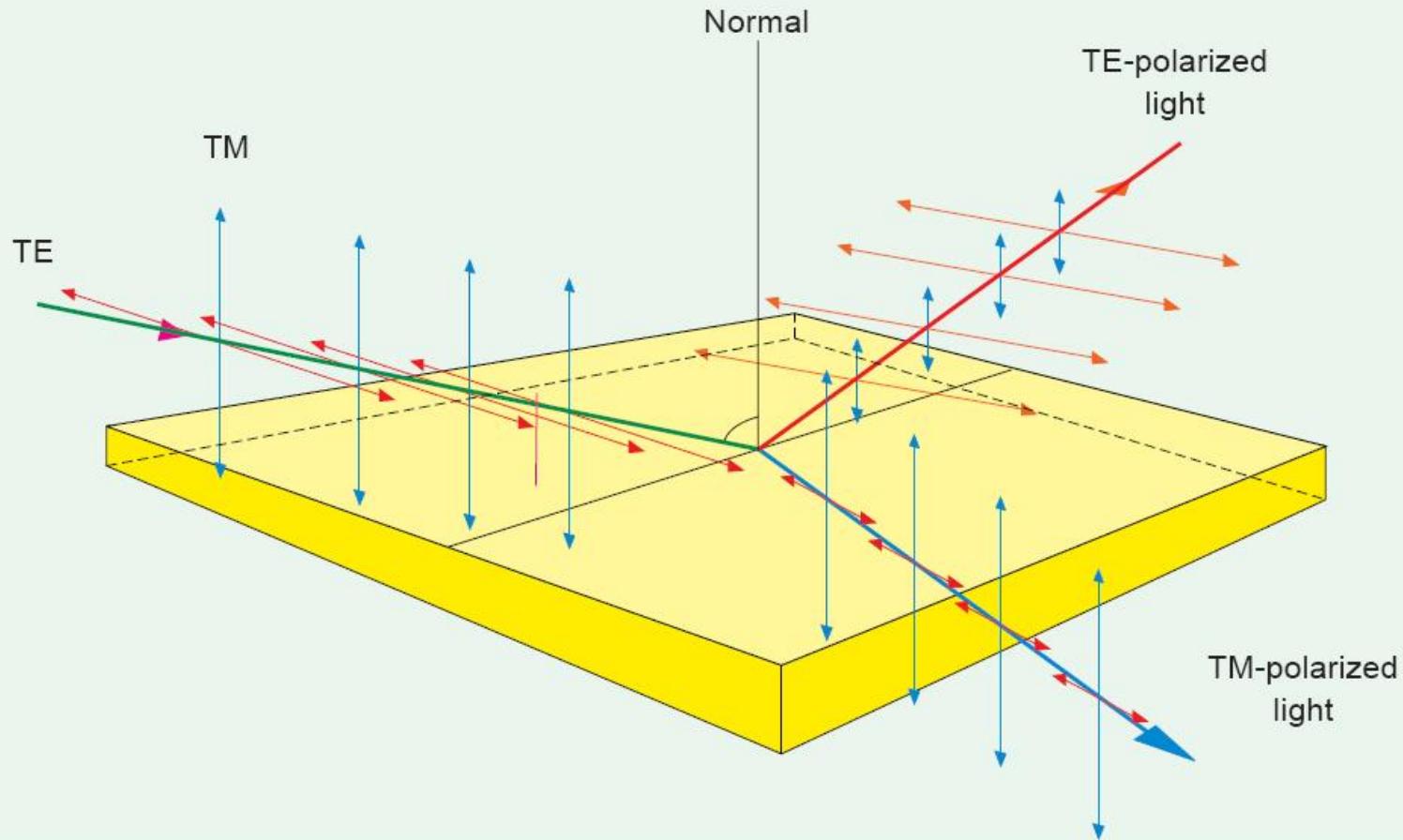
- ▶ Razele de lumina paralele sunt concentrate intr-un punct numit focar, aflat la **distanța focală** de planul lentilei
- ▶ O sursa omnidirectională pozitionată în focar va permite obținerea unui fascicul paralel

$$\frac{1}{a} + \frac{1}{b} = \frac{1}{f}$$

$$x \cdot y = f^2$$



Polarizarea luminii



Polarizarea luminii

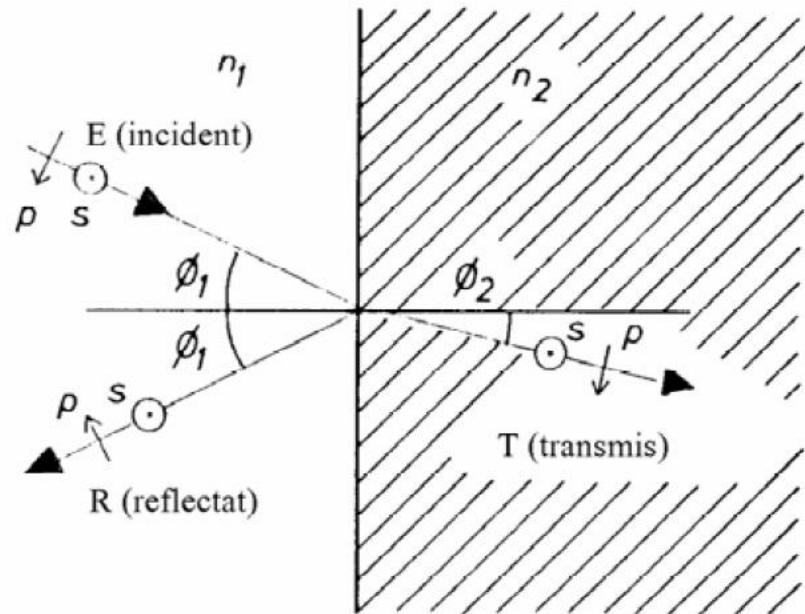
- ▶ incidenta oblica
- ▶ reflexiile in amplitudine a campului:

$$r_s = -\frac{\sin(\phi_1 - \phi_2)}{\sin(\phi_1 + \phi_2)}$$

$$r_p = \frac{\tan(\phi_1 - \phi_2)}{\tan(\phi_1 + \phi_2)}$$

$$t_s = \frac{2 \sin \phi_2 \cos \phi_1}{\sin(\phi_1 + \phi_2)}$$

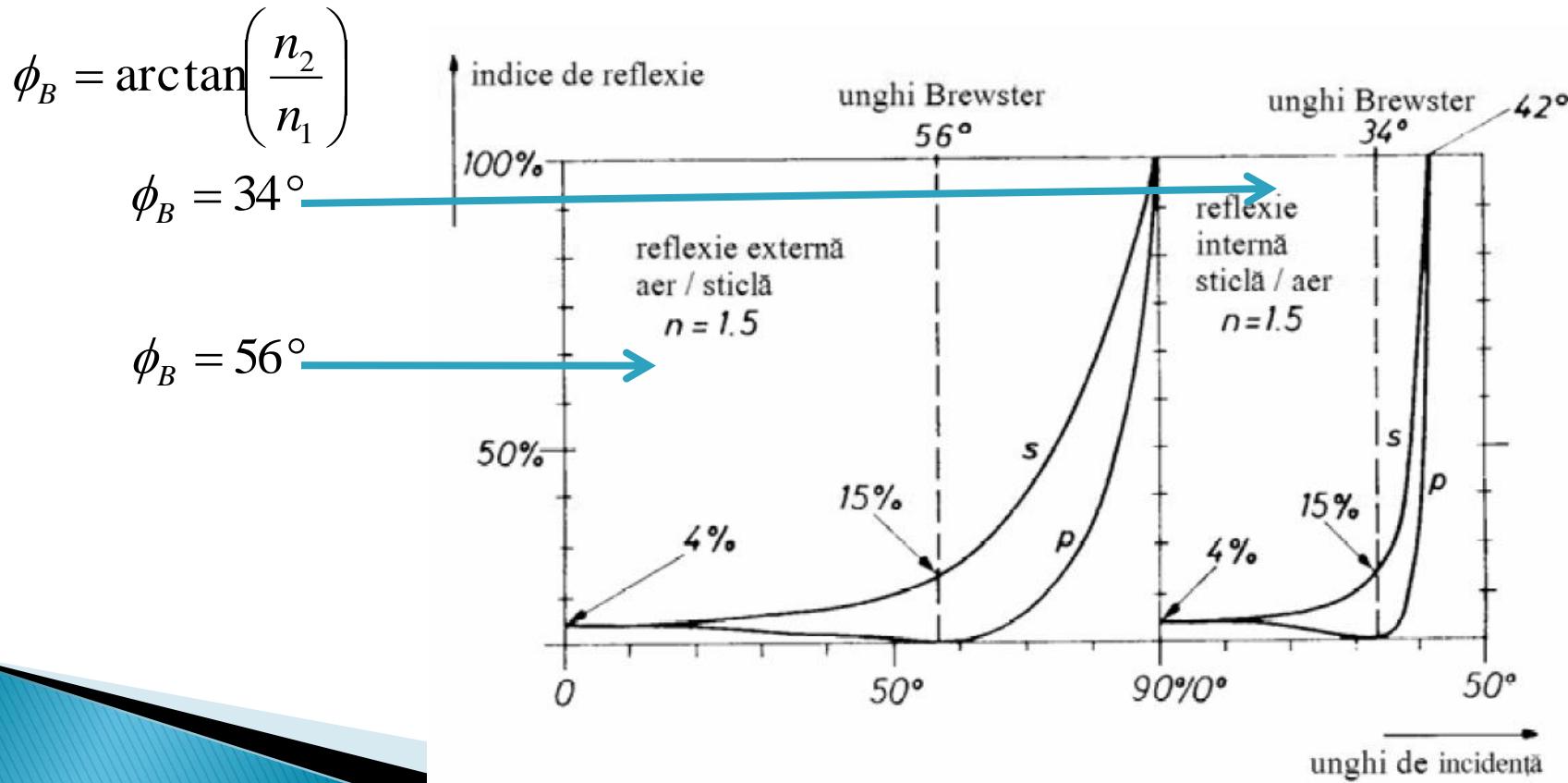
$$t_p = \frac{2 \sin \phi_2 \cos \phi_1}{\sin(\phi_1 + \phi_2) \cos(\phi_1 - \phi_2)}$$



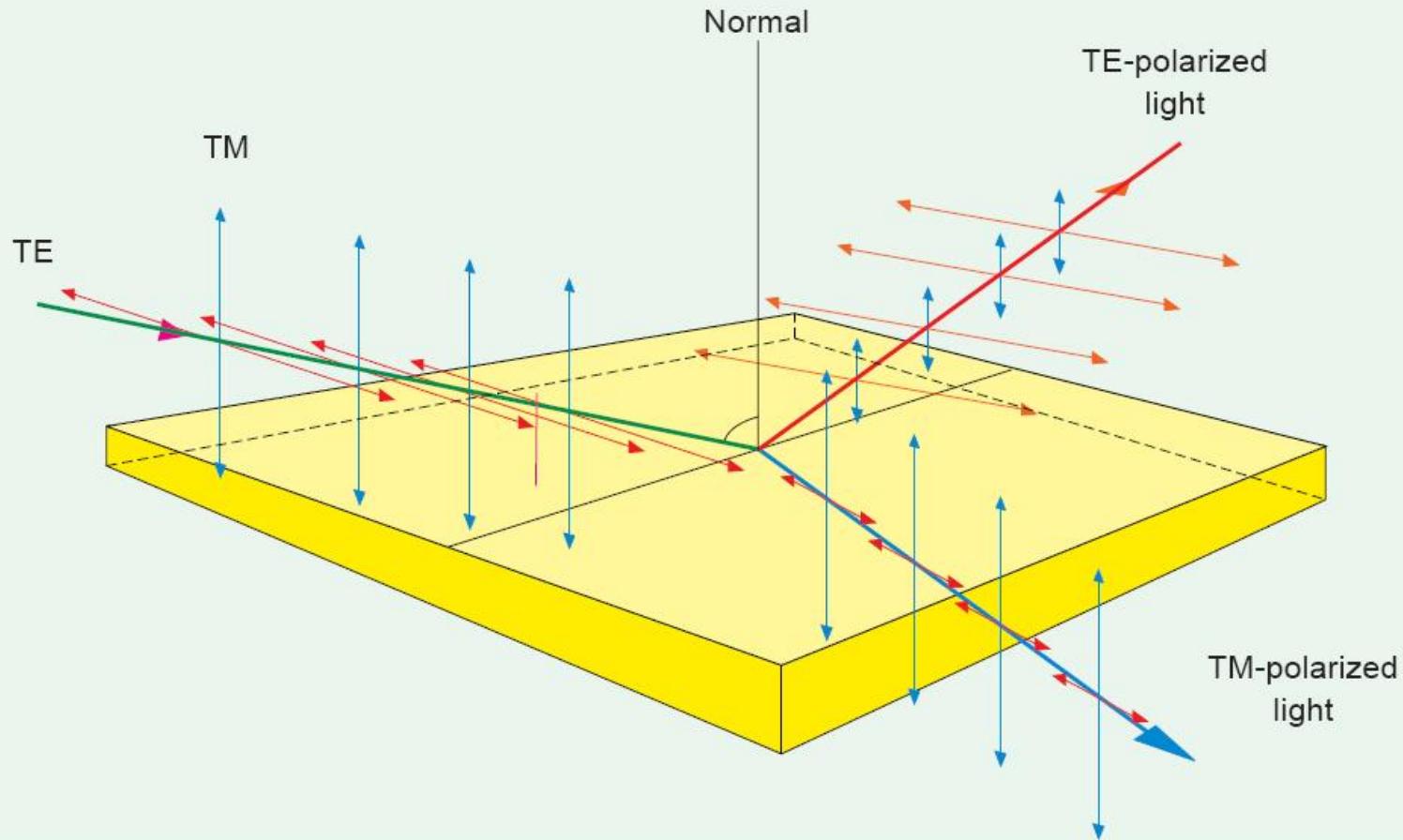
Unghi Brewster

$$r_p = 0 \Rightarrow \tan(\phi_1 + \phi_2) \rightarrow \infty \Rightarrow \phi_1 + \phi_2 = \frac{\pi}{2}$$

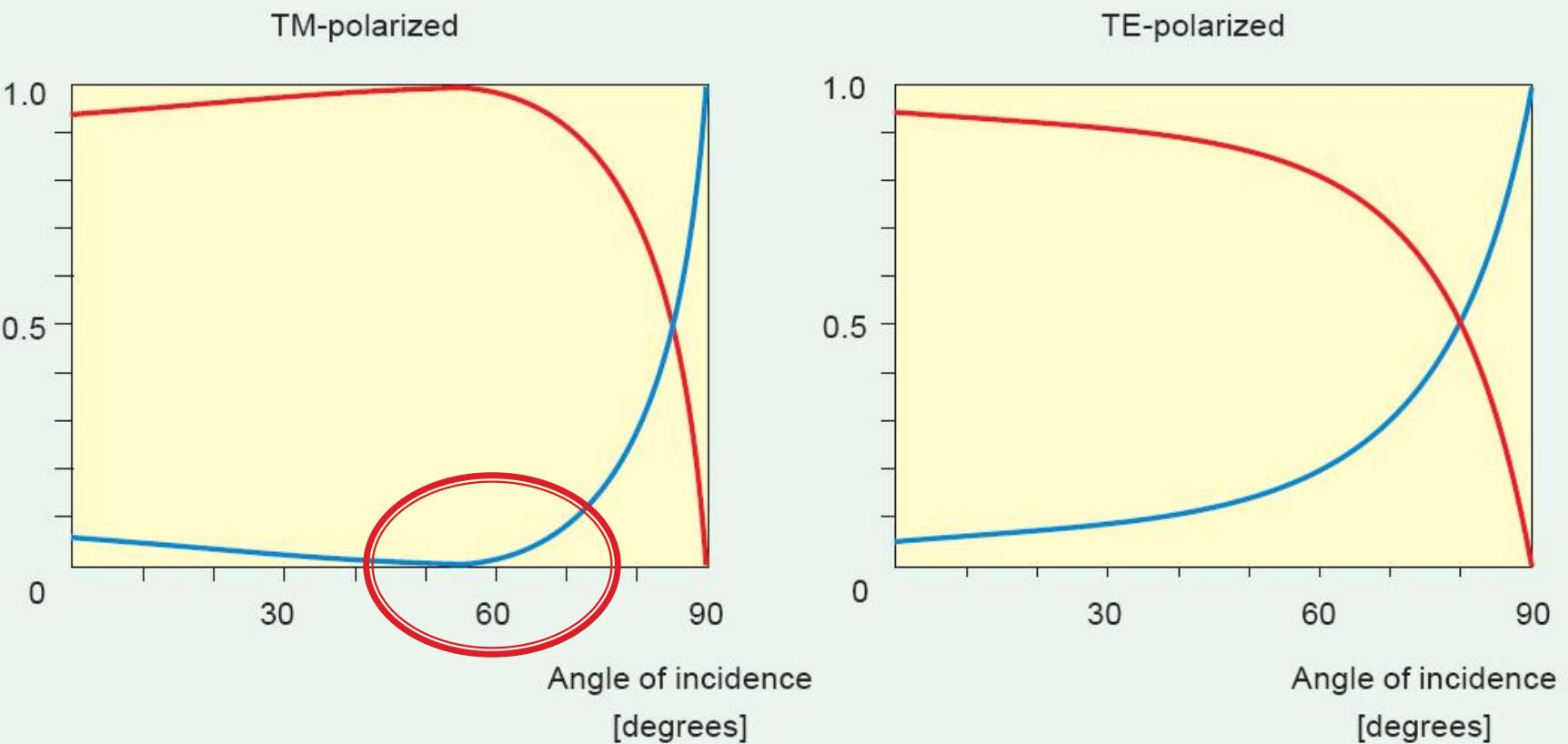
$$n_1 \cdot \sin \phi_1 = n_2 \cdot \sin \phi_2 = n_2 \cdot \cos \phi_1$$



Polarizarea luminii



Polarizarea luminii



Probleme

- ▶ Într-un LASER Fabry–Perrot, coerenta luminii este obtinuta prin reflexii successive ale luminii intre doua oglinzi paralele, separate de o distanta egală cu un multiplu a jumătate de lungime de undă ce se dorește emisă. Interferența constructivă și coerenta dintre lumina incidentă și reflectată asigură amplificarea numai a luminii care îndeplinește această condiție. Se dorește realizarea unei diode LASER cu lungimea de undă $\lambda_0 = 1305\text{nm}$ utilizând un material cu $\epsilon_{r1} = 10.80$.

$$\boxed{\lambda = \lambda(n)}$$

Probleme

- ▶ Care trebuie să fie distanța între oglinzi dacă se alege în aşa fel încât să corespundă la 380 jumătăți de lungime de undă? (1p)
- ▶ Dacă oglinda este realizată prin inserarea în material a unei lamele dintr-un dielectric cu $n_2 = 2.23$, ce procent din lumină incidentă părăsește zonă activă dintre cele două oglinzi la fiecare reflexie? (1p)
- ▶ Dacă în total se emit 3 linii spectrale corespunzătoare selectării luminii la care distanța dintre oglinzi calculată la a) este egală cu $(380 - 1)$, (380) , $(380 + 1)$ jumătăți de lungime de undă, care este lățimea spectrală în domeniul frecvență a diodei? Valoarea trebuie exprimată în GHz. (2p)
- ▶ Care este unghiul Brewster de obținere a luminii liniar polarizate pentru trecerea din materialul cu $\epsilon_{r1} = 10.80$ în aer. (1p)
- ▶ Rezolvări: <http://rf-opto.eti.tuiasi.ro>

$$\lambda = \lambda(n)$$

unghi Brewster

lamela dielectrică

Probleme

- ▶ Într-un material cu indicele de refracție $n_1 = 3.75$ se interpune un strat de material (2) cu $\epsilon_{r2} = 5.20$ pentru a realiza o oglindă parțial reflectantă la realizarea unui LASER cu $\lambda_0 = 950\text{nm}$. Înălțimea stratului (2) este aleasă pentru reflectivitate maximă la incidentă normală.
 - Care este înălțimea cea mai mică a stratului (2) pentru a obține acest efect? (2p)
 - Ce procent din puterea incidentă este întoarsă în materialul (1)? (1p)
 - O radiație care sosește cu înclinația de 41.2° față de normală la suprafața de separație, va trece din mediul (1) în mediul (2)? (1p)
- ▶ Rezolvari: <http://rf-opto.etti.tuiasi.ro>

lamela dielectrica

unghi critic

Contact

- ▶ Laboratorul de microunde si optoelectronica
- ▶ <http://rf-opto.etti.tuiasi.ro>
- ▶ rdamian@etti.tuiasi.ro